

Note 4

# Variables

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# Topics

- Name
- Assignment
- l-value and r-value
- Scope
- Binding

# Variables and assignments

- Components of a variable
  1. name : identifier composed of letters
  2. memory location : bound to the variable
  3. current value : stored in the location
  4. data type : static/dynamic binding
  5. scope : static/dynamic
  6. life time : interval during which a location is bound to the variable
- An assignment changes the contents of some components of a variable.

Scheme

```
> (set! x 10)
10 //the type is an integer of value 10
> (set! x 4.5)
4.5 //now, the type is a real number of value 4.5
```

# location (l-value) and value (r-value)

- The *location* of the variable is regarded as a kind of value owned by the variable.  
→ so, we call the location the l-value of the variable.

- To make a distinction, the *real value* of the variable is called the r-value.

**Ex:** `char z = 'o';` // the l-value of z is the address of z and the r-value is 'o'

- A rule of assignments:

*“The **l**-value of an assignment should have the **l**-value, and its **r**-value should have the **r**-value.”*

C++

```
float x; // create real variable x with the l-value in which the r-value is undefined
float y = 4.1; // create real variable y with the r-value defined by storing 4.1 to the l-value of y
x = y; // store the r-value of y into the l-value of x
y = y * 3.0; // store the r-value of y times 3.0 into the l-value of y
```

- When different variables have the same l-value, it is called *aliasing*. → Ex:

```
char d;
char & c = d; // c and d share the same location
```

# Properties of l-values and r-values

- **referencing**: the operation of getting the l-value of a variable

EX: `char* p = &c;` → note the graphical interpretation!

- **dereferencing**: the operation of going from a reference to the r-value it refers

→ In C++, the right-hand side is always dereferenced once.

```
char c, d;  
char *p, **q, **r;  
c = d;  
q = r;  
d = p;  
p = c;  
r = c;
```

*// OK! dereferenced once*

*// OK! dereferenced once*

*// error! Should be dereferenced twice*

*// error! no dereferencing necessary*

*// error! no dereferencing sufficient*

# Properties of l-values and r-values

- Some expressions, such as *id*, *array reference* and *dereference*, have both l-values and r-values.
  - All other expressions have r-values only.
  - Thus, these other expressions can **NOT** appear on the left-hand side of assignments.

```
4.5 = 10.1;  
"jane" = y;  
y + 1 = a[i];  
x = 10.1;  
a[i] = y + 1  
employee.name = "jane"  
*p = foo(x,y)  
foo(x,y) = 1.1;
```

```
// illegal - integers have no l-values  
// illegal - strings have no l-values  
// illegal - arithmetic expressions have no l-values  
// legal - id expressions have l-values  
// legal - array references have l-values  
// legal  
// legal - dereference expressions have l-values  
// maybe legal, maybe illegal
```

gnu c++ says error: 'non-lvalue in assignment'

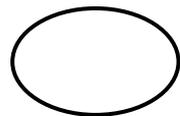
# Graphical notation for variables



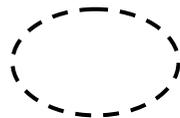
name



Location that can contain an ordinary data value



Location that can contain a reference (address) value



Location that can contain a reference-reference value

# Graphical notation for variables

```
char c = 'w';
```



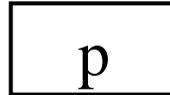
```
char d = c;
```



```
char& e = d;
```



```
char* p = &c;
```



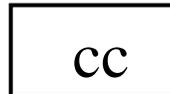
```
char** q = &p;
```



```
char** r = q;
```



```
const char cc = 'w';
```

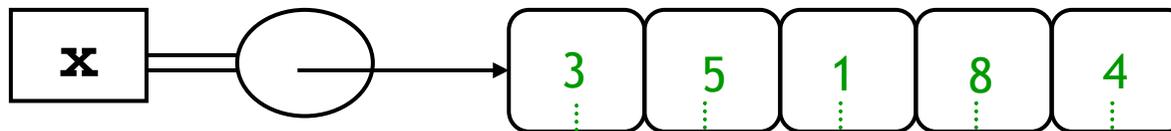


# Array variables

- In Pascal, when you declare

```
x, y : array [1..5] of integer;
```

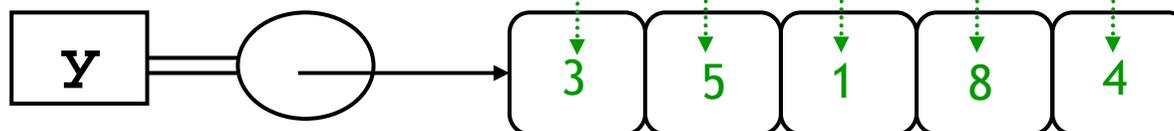
the compiler creates not only the storage for 5 integers, but also a pointer to its beginning address.



When we have an array assignment

```
y = x;
```

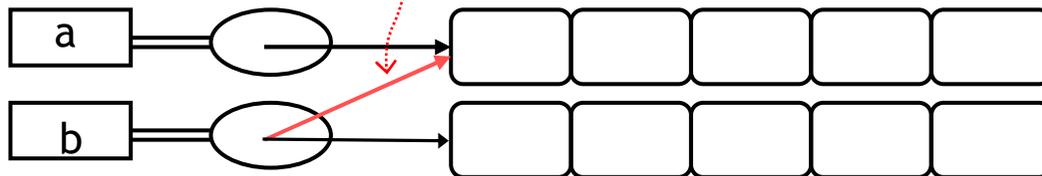
the whole contents of the array on right-hand side are copied to the location of the array on the left-hand side.



