

# CHAPTER 3

## ORBITALS AND BONDING

### Contents

**Atomic and Molecular Orbital**

**Hybridization**

**Resonance**

## 3.1 Atomic orbitals (AO)

- ⇒ Describes the location of e<sup>-</sup> density in atom
- ⇒ Given by quantum mechanical wave function

### Shape of Atomic Orbitals

Sign does not related to charge;  
mathematical value of the wave  
function, e<sup>-</sup> density  $\propto$  (wave ftn)<sup>2</sup>

The more nodes, the higher energy;  
node is where wave ftn is zero; no  
e<sup>-</sup> density

Any other s and p (3s, 4p, 3p, 4p...  
orbitals can be treated similar to  
2s and 2p.

## quantum numbers

$n$  (principle quantum #) = 1, 2, 3, ... -- shell; 2

$l$  (azimuthal quantum #) = 0, 1, 2, to  $n-1$  -- sub-shell, shape;  $2p$

$m_l$  (magnetic quantum #) =  $-l$  to  $l$  -- orientation;  $2p_z$

*If  $l=1$  then  $-1, 0, +1$*

$m_s$  (spin quantum #) =  $+1/2$  or  $-1/2$  -- spin of  $e^-$ ;  $\uparrow\downarrow$

# Electron configuration in AO

⇒ **Distribution of electrons among orbitals**

1. **Each e<sup>-</sup> is placed in the lowest E orbital available**
2. **Pauli exclusion principle: a maximum of two e<sup>-</sup>s in each orbital**
3. **Hund's rule: when degenerated orbitals are available(2p), e<sup>-</sup>s first occupy them singly with the same signs.**

## 3.2 Molecular orbitals (MO)

⇒ Describes the location of  $e^-$  density in molecule

Ex)  $H_2$ ,

a.  $1s_a - 1s_b$  combination

Node between the two nuclei.

⇒ antibonding MO: higher the in E than the AO's (less stable by  $2\Delta E$ )

b.  $1s_a + 1s_b$  combination

in the overlap region, the e-density increases.

⇒ bonding MO: lower the in E than the AO's

# Energy level diagram

**H<sub>2</sub> is more stable than two atoms by 2  $\Delta E$ : need 2  $\Delta E$  to break H<sub>2</sub> into two atoms**

# The shape of a sigma bond

# Is He<sub>2</sub> possible ?

He<sub>2</sub>

There is no gain by making He<sub>2</sub>.

More complicated molecules; e<sup>-</sup>'s loacted over all atome

⇒ Delocalized MO should be used!

Still localized MOs is applied to the complicated molecules because it is much easier to understand!



**Assuming the all the molecules have localized MOs, following generalization was made.**

- 1. The # of MO = the # of AO**
- 2. Two AOs  $\rightarrow$  1 bonding MO + 1 antibonding MO**
- 3. Usually there are enough e<sup>-</sup>'s to fill the bonding MOs and anti bonding MOs are empty, although not always true.**
- 4. If 3 is true then, bonding  $E = \# \text{ of e}^- \times \Delta E$**
- 5. The magnitude of  $\Delta E$  increases with increasing overlap of the AOs. If the atoms are too close, then repulsion decrease the E.**

## 3.3 Sigma Bonds and $sp^3$ Hybridization

Four bonds are found to be identical from experiments.

How?

Carbon, C, has one 2s and three 2p AOs in the valence shell

↓ Hybridization

Four  $sp^3$  hybrid AOs

**Therefore the formation of CH<sub>4</sub> is**

**⇒ 2s e<sup>-</sup> + 2 2p e<sup>-</sup> of Carbon →  
excited to 1 2s e<sup>-</sup> + 3 2p e<sup>-</sup>**

**⇒ 1 2s AO + 3 2p AOs →  
4 sp<sup>3</sup> hybridized AO**

**⇒ sp<sup>3</sup> AO of C + 1s AO of H →  
σ bonding MO + σ\* antibonding MO with 2 e<sup>-</sup>**

**⇒ 4 σ MOs -- 4 equivalent σ<sub>sp<sup>3</sup> - 1s</sub> bonds**

**Orbital  
pictures for  
other  
molecules**

**How the pi ( $\pi$ )  
bonds and  
antibonds are  
formed.**

# Formation of pi and sigma bonds

# Formation of pi and sigma bonds from $2p$ AOs

## 3.4 Double Bonds and $sp^2$ Hybridization

Experimental data for  $\text{CH}_2=\text{CH}_2$  shows planar arrangement. How?

Three  $sp^2$  AOs from  $2s$ ,  $2p_x$  and  $2p_y$

Then  $\text{CH}_2\text{CH}_2$  is



## Therefore the formation of $\text{CH}_2=\text{CH}_2$ is

- 2  $2s$   $e^-$  + 2  $2p$   $e^-$  of Carbon  $\rightarrow$  excited to 1  $2s$   $e^-$  + 3  $2p$   $e^-$
- 1  $2s$  AO + 3  $2p$  AOs  $\rightarrow$  3  $sp^2$  hybridized AO + 1  $2p$  AO
- $sp^2$  AO of C +  $1s$  AO of H  $\rightarrow$   $\sigma_{sp^2 - 1s}$  bond
- $sp^2$  AO of C +  $sp^2$  AO of C  $\rightarrow$   $\sigma_{sp^2 - sp^2}$  bond
- $2p$  AO of C +  $2p$  AO of C  $\rightarrow$   $\pi_{2p - 2p}$  bond

