

# Fully Coupled Constitutive Model for Electrostrictive Ceramic Materials -Hom and Shankar

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# Adaptive Structure

## ❖ Active smart materials system

- { Sensors ... to detect changes in environment
- { actuators ... used in a feedback loop to respond to those changes

## ❖ Most common ceramic materials

- Piezoelectrics ... based on lead zirconate titanate  $Pb(Zr,Ti)O_3$ 
  - can convert electrical energy into small but accurate displacements with a fast response time
  - more compact, consume less power, less prone to overheating
  - can detect minute displacements by converting mechanical work into electrical energy

# Adaptive Structure

- electrostrictive ceramics
  - generally offer higher electrically induced strains with lower hysteresis
  - but with the penalties of complicated electromechanical behavior and temperature dependency
  - electromechanical coupling efficiency for electrostrictors is comparable to that for piezoelectrics
- $\left\{ \begin{array}{l} \text{piezoelectrics} \\ \text{electrostrictor} \end{array} \right\} \rightarrow$  belong to a class of ionic crystals known as ferroelectrics
- Ferroelectrics ... consist of subvolumes, called domains that have a uniform, permanent, reorientable polarization
- direction of polarization for each domain is randomly oriented  $\rightarrow$  the crystal itself has no net bulk polarization

# Adaptive Structure

- Above a characteristic temperature (the Curie temperature), a ferroelectric undergoes a transition where the spontaneous polarization disappears
- Piezoelectricity is induced in a ferroelectric ceramic by applying a high electric field at elevated temperatures during manufacture → “poling” process
  - partially aligns the polar axes of the domains to create a macroscopic polarization in the crystal.
- The resulting piezoelectric will deform when subjected to an electric field and polarize when mechanically stressed
  - for low electric field [ $< 0.1 \text{ MV} / \text{m}$  for  $\text{Pb}(\text{Zr}, \text{Ti}) \text{O}_3$ ]
    - electrically induced strain  $\propto$  the applied field
    - electric field  $\propto$  induced polarization
  - For higher AC fields [ $> 0.6 \sim 1.1 \text{ MV} / \text{m}$  *peak – peak*]
    - significant electromechanical hysteresis
    - can create servo-displacement control problems

# Adaptive Structure

## ❖ Electrostriction

- induced strain  $\propto$  (induced polarization)<sup>2</sup>
- the same deformation occurs when the field is reversed, in contrast to piezoelectricity
- relaxor – ferroelectrics can exhibit large electrostrictive strains
- spontaneous polarization is not suddenly lost at a specific Curie temperature but slowly decays with increasing temperature
- significant electrostriction with minimal hysteresis is possible both above and below the nominal transition temperature
- most promising relaxor – ferroelectrics materials ... lead magnesium niobate  
 $Pb(Mg_{1/3} Nb_{2/3}) O_3 (PMN)$ , or its solid relations with lead titanate  
 $Pb(Mg_{1/3} Nb_{2/3}) O_3 - PbTiO_3 (PMN - PT)$
- high electrically-induced strains ( $\sim 0.1\%$ ) and low hysteresis ( $< 5\%$ ) over moderate electric fields ( $\sim 1 \text{ MV} / \text{m peak} - \text{peak}$ )