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# Overview of Transmit Diversity

이 광복

이동통신연구실

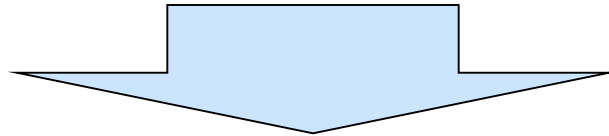
서울대학교

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# Introduction

- Fading
  - Fluctuation of Received SNR
- Diversity
  - Reduce the fluctuation of Received SNR
  - Time, Space(antenna), Frequency, Polarization
- Antenna Diversity
  - Conventional System: Receiver Diversity
  - Multiple mobile antennas: 구현어려움
  - Future system: Forward Traffic량 증가



## Transmit Diversity

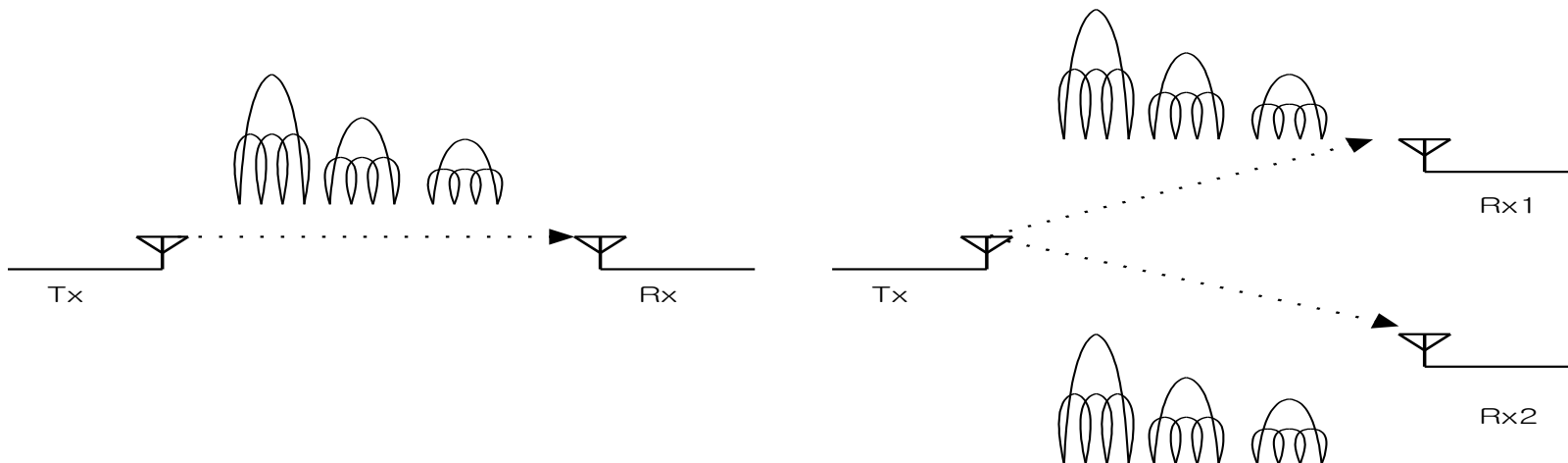
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## Introduction(cont'd)

- Transmit Diversity in 3GPP
  - Space-Time Transmit Diversity(STTD)
  - Orthogonal Transmit Diversity(OTD)
  - Time Switched Transmit Diversity(TSTD)
  - Transmit Antenna Array(TxAA)
- STTD, OTD, TSTD
  - Open Loop: No feedback information
- TxAA
  - Closed Loop: Feedback information
- Base selection Tx Div
- MIMO

# RAKE & Rx Antenna Diversity



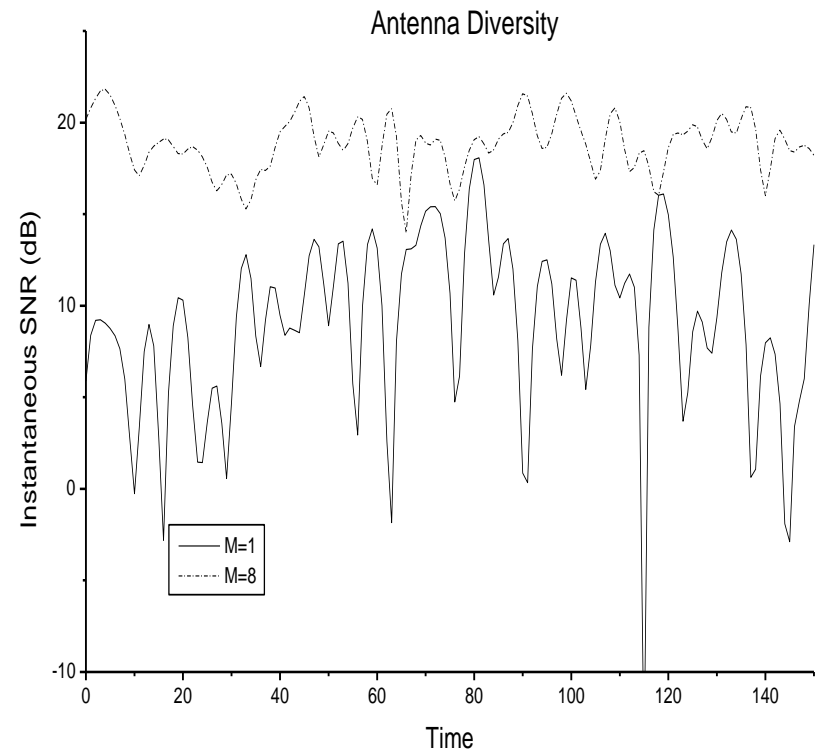
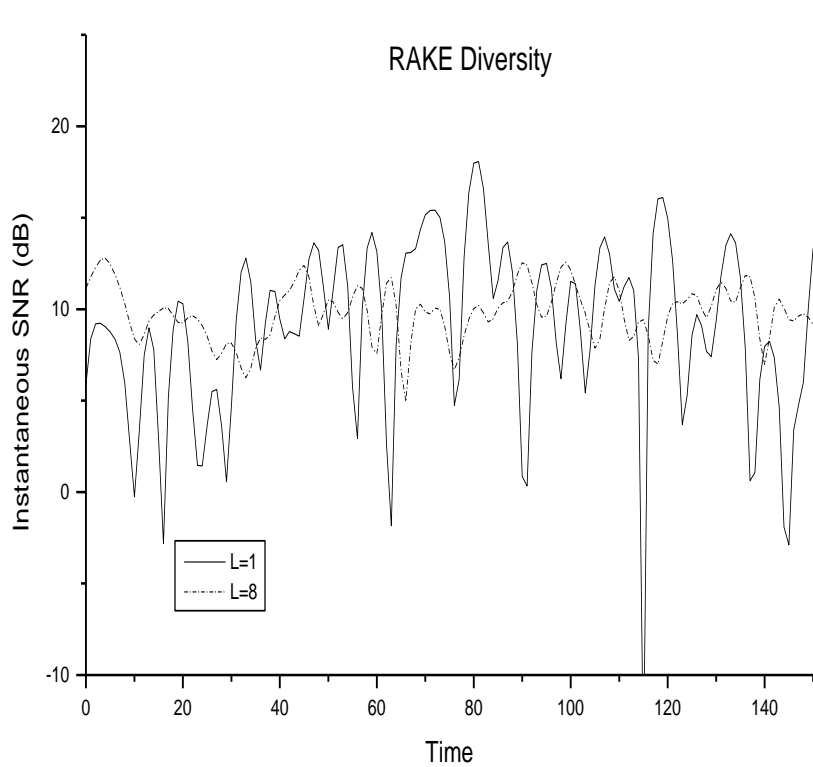
## RAKE

