

K- Language v0.2

1 Semantics

$$\begin{aligned} n &\in \mathbb{Z} \\ b &\in \mathbb{B} = \{T, F\} \\ v &\in Val = \mathbb{Z} + \mathbb{B} + \{\cdot\} \\ \sigma &\in Env = Id \rightarrow Addr \\ M &\in Mem = Addr \rightarrow Val \end{aligned}$$

$$\overline{\sigma, M \vdash \text{NUM } (n) \Downarrow n, M}$$

$$\overline{\sigma, M \vdash \text{TRUE} \Downarrow T, M}$$

$$\overline{\sigma, M \vdash \text{FALSE} \Downarrow F, M}$$

$$\overline{\sigma, M \vdash \text{UNIT} \Downarrow \cdot, M}$$

$$\overline{\sigma, M \vdash \text{VAR } x \Downarrow v, M} M(\sigma(x)) = v$$

$$\frac{\sigma, M \vdash E_1 \Downarrow n_1, M_1 \quad \sigma, M_1 \vdash E_2 \Downarrow n_2, M_2}{\sigma, M \vdash \text{ADD } (E_1, E_2) \Downarrow n, M_2} n = n_1 + n_2$$

$$\frac{\sigma, M \vdash E_1 \Downarrow n_1, M_1 \quad \sigma, M_1 \vdash E_2 \Downarrow n_2, M_2}{\sigma, M \vdash \text{SUB } (E_1, E_2) \Downarrow n, M_2} n = n_1 - n_2$$

$$\frac{\sigma, M \vdash E_1 \Downarrow n_1, M_1 \quad \sigma, M_1 \vdash E_2 \Downarrow n_2, M_2}{\sigma, M \vdash \text{MUL } (E_1, E_2) \Downarrow n, M_2} n = n_1 \times n_2$$

$$\frac{\sigma, M \vdash E_1 \Downarrow n_1, M_1 \quad \sigma, M_1 \vdash E_2 \Downarrow n_2, M_2}{\sigma, M \vdash \text{DIV } (E_1, E_2) \Downarrow n, M_2} n = n_1 \div n_2$$

$$\frac{\sigma, M \vdash E_1 \Downarrow n_1, M_1 \quad \sigma, M_1 \vdash E_2 \Downarrow n_2, M_2}{\sigma, M \vdash \mathbf{EQUAL} (E_1, E_2) \Downarrow T, M_2} n_1 = n_2$$

$$\frac{\sigma, M \vdash E_1 \Downarrow n_1, M_1 \quad \sigma, M_1 \vdash E_2 \Downarrow n_2, M_2}{\sigma, M \vdash \mathbf{EQUAL} (E_1, E_2) \Downarrow F, M_2} n_1 \neq n_2$$

$$\frac{\sigma, M \vdash E_1 \Downarrow b_1, M_1 \quad \sigma, M_1 \vdash E_2 \Downarrow b_2, M_2}{\sigma, M \vdash \mathbf{EQUAL} (E_1, E_2) \Downarrow T, M_2} b_1 = b_2$$

$$\frac{\sigma, M \vdash E_1 \Downarrow b_1, M_1 \quad \sigma, M_1 \vdash E_2 \Downarrow b_2, M_2}{\sigma, M \vdash \mathbf{EQUAL} (E_1, E_2) \Downarrow F, M_2} b_1 \neq b_2$$

$$\frac{\sigma, M \vdash E_1 \Downarrow \cdot, M_1 \quad \sigma, M_1 \vdash E_2 \Downarrow \cdot, M_2}{\sigma, M \vdash \mathbf{EQUAL} (E_1, E_2) \Downarrow T, M_2}$$

$$\frac{\sigma, M \vdash E_1 \Downarrow n_1, M_1 \quad \sigma, M_1 \vdash E_2 \Downarrow n_2, M_2}{\sigma, M \vdash \mathbf{LESS} (E_1, E_2) \Downarrow T, M_2} n_1 < n_2$$

$$\frac{\sigma, M \vdash E_1 \Downarrow n_1, M_1 \quad \sigma, M_1 \vdash E_2 \Downarrow n_2, M_2}{\sigma, M \vdash \mathbf{LESS} (E_1, E_2) \Downarrow F, M_2} n_1 \geq n_2$$

$$\frac{\sigma, M \vdash E_1 \Downarrow T, M_1 \quad \sigma, M_1 \vdash E_2 \Downarrow T, M_2}{\sigma, M \vdash \mathbf{LESS} (E_1, E_2) \Downarrow F, M_2}$$

$$\frac{\sigma, M \vdash E_1 \Downarrow T, M_1 \quad \sigma, M_1 \vdash E_2 \Downarrow F, M_2}{\sigma, M \vdash \mathbf{LESS} (E_1, E_2) \Downarrow F, M_2}$$

