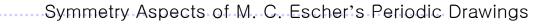




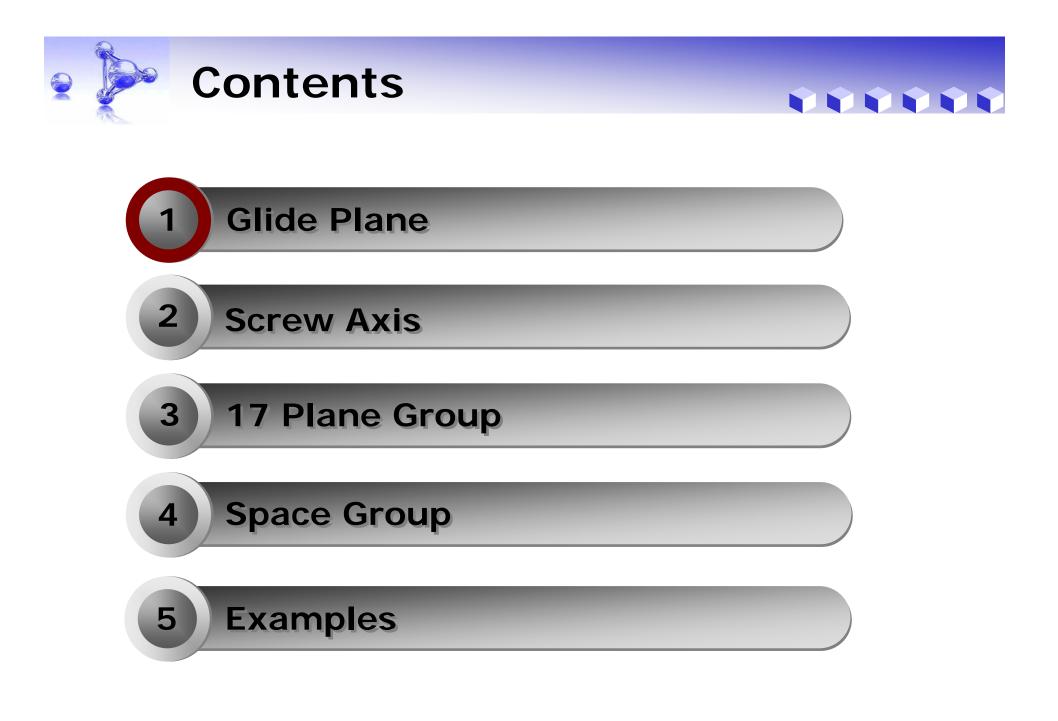
Chapter 7 Space Group



Reading Assignment: 1. W. B-Ott, Crystallography-chapter 9















- 32 point groups- symmetry groups of many molecules and of all crystals so long as morphology is considered
- space group- symmetry of crystal lattices and
 - crystal structures
 - 14 Bravais lattice
 - centered lattices- new symmetry operations
 - reflection + translation
 - rotation + translation





Space Lattice

- 14 Bravais lattice

, <u>, , , , , , , , , , , , , , , , , , </u>	Р	С	I	F		
Triclinic	PĪ					
Monoclinic	P 2/m	C 2/m				
Orthorhombic	P 2/m 2/m 2/m	C 2/m 2/m 2/m	I 2/m 2/m 2/m	F 2/m 2/m 2/m		
Tetragonal	P 4/m 2/m 2/m		I 4/m 2/m 2/m			
Trigonal		R 3 2/m				
Hexagonal	P 6/m 2/m 2/m					
Cubic	P4/m 32/m	· · · · · · · · · · · · · · · · · · ·	I 4/m 3̄ 2/m	F 4/m 3̄ 2/m		

The 14 Bravais lattice represent the 14 and only way in which it is possible to fill space by a three-dimensional periodic array of points.



W. B-Ott, Crystallography



표 1.1 결정계, 결정축계, Bravais 격자

결정 패밀리	결정계	결정축계	격자 상수	Bravais 격자
입 방 (cubic)	입 방	입 방	$a = b = c$ $\alpha = \beta = \gamma = 90^{\circ}$	P, I, F
육 방	육 방	육 방	$a = b \neq c$ $\alpha = \beta = 90^{\circ}, \ \gamma = 120^{\circ}$	Р
(hexagonal)	삼 방 (trigonal)	능 면 (rhombohedral)	a = b = c $\alpha = \beta = \gamma \neq 90^{\circ}$	R
정 방 (tetragonal)	정 방	정 방	$a = b \neq c$ $\alpha = \beta = \gamma = 90^{\circ}$	P, I
사 방 (orthorhombic)	사 방	사 방	$a \neq b \neq c$ $\alpha = \beta = \gamma = 90^{\circ}$	P, C(A, B), I, F
단 사	다시	rl al	1. c-unique $a \neq b \neq c$ $\alpha = \beta = 90^{\circ} \neq \gamma$	(P), (A)
(monoclinic)	단 사	단 사	2. b-unique $a \neq b \neq c$ $\alpha = \gamma = 90^{\circ} \neq \beta$	P, C
삼 사 (triclinic)	삼 사	삼 사	$a \neq b \neq c$ $\alpha \neq \beta \neq \gamma \neq 90^{\circ}$	Р

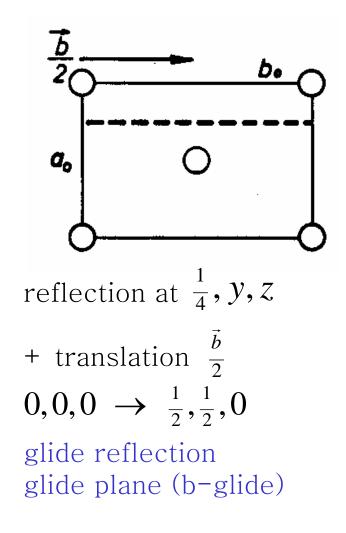


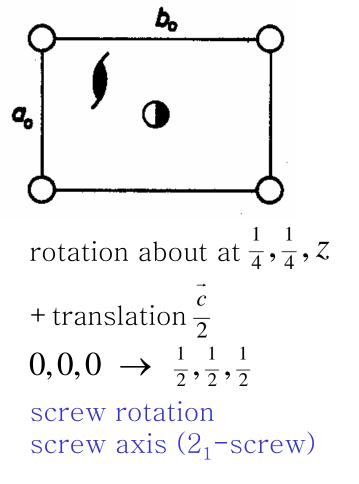
정수진, 결정학개론



i) orthorhombic C-lattice

ii) orthorhombic I-lattice







W. B-Ott, Crystallography



Table 5.1. Compound symmetry operations of simple operations. The corresponding symmetry elements are given in round brackets

	Rotation	Reflection	Inversion	Translation
Rotation	×	Roto- reflection	Roto- inversion	Screw rotation
Reflection	(Roto- reflection axis)	×	2-fold rotation	Glide reflection
Inversion	(Roto- inversion axis)	(2-fold rotation axis)	×	Inversion
Translation	(Screw axis)	(Glide plane)	(Inversion centre)	×