- Diversity Order  $\propto L$
- Average SNR Gain = 0

## Rx Antenna

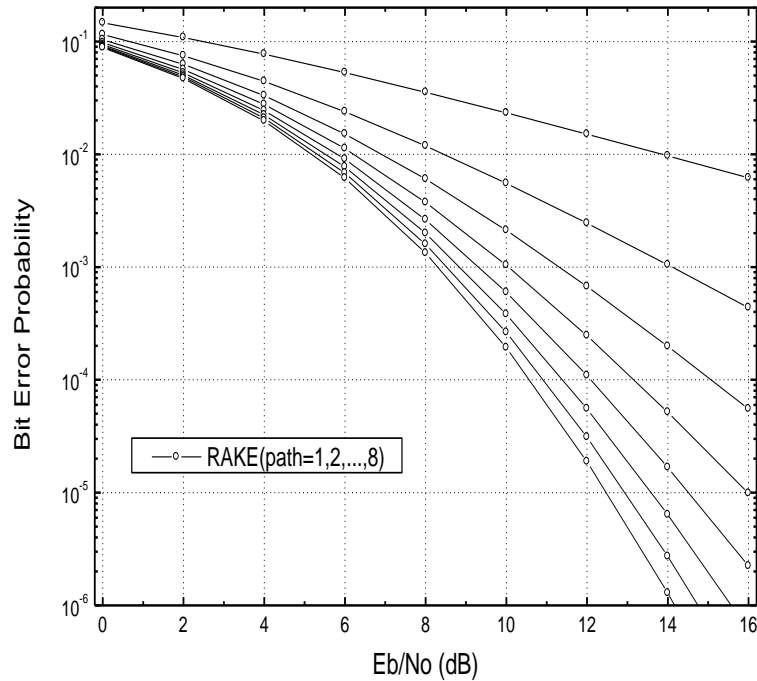
- Diversity Order  $\propto M \cdot L$
- Average SNR Gain  $\propto M$

# Performance of Rx Diversity



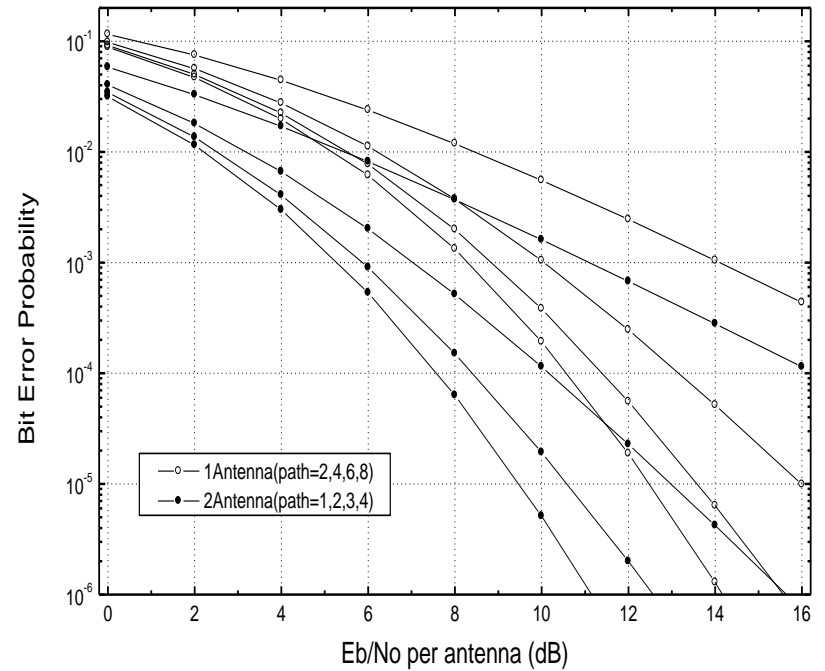
# Performance of Rx Diversity(cont'd)