# Array variables

- In C++, an array is really a pointer. So, arrays and pointers can be mixed. Thus, after `b = a`, we should have ...

```
int a[5], b[5];
```

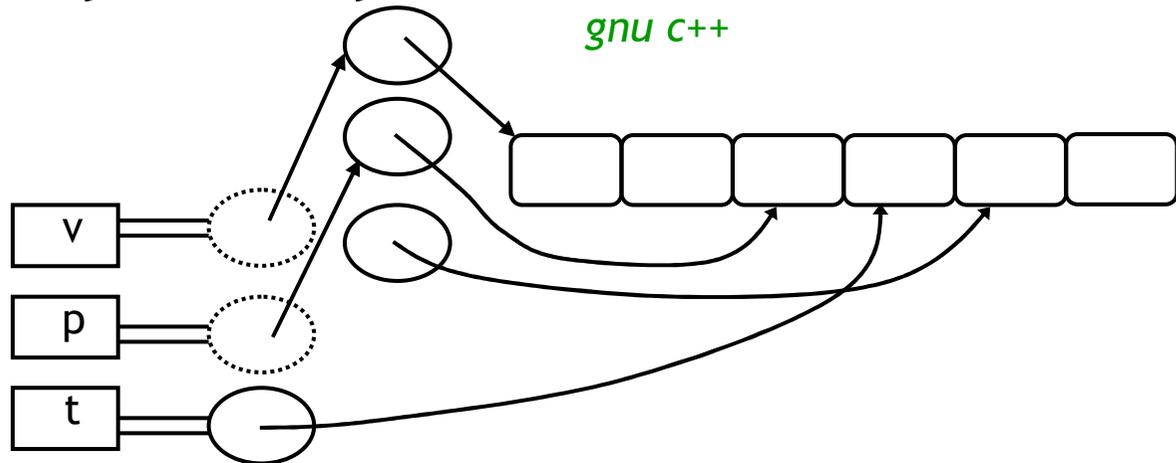


*But in practice, this is totally implementation dependent*  
*SUN C++: illegal*  
*GNU C++: copy*

*like Pascal*

- In C++, a multi-dimensional array is simulated with arrays of arrays.

```
int v[3][2];  
int **p = v + 1;  
int *t = *p + 1;
```



*Thus, given `int c[5], d[3];`  
`d = c` would be illegal with  
`gnu c++`*

# Name conflicts

- In languages, a name can be used to mean several different objects. → Ex) Ford: : a name of a man, a car, or a company ...
- Using the same name to represent different objects in different places causes a **name conflict** and potentially ambiguity of the language.
- But, name conflicts are often necessary to improve naturalness of a language and readability/writability.

Ford drives a car.

They work for the Ford.

She drives a Ford.

→ *How do we know which Ford means which in each sentence?*

Ford1 drives a car.

They work for the Ford2.

She drives a Ford3.

→ *OK. no more naming conflict! So, the meaning is clearer. But do you like it?*

# Scope

- Ambiguity due to naming conflicts can be resolved by associating names with the **environments** where each name is defined.
  - Jane in Ohio, Jane in Maine, Jane in Virginia
- In a programming language, a **scope** is a program environment in which names are defined or declared.
  - procedures and blocks (Pascal, C), lambda expressions (Scheme)
- Through a declaration within some scope, a name is bound to a variable with certain attributes, and the variable is called a **bound variable**.
- A variable which is not bound in the scope is called a **free variable**.

# Scope

```
{ // beginning of a new environment/scope
  int a[10]; int i; char c; // declarations of three names
  c ... // a reference to 'c': bound to a character variable
  ... a[i] // references to 'a' and 'i': bound to integer variables
  x ... // a reference to the free variable 'x' within this scope
} // end of a scope
... c ... // The name no longer represents a character variable.
// Then, what is it now?
```

→ A binding of a name is visible and effective inside the scope where the name is declared.

- The idea of a scope is to limit the boundary of a declaration of a name.
- Outside the boundary of a declaration, that declaration and binding should not be visible.

# Example: scopes in mathematics

- The notion of a scope also appears in mathematics.

scope 1

*Let  $x$  be the amount of salary that Susan receives every month, and  $y$  be the price of the new car she wants to have.*

*Then, the time that it takes for her to buy the car is  $y/x$  months.*

---

*Now, let  $x$  be the amount of money that John wastes every day, and  $y$  be the total amount of money he currently has.*

*Then, the time that it takes before he goes bankrupt is  $y/x$  days.*

scope 2

declarations

references

- Existential,  $\exists$ , and universal,  $\forall$ , quantifiers provide a formal notion of scope.

declarations

→  $(\forall x (\exists y f(x,y))) \vee (\forall z g(x,y,z))$

$\forall x$   
scope of  $x$

$\exists y$   
scope of  $y$

$\forall z$   
scope of  $z$

free variable

→ A declaration of  $x$  makes  $x$  a bound variable.