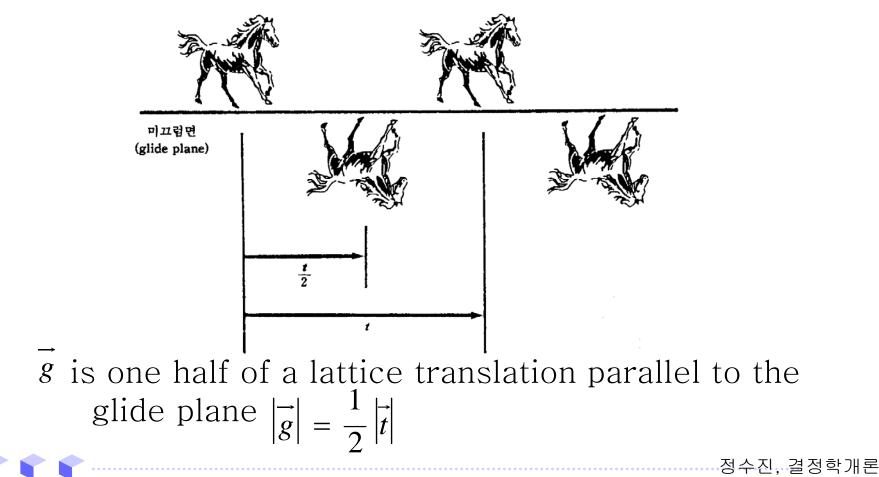
W. B-Ott, Crystallography



Glide Plane

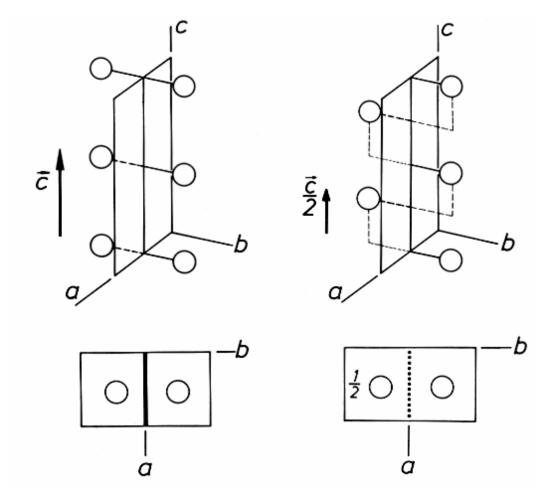


ii) translation by the vector \vec{g} parallel to the plane of glide reflection where $|\vec{g}|$ is called glide component





Mirror Plane vs. Glide Plane



 glide plane can occur in an orientation that is possible for a mirror plane



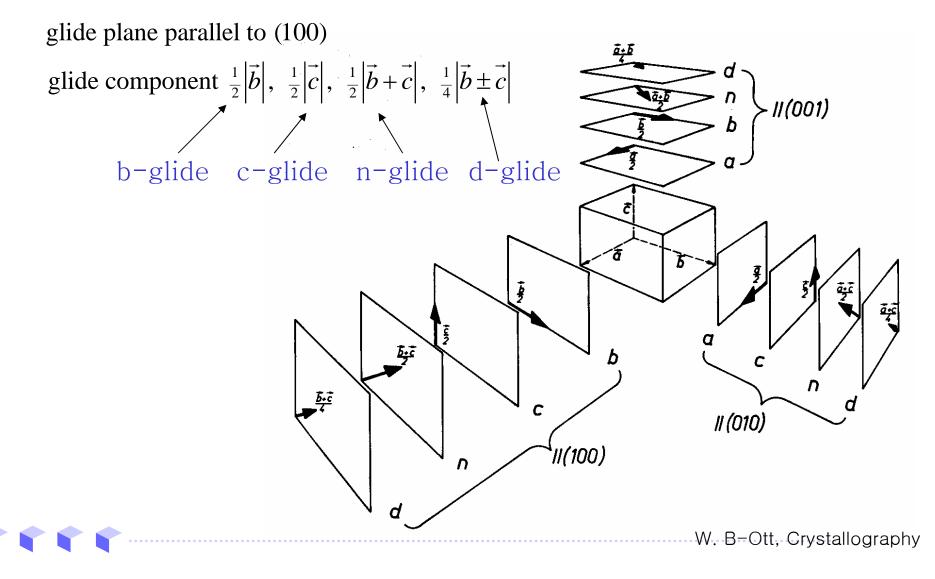
W. B-Ott, Crystallography

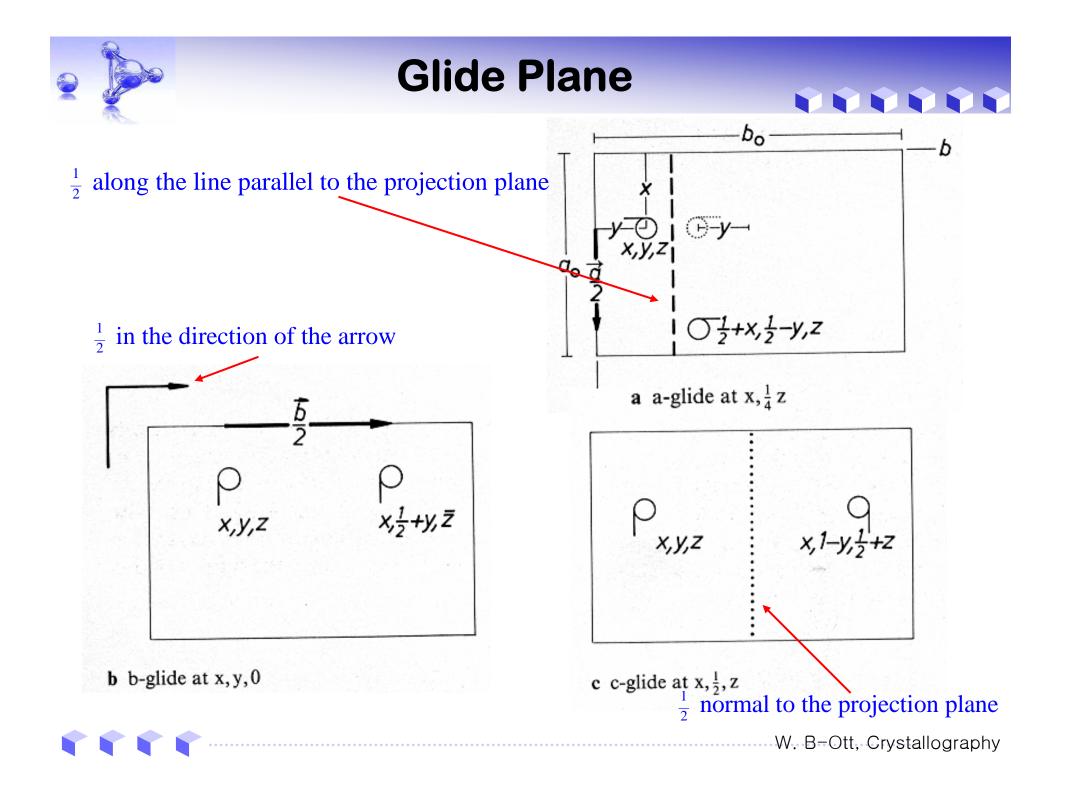


Glide Plane

- orthorhombic $P \frac{m}{2} \frac{m}{2} \frac{m}{2}$

(100), (010), (001) possible







Glide Plane



 $\frac{\frac{1}{2}}{4}$ in the direction of the arrow $\frac{\frac{1}{4}}{\frac{1}{2}}$

d n-glide at x, y, $\frac{1}{4}$ with glide component $\frac{1}{2}|\vec{a} + \vec{b}|$