## <RAKE>



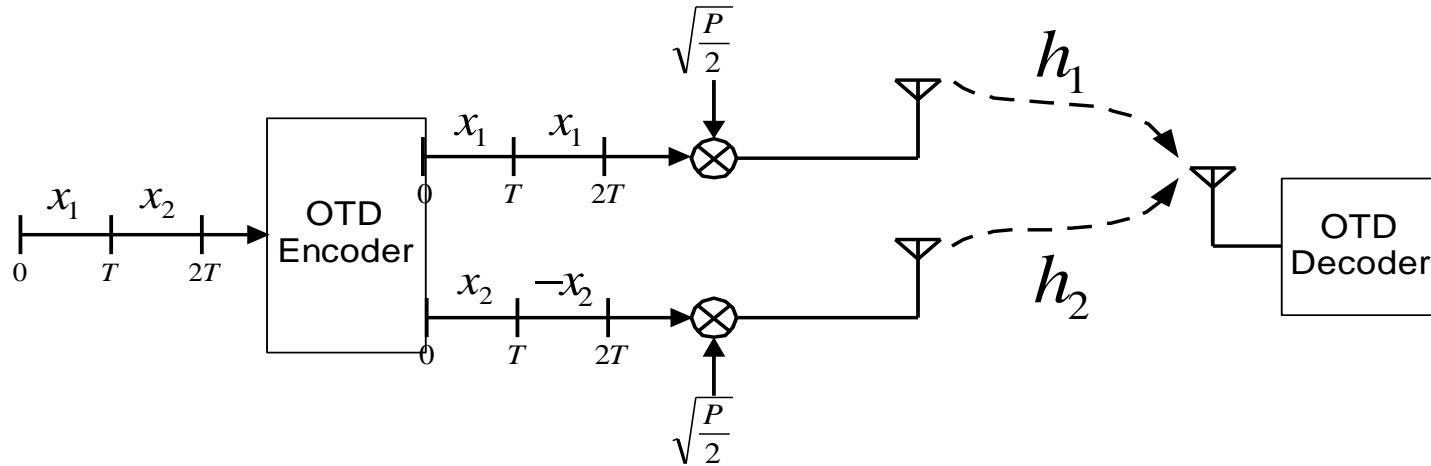
- Diversity Order  $\propto L$
- Average SNR Gain = 0

## <Antenna+RAKE>



- Diversity Order  $\propto M \cdot L$
- Average SNR Gain  $\propto M$

# Orthogonal Transmit Diversity (OTD)



- OTD Encoder:

	Time 1	Time 2
Ant. 1	$x_1$	$x_1$
Ant. 2	$x_2$	$-x_2$

- Received Signal:

$$r_1 = \sqrt{\frac{P}{2}} (h_1 x_1 + h_2 x_2) + n_1$$

$$r_2 = \sqrt{\frac{P}{2}} (h_1 x_1 - h_2 x_2) + n_2$$

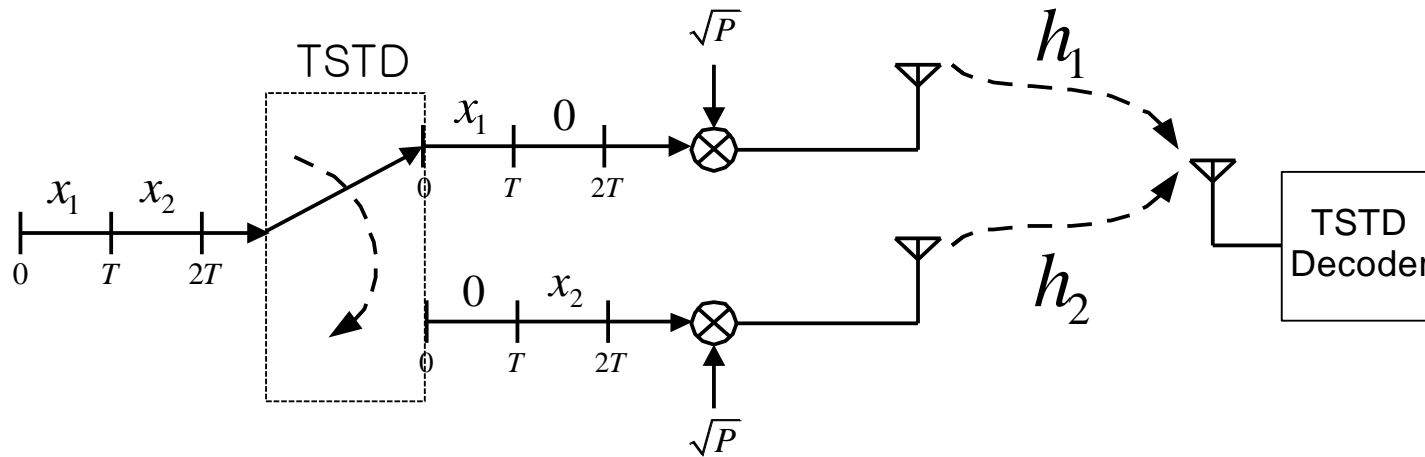
- OTD Decoder:

$$\hat{x}_1 = h_1^* (r_1 + r_2) = \sqrt{2P} |h_1|^2 x_1 + \eta_1$$

$$\hat{x}_2 = h_2^* (r_1 - r_2) = \sqrt{2P} |h_2|^2 x_2 + \eta_2$$

- Different Symbol  $\rightarrow$  Different Fading
- Interleaving Effects
- Useful at Slow Fading Environment

# Time Switched Transmit Diversity (TSTD)



- TSTD Encoder:

	Time 1	Time 2
Ant. 1	$x_1$	$0$
Ant. 2	$0$	$x_2$

- Received Signal:

$$r_1 = \sqrt{P} (h_1 x_1) + n_1$$

$$r_2 = \sqrt{P} (h_2 x_2) + n_2$$

- TSTD Decoder:

