

# Quiz #1

2008.10.01

1. (15) Calculate  $\int_C \vec{F}(\vec{r}) \cdot d\vec{r}$  for the following data. If  $\vec{F}$  is a force, this gives the work done in the displacement along C.

$$\vec{F} = [\cosh x, \sinh y, e^z], \quad C: r = [t, t^2, t^3] \quad \text{from } (0, 0, 0) \text{ to } \left(\frac{1}{2}, \frac{1}{4}, \frac{1}{8}\right)$$

2. (15) Using Green's theorem, evaluate  $\int_C \vec{F}(\vec{r}) \cdot d\vec{r}$  counterclockwise around the boundary curve C of the region R.

$$\vec{F} = [-e^y, e^x], \quad R \text{ the triangle with vertices } (0, 0), (2, 0), (2, 1)$$

3. (10) Evaluate the integral  $\iint_S (\nabla \times \vec{F}) \cdot \vec{n} dA$  directly for the given  $\vec{F}$  and S.

$$\vec{F} = [4z^2, 16x, 0], \quad S: z = y \quad (0 \leq x \leq 1, 0 \leq y \leq 1)$$