 $\frac{1}{2}$ along the line parallel to the projection plane combined with $\frac{1}{2}$ normal to the projection plane

 $\bar{x}_{,\frac{1}{2}+y_{,\frac{1}{2}+z}$ x,y,z

e n-glide at 0, y, z with glide component $\frac{1}{2}|\vec{b} + \vec{c}|$

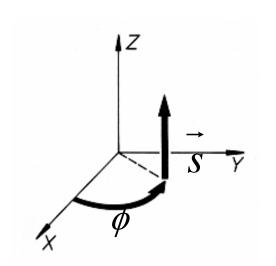


Screw Axis



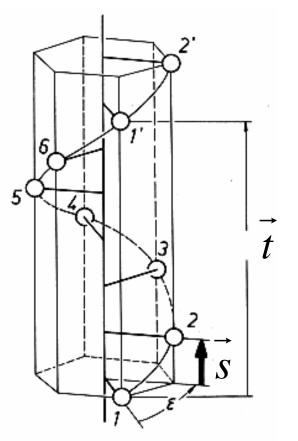
- rotation
$$\phi = \frac{2\pi}{X} (X=1,2,3,4,6)$$

- translation by a vector \vec{s} parallel to the axis where $|\vec{s}|$ is called the screw component



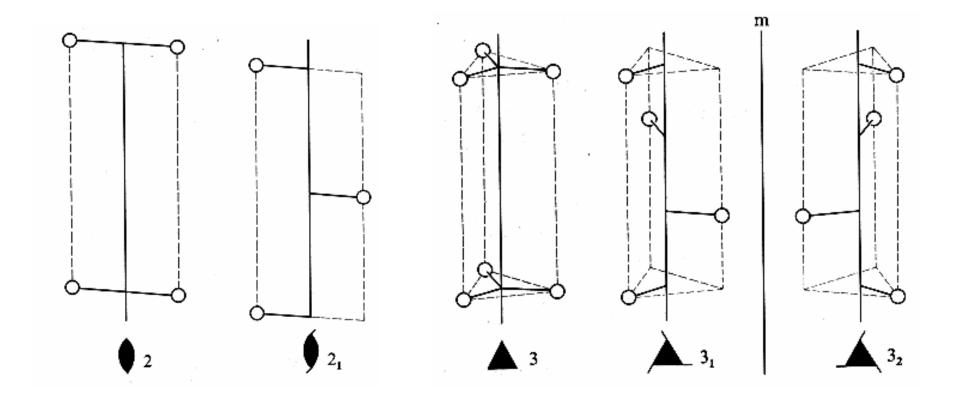
$$\left| \vec{s} \right| = \frac{p}{X} \left| \vec{t} \right|$$
 p=0,1,2...,X-1

$$X_{p} = X_{0}, X_{1}, \dots, X_{X-1}$$



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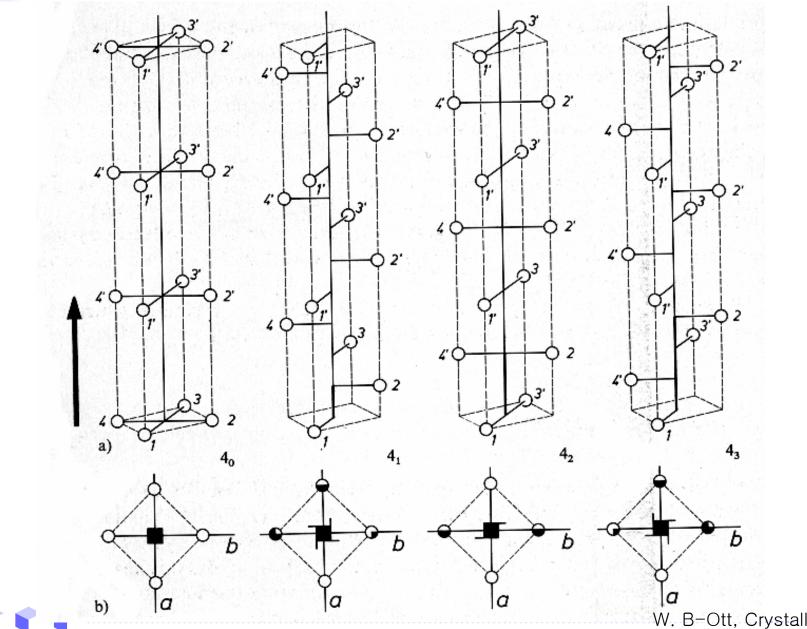