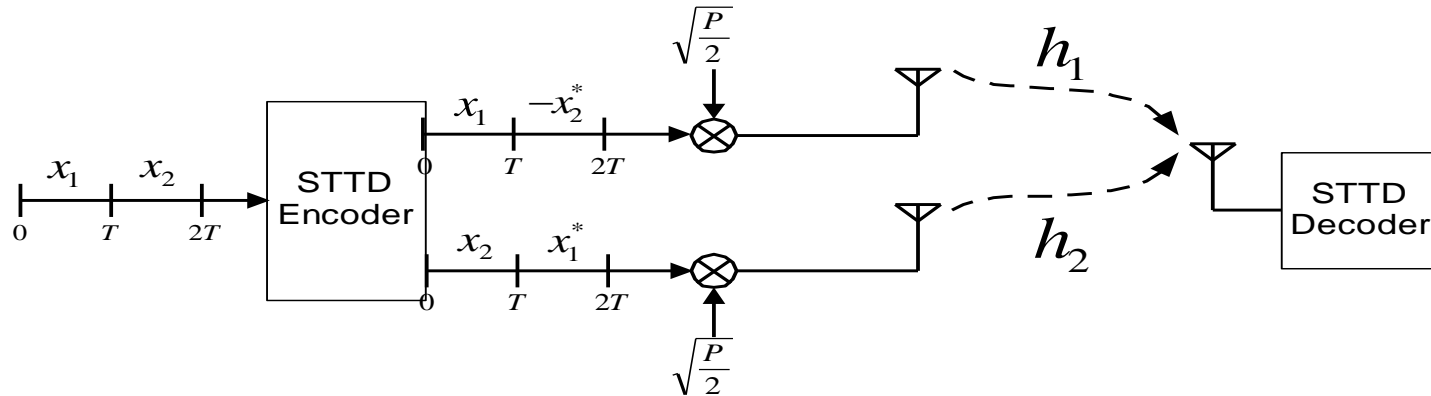
$$\hat{x}_1 = h_1^* \cdot r_1 = \sqrt{P} |h_1|^2 x_1 + \eta_1$$

$$\hat{x}_2 = h_2^* \cdot r_2 = \sqrt{P} |h_2|^2 x_2 + \eta_2$$

- Different Symbol  $\rightarrow$  Different Fading
- Interleaving Effects
- Useful at Slow Fading Environment



# Space-Time Transmit Diversity (STTD)



- STTD Encoder:

	Time 1	Time 2
Ant. 1	$x_1$	$-x_2^*$
Ant. 2	$x_2$	$x_1^*$

- Received Signal:

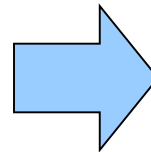
$$r_1 = \sqrt{\frac{P}{2}} (h_1 x_1 + h_2 x_2) + n_1$$

$$r_2 = \sqrt{\frac{P}{2}} (-h_1 x_2^* + h_2 x_1^*) + n_2$$

- STTD Decoder:

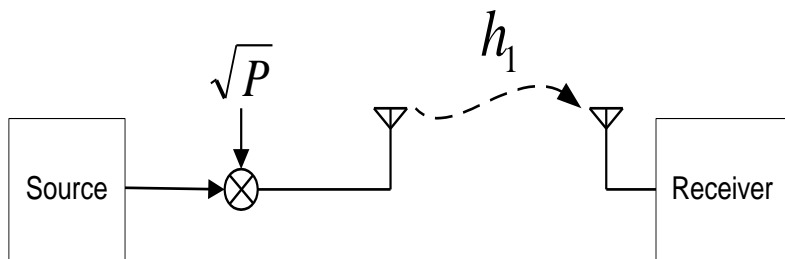
$$\hat{x}_1 = r_1 h_1^* + r_2^* h_2 = \sqrt{\frac{P}{2}} (|h_1|^2 + |h_2|^2) x_1 + \eta_1$$

$$\hat{x}_2 = r_1 h_2^* - r_2^* h_1 = \sqrt{\frac{P}{2}} (|h_1|^2 + |h_2|^2) x_2 + \eta_2$$