$$\frac{\sigma, M \vdash E_1 \Downarrow F, M_1 \quad \sigma, M_1 \vdash E_2 \Downarrow T, M_2}{\sigma, M \vdash \mathbf{LESS} (E_1, E_2) \Downarrow T, M_2}$$

$$\frac{\sigma, M \vdash E_1 \Downarrow F, M_1 \quad \sigma, M_1 \vdash E_2 \Downarrow F, M_2}{\sigma, M \vdash \mathbf{LESS} (E_1, E_2) \Downarrow F, M_2}$$

$$\frac{\sigma, M \vdash E_1 \Downarrow \cdot, M_1 \quad \sigma, M_1 \vdash E_2 \Downarrow \cdot, M_2}{\sigma, M \vdash \mathbf{LESS} (E_1, E_2) \Downarrow F, M_2}$$

$$\frac{\sigma, M \vdash E \Downarrow T, M_1}{\sigma, M \vdash \mathbf{NOT} E \Downarrow F, M_1} \quad \frac{\sigma, M \vdash E \Downarrow F, M_1}{\sigma, M \vdash \mathbf{NOT} E \Downarrow T, M_1}$$

$$\frac{\sigma, M \vdash E \Downarrow v, M_1}{\sigma, M \vdash \mathbf{ASSIGN} (x, E) \Downarrow \cdot, M_1[v/\sigma(x)]}$$

$$\frac{\sigma, M \vdash E_1 \Downarrow v_1, M_1 \quad \sigma, M_1 \vdash E_2 \Downarrow v_2, M_2}{\sigma, M \vdash \mathbf{SEQ} (E_1, E_2) \Downarrow v_2, M_2}$$

$$\begin{array}{c}
\frac{\sigma, M \vdash E_1 \Downarrow T, M_1 \quad \sigma, M_1 \vdash E_2 \Downarrow v, M_2}{\sigma, M \vdash \text{IF2} (E_1, E_2, E_3) \Downarrow \cdot, M_2} \\
\\
\frac{\sigma, M \vdash E_1 \Downarrow F, M_1 \quad \sigma, M_1 \vdash E_3 \Downarrow v, M_2}{\sigma, M \vdash \text{IF2} (E_1, E_2, E_3) \Downarrow \cdot, M_2} \\
\\
\frac{\sigma, M \vdash E_1 \Downarrow T, M_1 \quad \sigma, M_1 \vdash E_2 \Downarrow v, M_2}{\sigma, M \vdash \text{IF1} (E_1, E_2) \Downarrow \cdot, M_2} \quad \frac{\sigma, M \vdash E_1 \Downarrow F, M_1}{\sigma, M \vdash \text{IF1} (E_1, E_2) \Downarrow \cdot, M_1} \\
\\
\frac{\sigma, M \vdash E_1 \Downarrow T, M_1 \quad \sigma, M_1 \vdash E_2 \Downarrow v, M_2 \quad \sigma, M_2 \vdash \text{WHILE} (E_1, E_2) \Downarrow \cdot, M_3}{\sigma, M \vdash \text{WHILE} (E_1, E_2) \Downarrow \cdot, M_3} \\
\\
\frac{\sigma, M \vdash E_1 \Downarrow F, M_1}{\sigma, M \vdash \text{WHILE} (E_1, E_2) \Downarrow \cdot, M_1} \\
\\
\frac{\sigma, M \vdash E_1 \Downarrow n_1, M_1 \quad \sigma, M_1 \vdash E_2 \Downarrow n_2, M_2 \quad \sigma, M_2[n_1/\sigma(x)] \vdash E_3 \Downarrow v, M_3 \quad \sigma, M_3 \vdash \text{FOR} (x, n_1 + 1, E_2, E_3) \Downarrow \cdot, M_4}{\sigma, M \vdash \text{FOR} (x, E_1, E_2, E_3) \Downarrow \cdot, M_4} n_1 \leq n_2 \\
\\
\frac{\sigma, M \vdash E_1 \Downarrow n_1, M_1 \quad \sigma, M_1 \vdash E_2 \Downarrow n_2, M_2}{\sigma, M \vdash \text{FOR} (x, E_1, E_2, E_3) \Downarrow \cdot, M_2} n_1 > n_2 \\
\\
\frac{\sigma, M \vdash E_1 \Downarrow v_1, M_1 \quad \sigma[l/x], M_1[v_1/l] \vdash E_2 \Downarrow v_2, M_2}{\sigma, M \vdash \text{LET} (x, E_1, E_2) \Downarrow v_2, M_2} l \notin \text{dom}(M_1) \\
\\
\frac{\text{Read } n}{\sigma, M \vdash \text{READ } x \Downarrow \cdot, M[n/\sigma(x)]} \quad \frac{}{\text{Read } n} \\
\\
\frac{\sigma, M \vdash E \Downarrow n, M_1 \quad \text{Write } n}{\sigma, M \vdash \text{WRITE } E \Downarrow \cdot, M_1} \quad \frac{}{\text{Write } n}
\end{array}$$