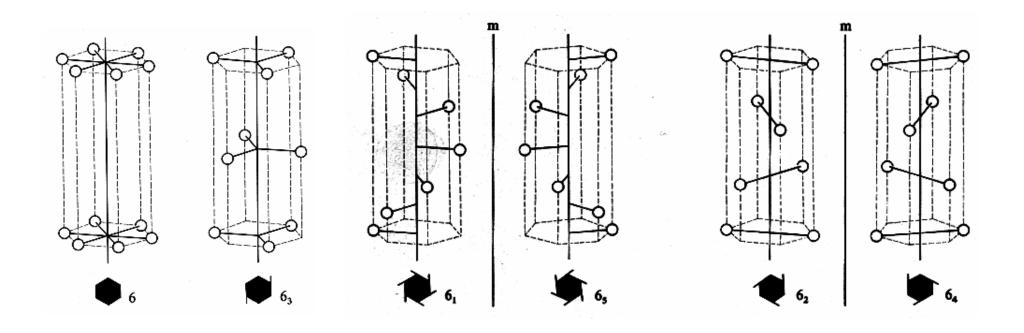


W. B-Ott, Crystallography

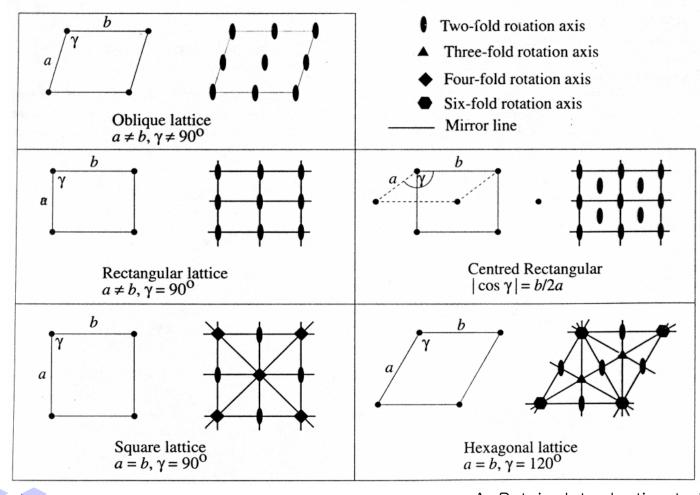








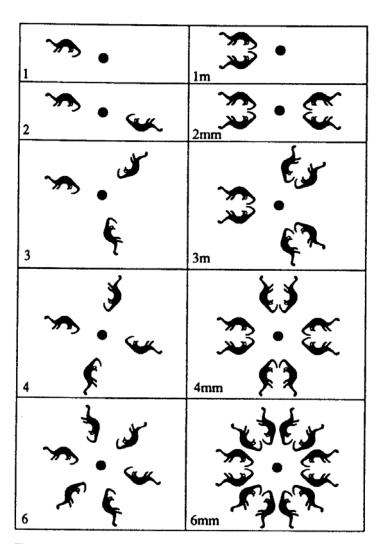
- 5 plane lattices + 10 plane point groups+ glide plane
- criterion: lattice itself must possess at least the symmetry of the motif





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Crystal system	Point groups compatible with crystal system	Lattices in system	Space groups compatible with lattice
Oblique $a \neq b, \gamma \neq 90^{\circ}$	1,2	p (primitive)	p1, p2
Rectangular $a \neq b, \gamma = 90^{\circ}$	1m, 2mm	p (primitive) c (centred)	pm, p2mm, pg, p2mg p2gg cm, c2mm
Square $a = b, \gamma = 90^{\circ}$	4, 4mm	p (primitive)	p4, p4mm, p4gm
Hexagonal $a = b, \gamma = 120^{\circ}$	3, 3m, 6, 6mm	p (primitive)	p3, p31m, p3m1 p6, p6mm

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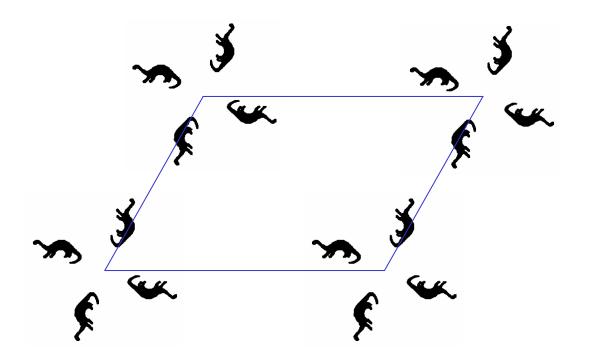


Lattice	Symmetry direction (position in Hermann–Mauguin symbol)				
Lattice	Primary	Secondary	Tertiary		
Two dimensions Oblique					
Rectangular	Rotation	[10]	[01]		
Square	point in plane	{[10] {[01]}	$ \left\{ \begin{bmatrix} 1 \overline{I} \\ 11 \end{bmatrix} \right\} $		
Hexagonal		{[10] [01] [[1]]	$ \begin{cases} [1\overline{1}] \\ [12] \\ [2\overline{1}] \end{cases} $		