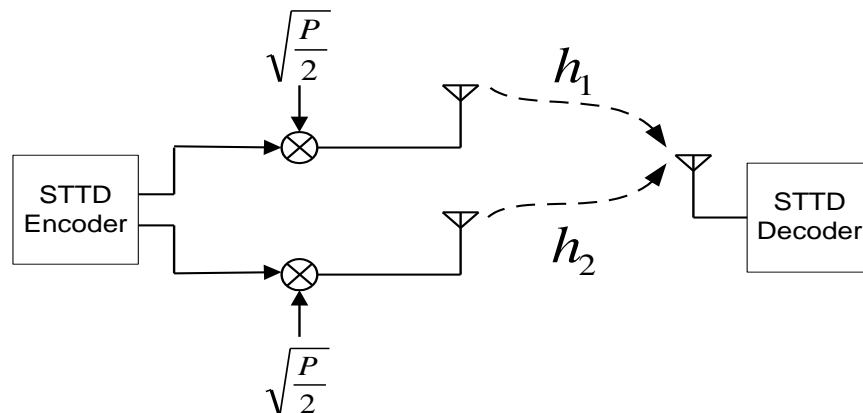


**Diversity**  
without BW Expansion

# No Tx Diversity VS STTD

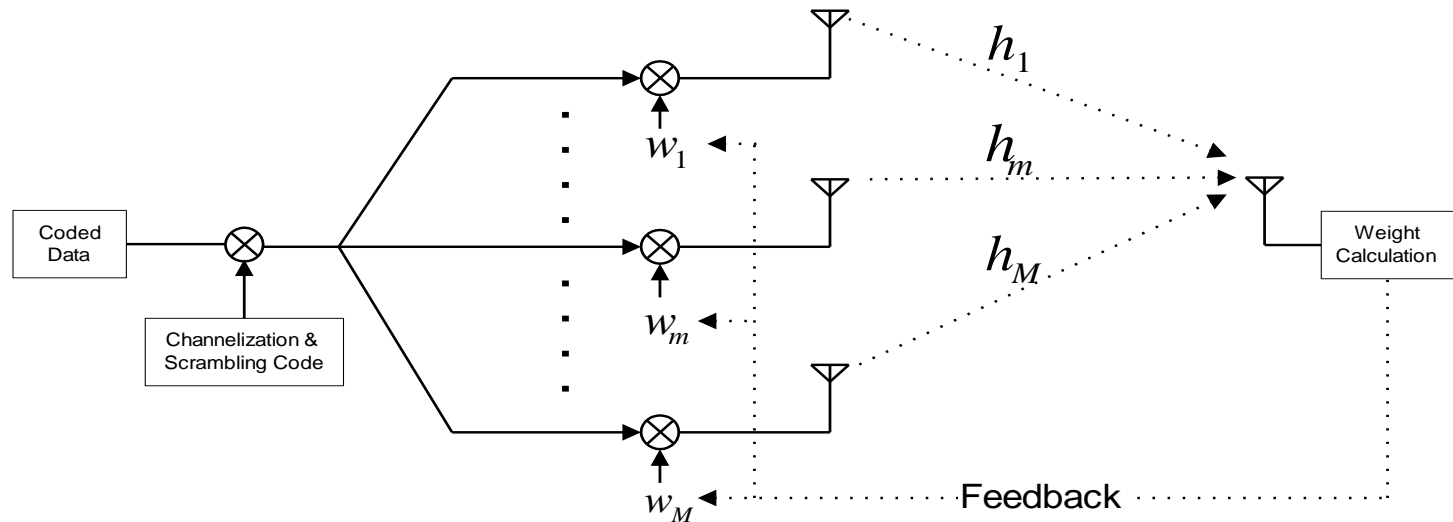


- Tx. Power =  $P$
- SNR:  $\gamma \propto P \cdot |h_1|^2$
- Avg. SNR:  $\gamma \propto P \cdot \sigma_0^2$
- Average SNR Gain = 0
- Diversity Order = 1



- Tx. Power =  $P$
- SNR:  $\gamma \propto \frac{P}{2} \cdot \{|h_1|^2 + |h_2|^2\}$
- Avg. SNR:  $\gamma \propto P \cdot \sigma_0^2$
- Average SNR Gain = 0
- Diversity Order = 2

