## SEOUL NATIONAL UNIVERSITY SCHOOL OF MECHANICAL AND AEROSPACE ENGINEERING

SYSTEM ANALYSIS Spring 2014

HW#4

Assigned: March 26 (We)

Due: April 7 (Mo)

1. Obtain the state model for the transfer function model

$$\frac{Y(s)}{u(s)} = \frac{6}{3s^2 + 6s + 10}$$

2. Obtain the state model for the system of the following equations of motion

$$10\ddot{x}_1 + 8\dot{x}_1 - 5\dot{x}_2 + 40x_1 - 25x_2 = 0$$
  
$$5\ddot{x}_2 - 25x_1 + 25x_2 - 5\dot{x}_1 + 5\dot{x}_2 = u(t)$$

- 3. A representation of car's suspension suitable for modeling the bounce and pitch motion is shown in Figure below, which is a side view of the vehicle's body showing the front and rear suspensions. The bid mass is m and its moment of inertia about the mass center is  $I_G$ . As usual,  $\mathcal{X}$  and  $\theta$  are the displacements from the equilibrium position corresponding to  $y_1 = y_2 = 0$ .
- (1) Assume that  $\mathcal{X}$  and  $\theta$  are small, and derive the equations of motion for the bounce motion  $\mathcal{X}$  and the pitch motion  $\theta$ .
  - (2) Obtain state-variable model.
- (3) Use matlab to obtain and plot the solution for x(t) and  $\theta(t)$  when  $y_1(t) = 0$  and  $y_2(t) = \delta(t)$ . The initial conditions are zero.