17 Plane Groups

p1 p2	S S S S S
we we we we we	
~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~	
we we we we will	and and and and
~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~	
we we we we we	en an
	~~~ ~~ ~~ ~~ ~~ ~~ ~~ ~~ ~~ ~~ ~~ ~~ ~~

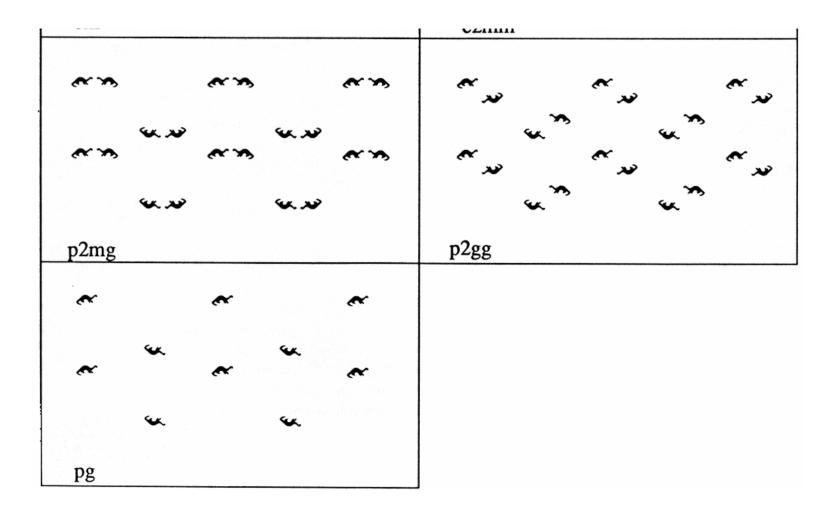


#### **17 Plane Groups**

		~ ~ ~	~ ~ ~				
p1	~ ~	~	* *	p2	s S	~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~	S S
~	~	×.	e s	~ ~	~ ~	~~~	~~~
S.	Sec.	귀엽 그는 것 집안 집안 같은 것		<b>EX 23</b>	~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~	<b>(K</b> , <b>X)</b>	w.w
5353	<u> </u>	Š	e s	~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~		~ m	~~
S.	sex.	٩.	<b>\$</b>	<b>K</b> XY	<b>Sec. 22</b>	<b>Ex. 22</b>	See 20
æ	~	č	×.	~~~	~ ~	~ m	~~
S.	Sec.	٩.	Sec.	80.20	84.20	Sec. 20	w.w
č.	æ	~	~	~~	~~~	~ >>	~ m
S.	×.	č.	č.	in sec. so	in si	in si	in si
pm				p2mm			

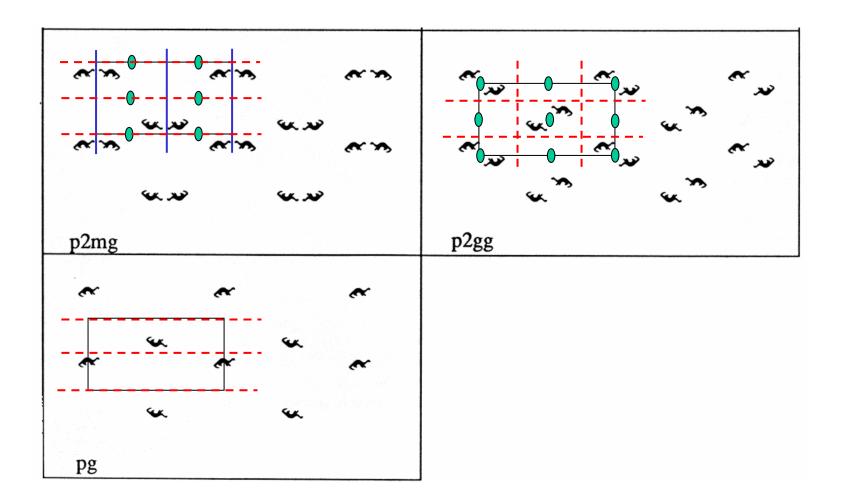






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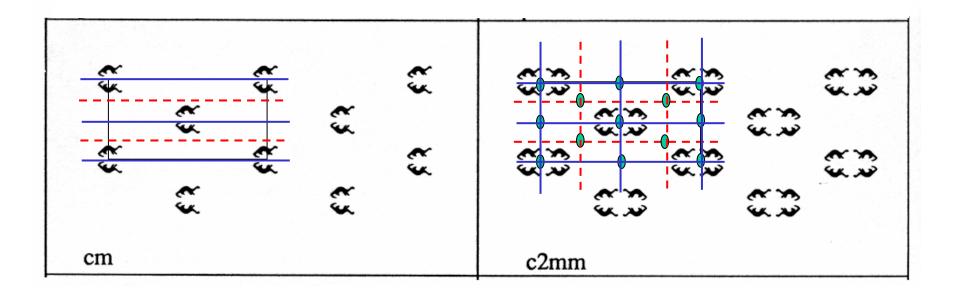


č.		~		~	a m		~~		an
s.		s.		×.			$\tilde{\mathbf{x}}$		~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~
	æ		~			~ ~		~~	
	Š		Š			~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~		~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~	