# Transmit Antenna Array (TxAA)



- Weighting

$$w_m = \frac{h_m^*}{\sqrt{\sum_{i=1}^M |h_i|^2}}$$

- Received signal

$$r = \left( \sum_{m=1}^M w_m h_m \right) x + n$$

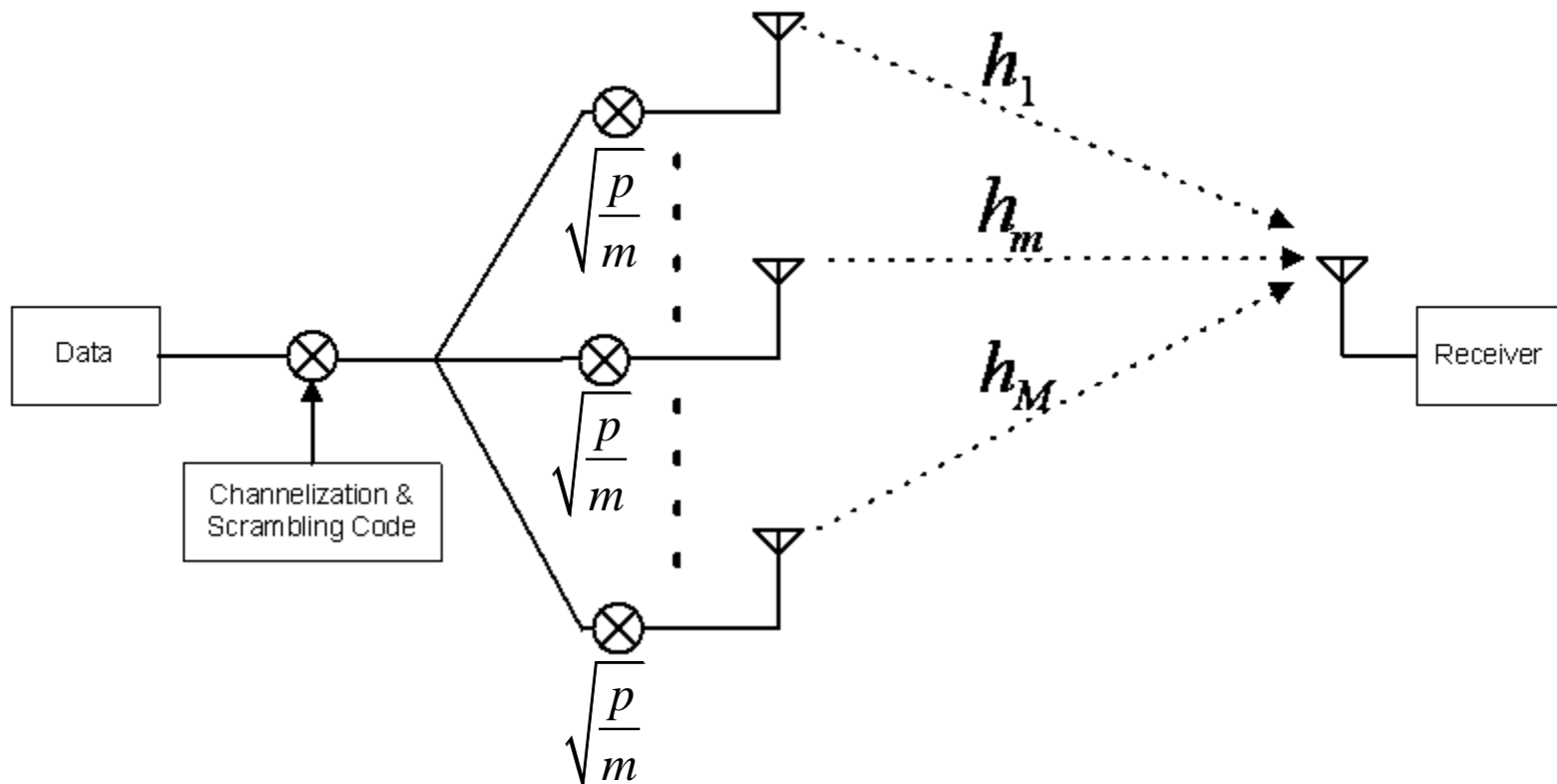
$$= x \sqrt{\sum_{m=1}^M |h_m|^2} + n$$

- SNR

$$\gamma \propto \sum_{m=1}^M |h_m|^2$$

- Diversity Order  $\propto M$
- Average SNR Gain  $\propto M$

# Transmit Diversity



- Performance ???

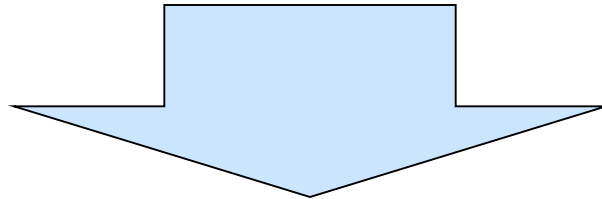
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Efficient Weight Vector  
Representation  
(***Basis Selection***)

## Basis selection Tx Div

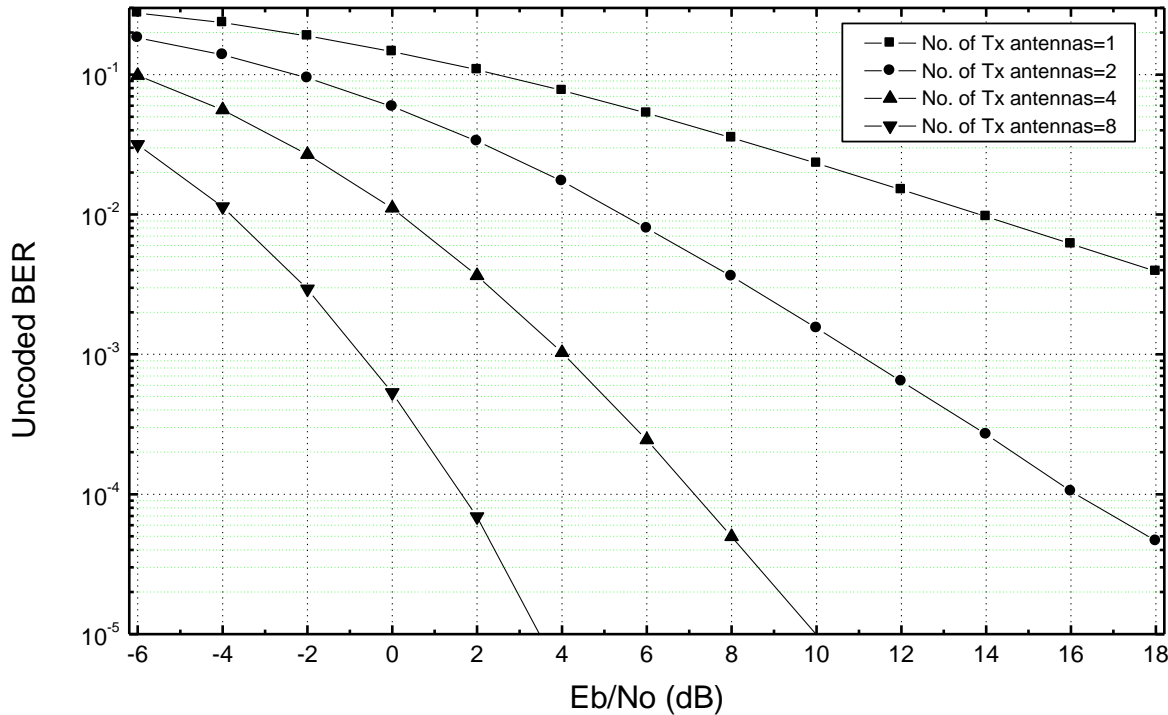
- STTD: Open Loop
  - 장점: No Feedback Information
  - 단점: 확장성( $M > 20$  이상의 경우, Coding scheme 없음)
- TxAA: Closed Loop
  - 장점: 성능향상  $\propto M$
  - 단점: Feedback Data량  $\propto M$ , Channel Tracking