## **$\Delta E$ of pi bonding**

**total double bond (C=C) = 145 kcal/mol**

**sigma bond (C-C) = 81 kcal/mol**

**The difference, 64 kcal/mol  $\Delta E$  of pi bonding, which is smaller than that of the sigma bond.**

**Therefore pi bond is more reactive than the sigma bond.**

**Is rotation of double bond possible ?**

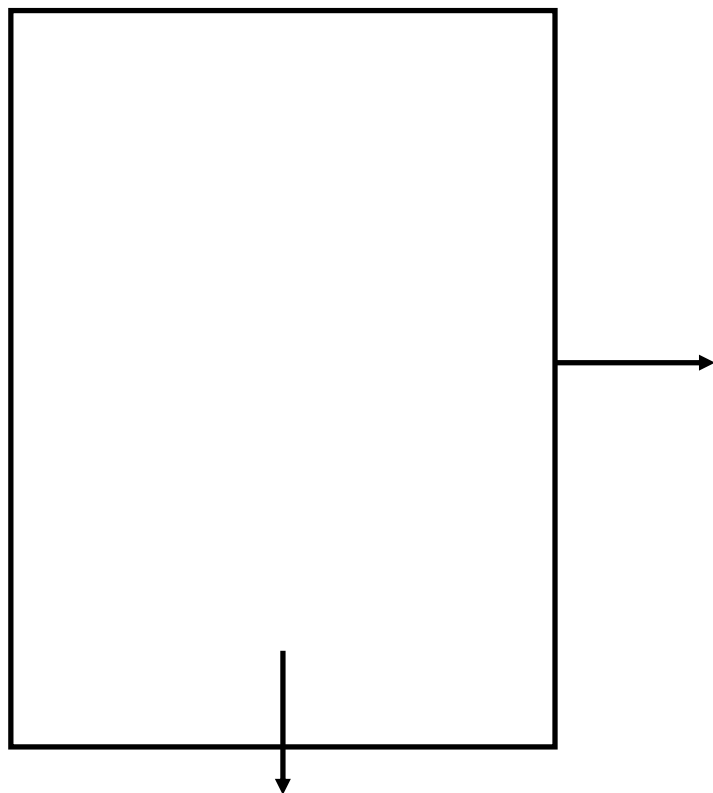
**Impossible!**

**$\pi$  bonding = 64 kcal/mol**

**thermal E at room temperature = 20 kcal/mol**

## 3.5 Triple bonds & *sp* hybridization

Experimental data for  $\text{HC} \equiv \text{CH}$  shows linear arrangement.



One 2s AO + one 2p AO = two *sp* AOs

## Therefore the formation of $\text{CH}\equiv\text{CH}$ is

- $2\ 2s\ e^- + 2\ 2p\ e^-$  of Carbon  $\rightarrow$  excited to  $1\ 2s\ e^- + 3\ 2p\ e^-$
- $1\ 2s\ \text{AO} + 3\ 2p\ \text{AOs} \rightarrow 2\ sp\ \text{hybridized AO} + 2\ 2p\ \text{AO}$
- $sp\ \text{AO of C} + 1s\ \text{AO of H} \rightarrow \sigma_{sp-1s}\ \text{bond}$
- $sp\ \text{AO of C} + sp\ \text{AO of C} \rightarrow \sigma_{sp-sp}\ \text{bond}$
- $2p\ \text{AO of C} + 2p\ \text{AO of C} \rightarrow \pi_{2p-2p}\ \text{bond}$ 
  - triple bond =  $1\ \sigma + 2\ \text{perpendicular}\ \pi$

## □ Why hybridize?

- to bond well

## □ Energy?

- Energy required for excitation
- Energy released by bonding
- Energy released > Energy required

## 3.6 Resonance and MO theory

In localized MO theory, each MO is located on only two atoms; not really true.

$\text{CH}_3\text{CO}_2^-$  shows;

1. *more than one Lewis structure*
2. *Any Lewis structure cannot represent the real molecule*  
*⇒ from experiment*
3. *The actual structure is a **resonance hybrid***

The real structure

three AOs overlap to form three MOs.

Four electrons are in these three AOs.

This delocalized MOs are more stable than the hypothetical delocalized MOs above.

**Example of conjugation; 3 or more parallel  $p$  orbitals**



## **3.7** Rules for resonance structures

## 3.8 Types of resonance interactions

1. unshared **(two) electrons** next to a pi bond

## 2. **one electron** next to a pi bond

**Equally** important →  
**large** resonance-stabilization →  
**less** reactive radical (than localized)

## 3. **empty p** orbitals (no electron) next to a pi bond **allyl cation**

**Equally** important → **large** resonance-stabilization → **less** reactive cation  
(than localized)

## 4. Pi bonds between atoms of different electronegativities

acetaldehyde

**Most stable**

**Less stable**

**impossible**

**OK**

**impossible**

## **5. Cycle of double bonds**

**Actual  
structure**

**Equivalent resonance; six bonds are identical from  
experimental results**

**Very large resonance energy**

**more important – major contributor**

**less important – minor contributor**

**Because of the two important resonance structures, this has large resonance energy. It is why phenol is more acidic than aliphatic alcohols**

# Resonance and property

## □ Bond length

□ C-C: 1.54 Å, C=C: 1.34 Å

□ in benzene, 1.40 Å

□ in naphthalene, 1.42 and 1.36 Å  92-93, Elaboration

## □ Stability and reactivity

## 3.9 Molecular Orbital Energies

### □ MO energies



□ **ethane**: only  $\sigma$  MOs

□ **ethylene**:  $\sigma$  &  $\pi$  MOs

□ **formaldehyde**:  $\sigma$  &  $\pi$  MOs and n AOs

See Fig 3.23-3.25