~		æ		~	~~~		~ ~		~~
S.		s.		×.			$\tilde{\mathbf{x}}$		~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~
	č.		~			~ ~		~ m	•
	S.		Sec.						



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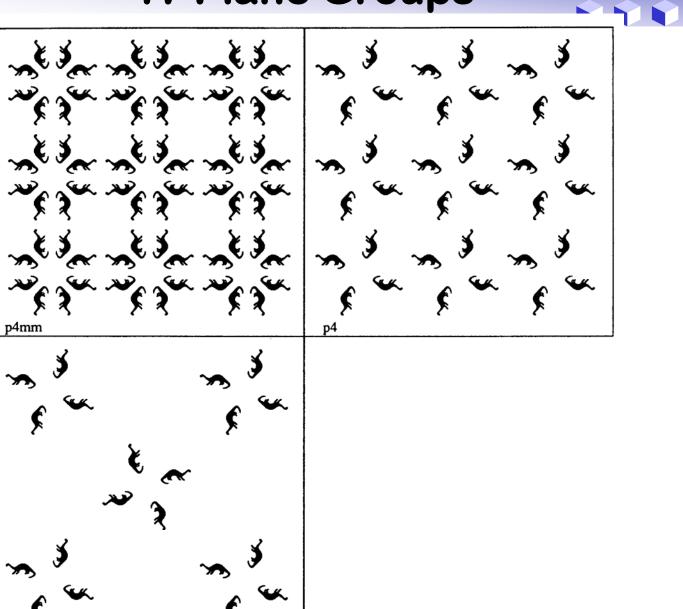






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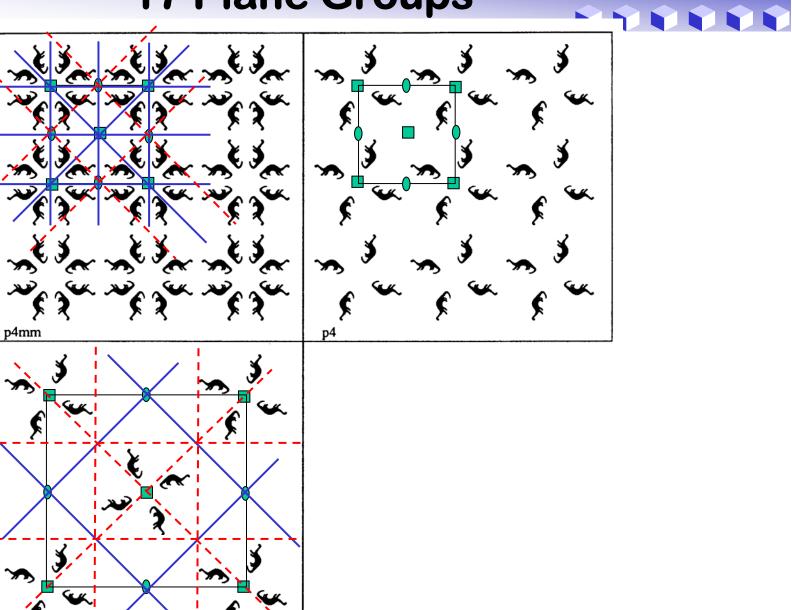


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p4gm

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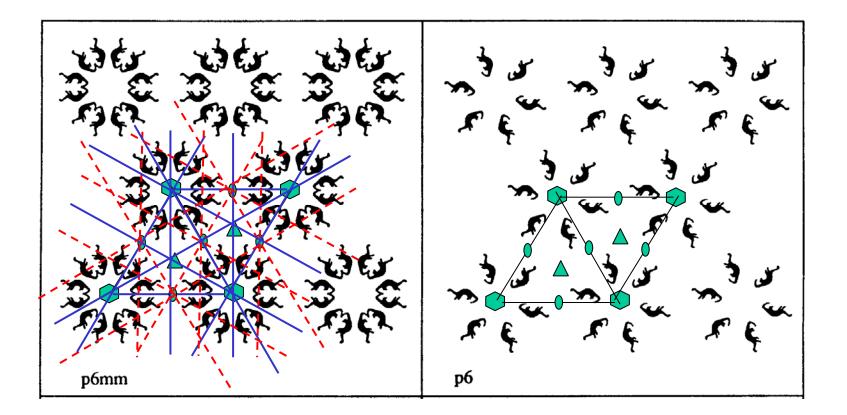




p4gm

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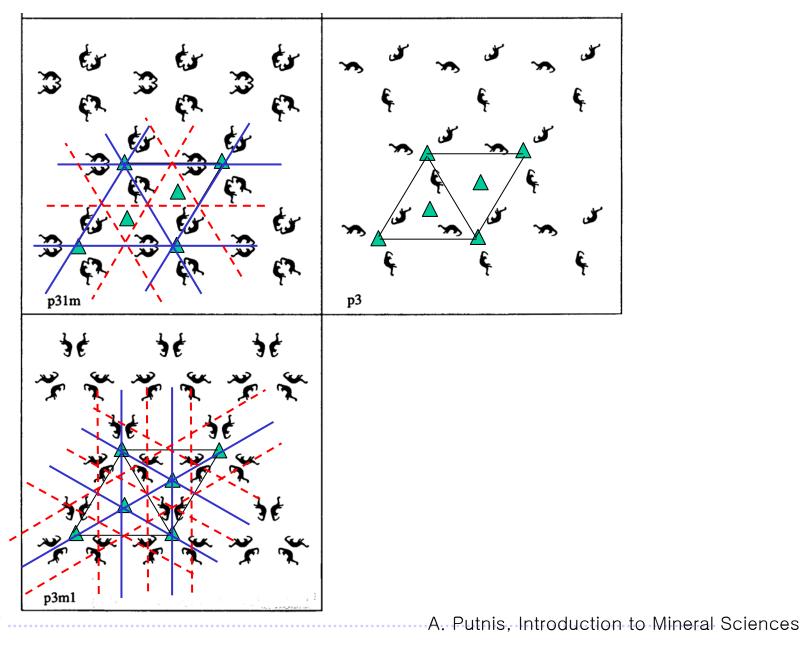




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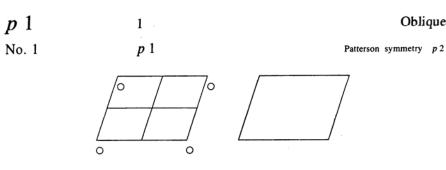


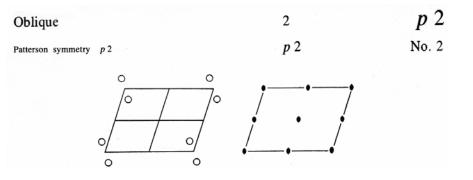




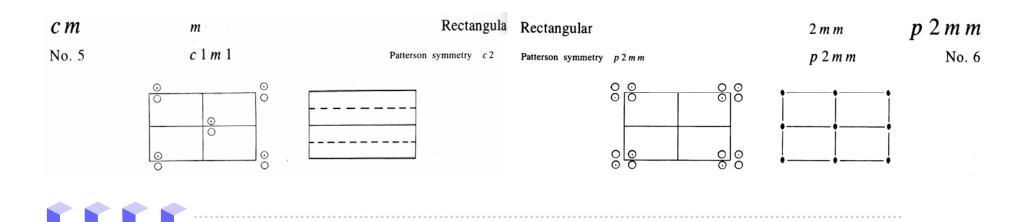
# International Tables for X-ray Crystallography

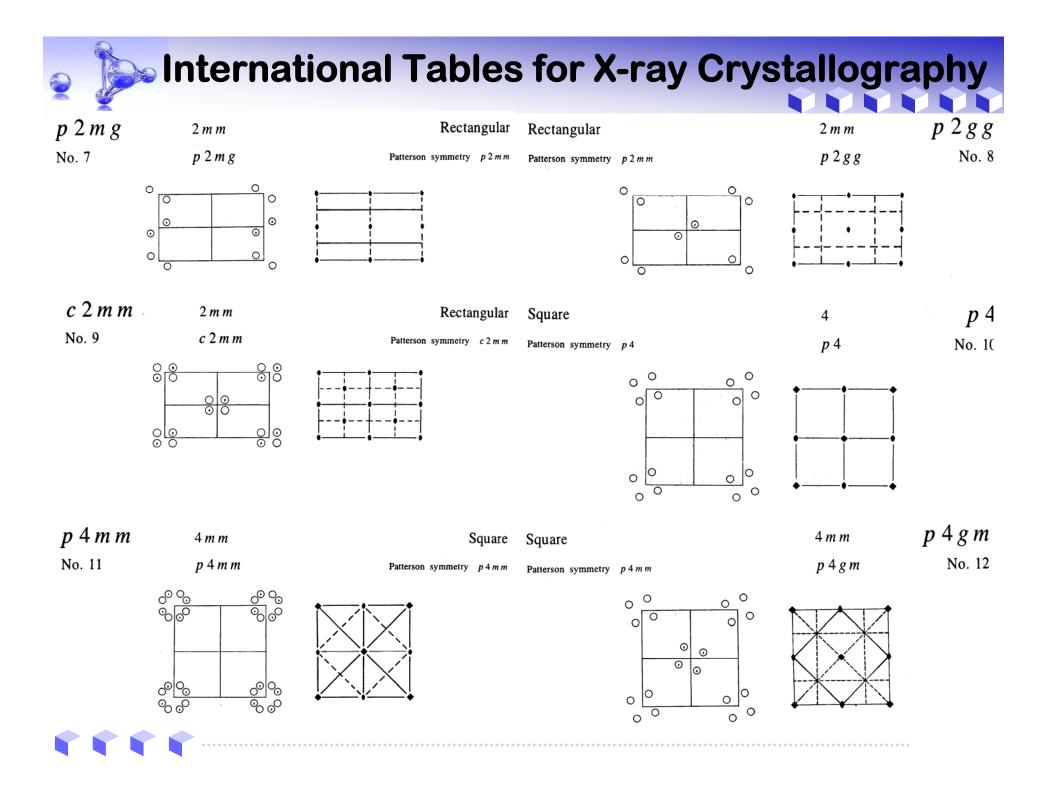
Oblique

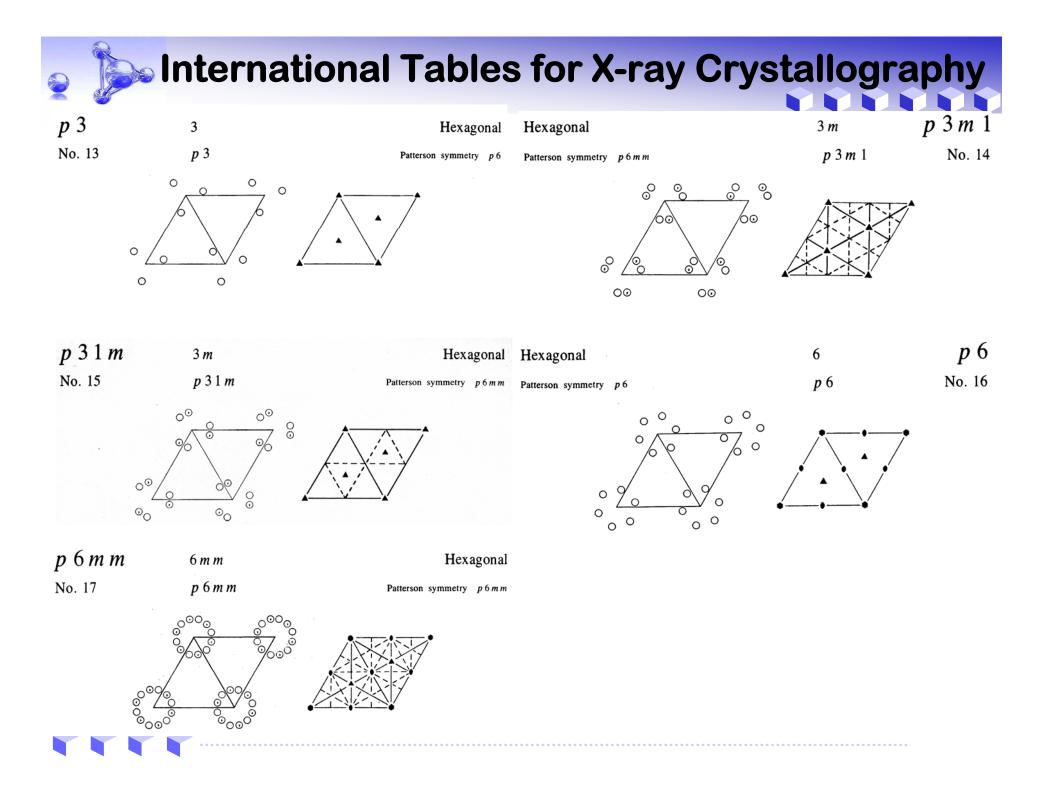


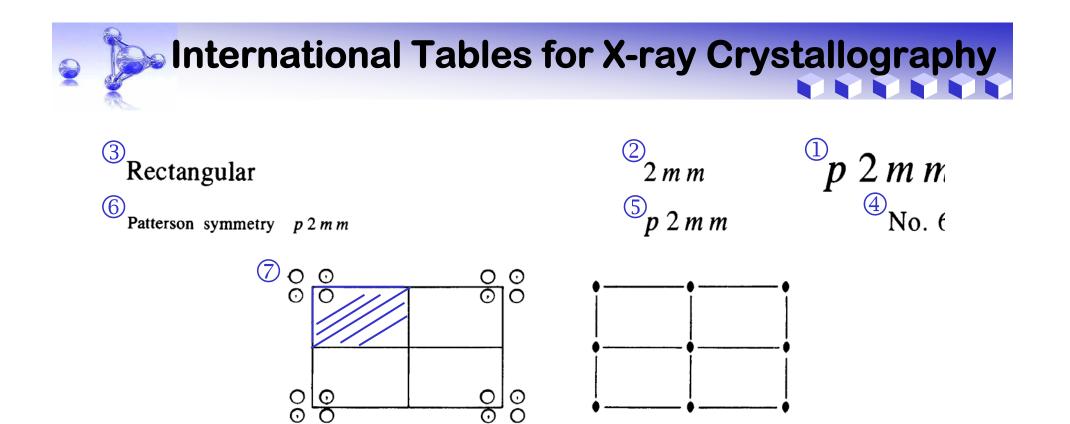


p m	m	Rectangular	Rectangular	m	pg
No. 3	p 1 m 1	Patterson symmetry p 2 m m	Patterson symmetry p 2 m m	<b>p</b> 1 g 1	No. 4









Origin at 2mm

Asymmetric unit  $0 \le x \le \frac{1}{2}; \quad 0 \le y \le \frac{1}{2}$ 

Symmetry operations

(1) 1 (2) 2 0,0 (3) m 0, y (4) m x,0