### Basis Selection

\* 서울대 이동통신연구실, 삼성

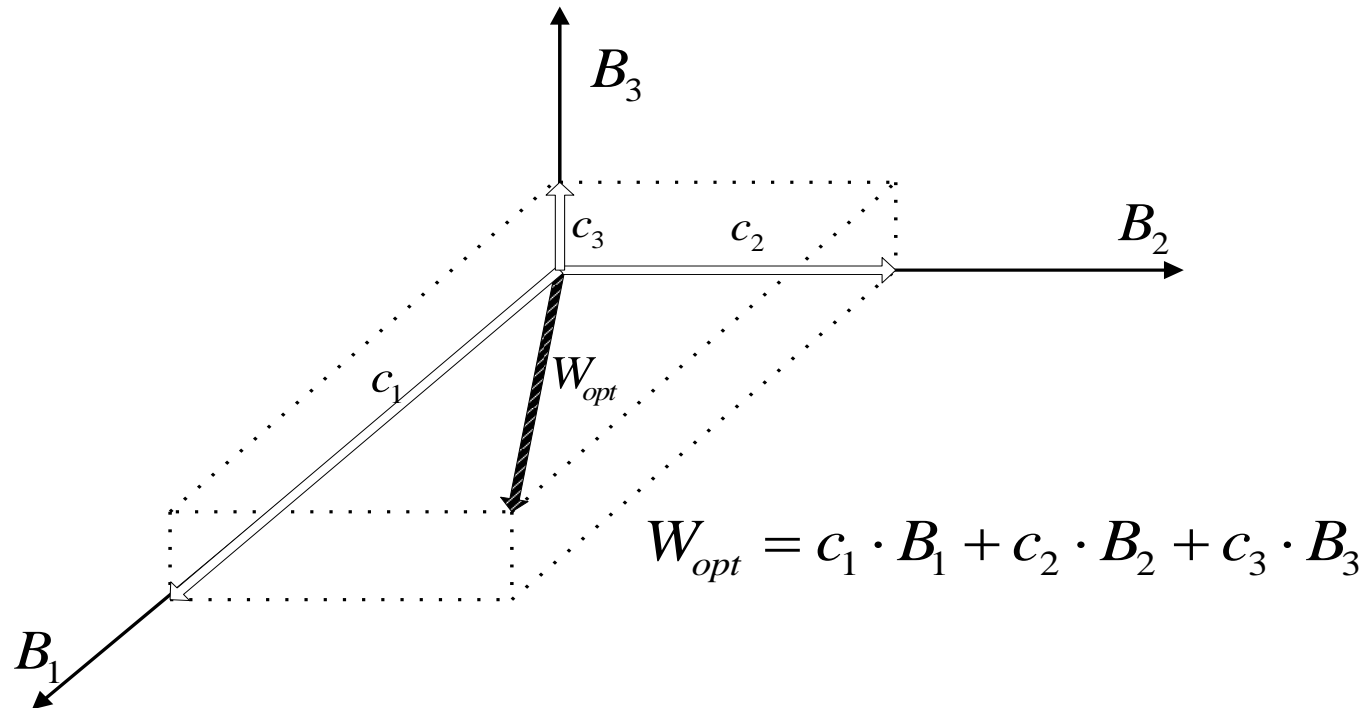
# Performace of Tx Diversity



- 4 tx antennas: 5.2dB gain at  $10^{-2}$  BER w.r.t. 2 antennas
- 8 tx antennas: 8.8dB gain at  $10^{-2}$  BER w.r.t. 2 antennas

# Basis Selection

- Basis Selection: Noble Approximation Technique



- $W_{opt} \cong \sum_{i=1}^S c_i \cdot B_i$  ,  $S$ : Selection Order



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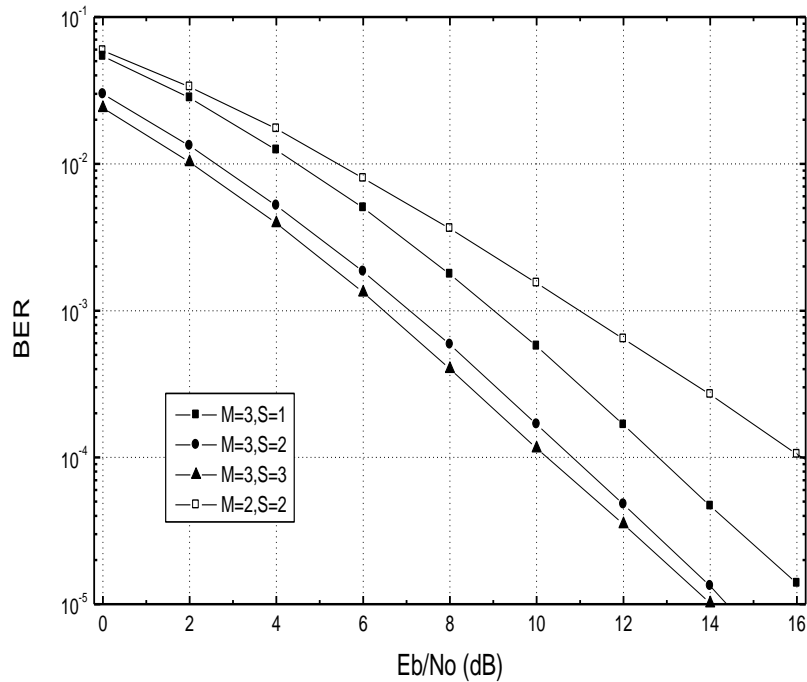
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## Basis Selection(cont'd)

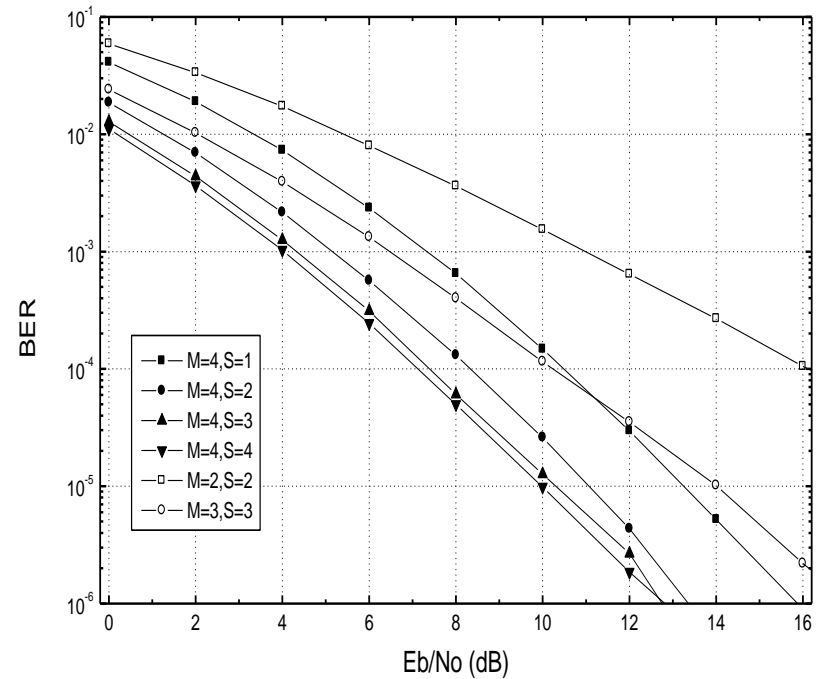
- Algorithm
  - ★ Calculate  $W_{opt}$
  - ★ Project  $W_{opt}$  to  $M$  bases, and Calculate  $c_i$
  - ★ Select the bases with the  $S$  largest coefficients
  - ★ Feedback the basis indices and the coefficients
- Feedback Data량: 감소
- 성능

