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$$G = \sqrt{\frac{P}{\mu V}}$$

$$\Rightarrow P = G^2 \mu V$$

$$\begin{aligned} \text{@ } 15^\circ\text{C: } P &= (100/s)^2 \times (1.139 \times 10^{-3} \text{ N} - s/m) \times (2800 \text{ m}^3) = 31900 \text{ W} \\ &= 31.9 \text{ kW} \end{aligned}$$

$$\begin{aligned} \text{@ } 5^\circ\text{C: } P &= (100/s)^2 \times (1.518 \times 10^{-3} \text{ N} - s/m) \times (2800 \text{ m}^3) = 42500 \text{ W} \\ &= 42.5 \text{ kW} \end{aligned}$$

Results indicate that as temperature ↓, viscosity ↑, so more power input is required for the same intensity of mixing

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i) $10^{-4} \text{ m} = 0.1 \text{ mm}$

a) Determine $v_{p(t)}$ using Stoke's law

$$\begin{aligned}v_{p(t)} &= \frac{g(\rho_p - \rho_w)d_p^2}{18\mu} = \frac{9.81 \text{ m/s}^2 \cdot (1.050 - 0.998) \times 10^3 \text{ kg/m}^3 \cdot (10^{-4} \text{ m})^2}{18 \cdot (1.002 \times 10^{-3} \text{ N} \cdot \text{s/m}^2)} \\ &= 2.83 \times 10^{-4} \text{ m/s}\end{aligned}$$

b) Check N_R

$$N_R = \frac{v_p d_p \rho_w}{\mu} = \frac{(2.83 \times 10^{-4} \text{ m/s}) \cdot (10^{-4} \text{ m}) \cdot (0.998 \times 10^3 \text{ kg/m}^3)}{1.002 \times 10^{-3} \text{ N} \cdot \text{s/m}^2} = 0.028$$

⇒ $N_R < 1$, so Stoke's law applies as assumed.

So, $v_{p(t)} = 2.83 \times 10^{-4} \text{ m/s}$

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ii) $10^{-3} \text{ m} = 1 \text{ mm}$

a) Determine $v_{p(t)}$ using Stoke's law

$$\begin{aligned} v_{p(t)} &= \frac{g(\rho_p - \rho_w)d_p^2}{18\mu} = \frac{9.81 \text{ m/s}^2 \cdot (1.050 - 0.998) \times 10^3 \text{ kg/m}^3 \cdot (10^{-3} \text{ m})^2}{18 \cdot (1.002 \times 10^{-3} \text{ N} \cdot \text{s/m}^2)} \\ &= 2.83 \times 10^{-2} \text{ m/s} \end{aligned}$$

b) Check N_R

$$N_R = \frac{v_p d_p \rho_w}{\mu} = \frac{(2.83 \times 10^{-2} \text{ m/s}) \cdot (10^{-3} \text{ m}) \cdot (0.998 \times 10^3 \text{ kg/m}^3)}{1.002 \times 10^{-3} \text{ N} \cdot \text{s/m}^2} = 28$$

⇒ $N_R > 1$, so Stoke's law cannot be applied.

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ii) $10^{-3} \text{ m} = 1 \text{ mm}$) Use the N_R calculated and apply the transient region solution

$$C_D = \frac{24}{N_R} + \frac{3}{\sqrt{N_R}} + 0.34 = \frac{24}{28} + \frac{3}{\sqrt{28}} = 1.76$$

$$v_{p(t)} = \sqrt{\frac{4g}{3C_D} \left(\frac{\rho_p - \rho_w}{\rho_w} \right) d_p} = \sqrt{\frac{4 \cdot 9.81 \text{ m/s}^2}{3 \cdot 1.76} \left(\frac{1.050 - 0.998}{0.998} \right) \cdot 10^{-3} \text{ m}}$$
$$= 1.97 \times 10^{-2} \text{ m/s}$$

The result does not match with the $v_{p(t)}$ used to get N_R (Stoke's solution – $2.83 \times 10^{-2} \text{ m/s}$)

Have to assume a smaller $v_{p(t)}$

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d) Assume $v_{p(t)}$, calculate NR , then calculate CD , then calculate $v_{p(t)}$ until assumed $v_{p(t)} = \text{calculated } v_{p(t)}$

Eventually, if you assume $v_{p(t)} = 1.7 \times 10^{-2} \text{ m/s}$,

$$N_R = \frac{v_p d_p \rho_w}{\mu} = \frac{(1.7 \times 10^{-2} \text{ m/s}) \cdot (10^{-3} \text{ m}) \cdot (0.998 \times 10^3 \text{ kg/m}^3)}{1.002 \times 10^{-3} \text{ N} \cdot \text{s/m}^2} = 16.9$$

$$C_D = \frac{24}{N_R} + \frac{3}{\sqrt{N_R}} + 0.34 = \frac{24}{16.9} + \frac{3}{\sqrt{16.9}} = 2.49$$

$$v_{p(t)} = \sqrt{\frac{4g}{3C_D} \left(\frac{\rho_p - \rho_w}{\rho_w} \right) d_p} = \sqrt{\frac{4 \cdot 9.81 \text{ m/s}^2 \left(\frac{1.050 - 0.998}{0.998} \right) \cdot 10^{-3} \text{ m}}{3 \cdot 2.49}}$$

$= 1.65 \times 10^{-2} \text{ m/s}$ (close to the assumption)

So, $v_{p(t)} \approx 1.7 \times 10^{-2} \text{ m/s}$

You may use computer software (e.g, Excel “find solution” function) to automate the calculation!