**Generators selected** (1); t(1,0); t(0,1); (2); (3)



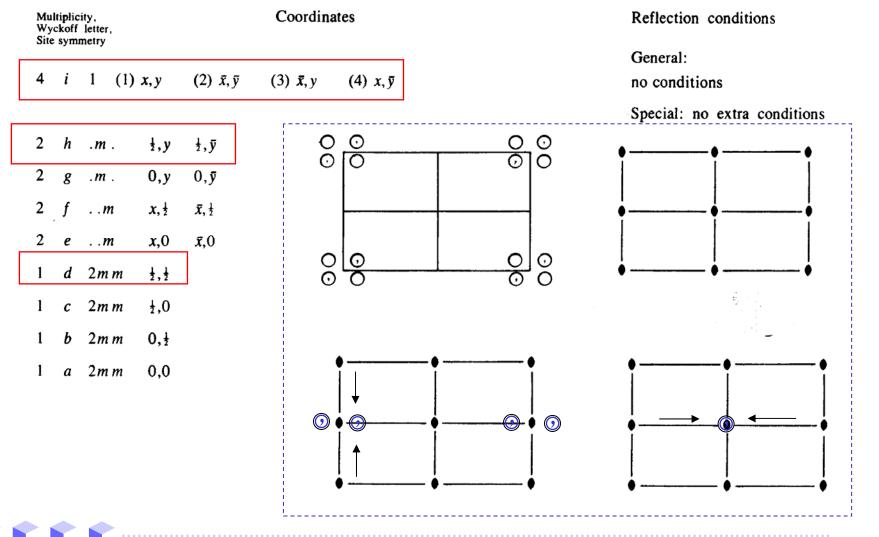
- short international (Hermann-Mauguin) symbol for the plane group
- ② short international (Hermann-Mauguin) symbol for the point group
- ③ crystal system
- ④ sequential number of plane group
- (5) full international (Hermann-Mauguin) symbol for the plane group
- 6 patterson symmetry
- diagram for the symmetry elements and the general position





#### **Generators selected** (1); t(1,0); t(0,1); (2); (3)

#### Positions





Maximal non-isomorphic subgroups

- I [2]p 211(p2) 1;2[2]p 1m1(pm) 1;3[2]p 11m(pm) 1;4
- IIa none

IIb [2] p 2m g(a'=2a); [2] p 2g m(b'=2b)(p2mg); [2] c 2m m (a'=2a,b'=2b)

Maximal isomorphic subgroups of lowest index

**IIc** [2]p 2mm(a'=2a or b'=2b)

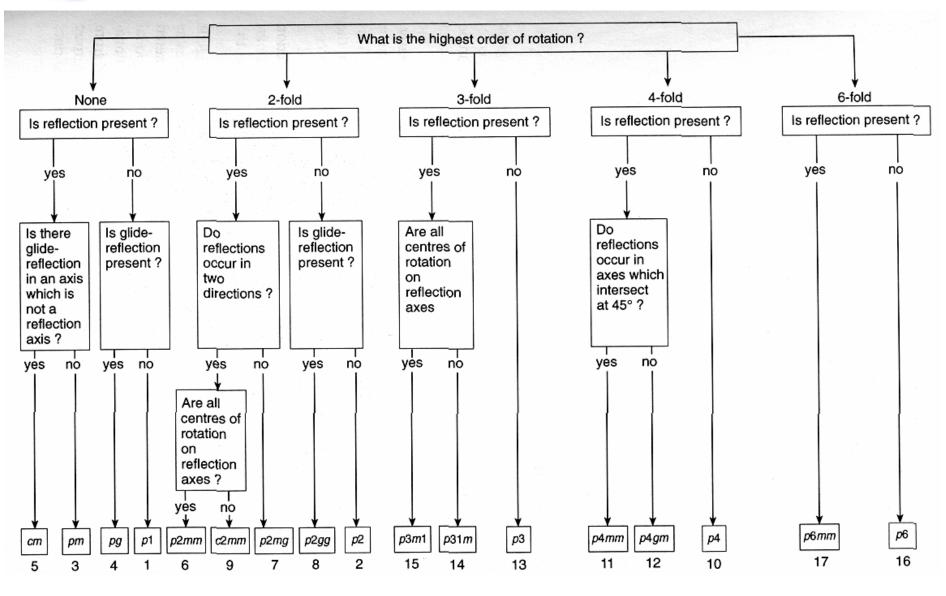
Minimal non-isomorphic supergroups

**II** [2] c 2m m





# Flow Diagram for Identifying Plane Groups

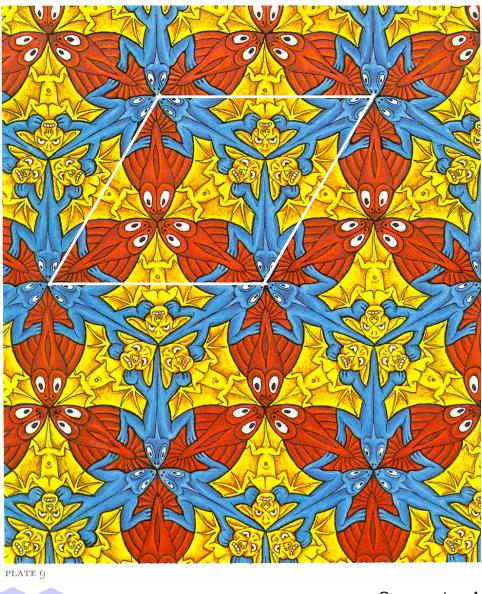


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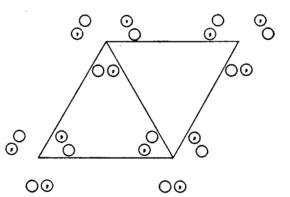


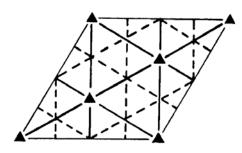
#### **Example I**











****

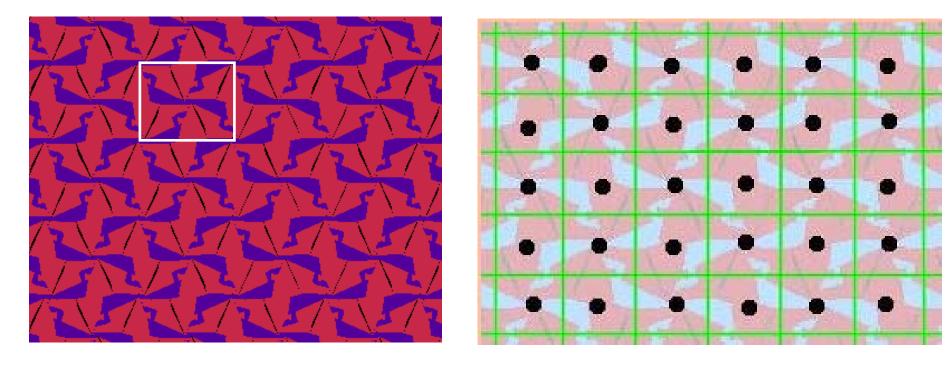
Symmetry Aspects of M. C. Escher's Periodic Drawings