# Performance (No. of paths=1)

$\langle M=3 \rangle$



$\langle M=4 \rangle$

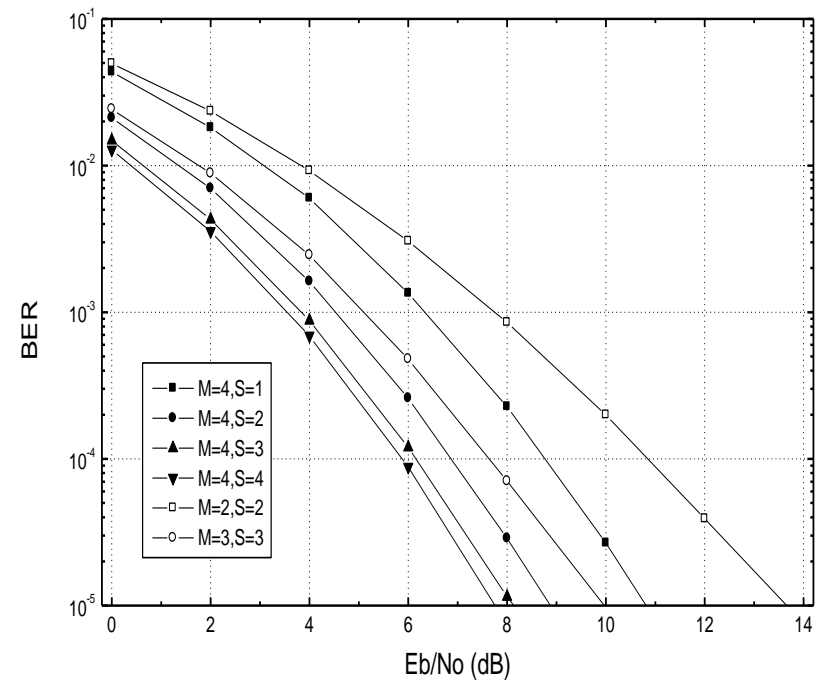
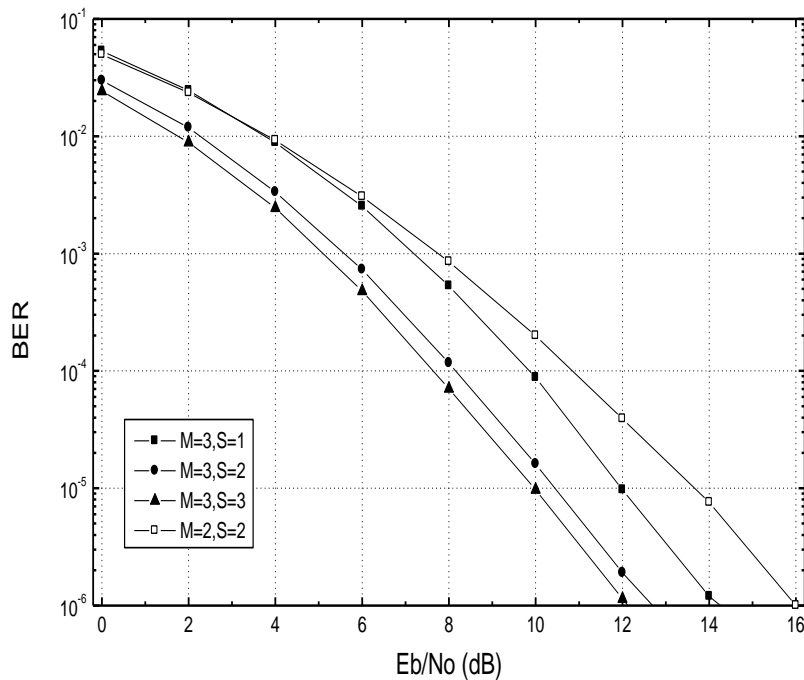


- Diversity order: slope

# Performance (No. of paths=2)

$\langle M=3 \rangle$

$\langle M=4 \rangle$



# Feedback Data량

- Direct Extension of 2 Antennas TxAA

$$N_D = (M - 1) \cdot N_2 \quad \text{where } M: \text{ No of Antennas}$$

$$N_2 : \text{ Required Bits for each antenna weight}$$

- Basis Selection

$$N_S = \left\lceil \log_2 \binom{M}{S} \right\rceil + (S - 1) \cdot N_2$$

- Examples ( $N_2=4$  bits)

<No. of Antennas=4>

S \	Direct Ext.	Basis Sel.
1	12 bits	2 bits
2		7 bits
3		10 bits
4		12 bits

<No. of Antennas=8>

S \	Direct Ext.	Basis Sel.
1	28 bits	3 bits
2		9 bits
3		14 bits
4		19 bits

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# Multiple Tx and Multiple Rx