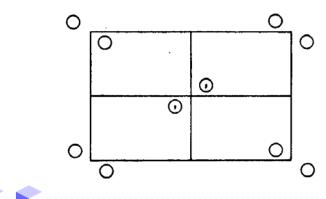


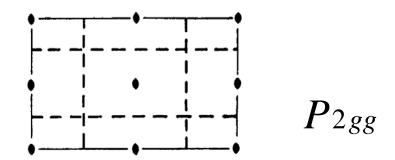
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### **Example II**





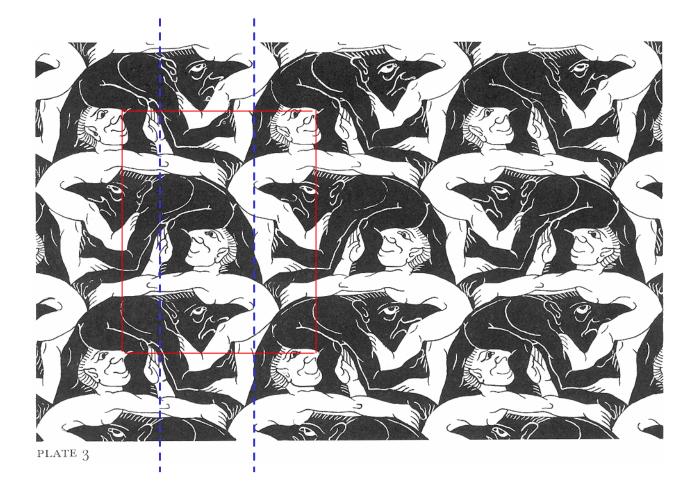




.....<u>http://www.clarku.edu/~djoyce/wallpaper/</u>







Pg



Symmetry Aspects of M. C. Escher's Periodic Drawings



### **Space Groups**



-Bravais lattice + point group → 230 space groups + screw axis + glide plane

- Bravais lattice + point group= 73
- Bravais lattice + screw axis = 41
- Bravais lattice + glide plane = 116





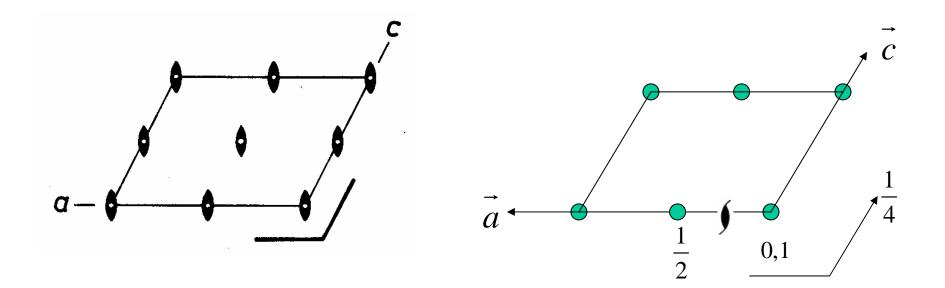
	<b>.</b>		· · · ·	
Three dimensions Triclinic	None			
Monoclinic*	[010] ('uniq [001] ('uniq			
Orthorhombic	[100]	[010]	[001]	
Tetragonal	[001]	{[100]} {[010]}	{[1Ī0] {[110]}	
Hexagonal	[001]	{[100] [010] [[I]0]	$ \left\{ \begin{bmatrix} 1 \ I 0 \\ [120] \\ [2I0] \\ \end{bmatrix} \right\} $	
Rhombohedral (hexagonal axes)	[001]	$ \left\{ \begin{matrix} [100] \\ [010] \\ [110] \end{matrix} \right\} $		
Rhombohedral (rhombohedral axes)	[111]	$ \begin{cases} [1\bar{1}0] \\ [01\bar{1}] \\ [\bar{1}01] \end{cases} $		
Cubic	([100]) [010] [[001]}	$ \begin{pmatrix} [111] \\ [1fI] \\ [1fI] \\ [I1I] \\ [I1I] \\ [I1I] \end{pmatrix} $	$ \left\{ \begin{matrix} [1\bar{I}0] \ [110] \\ [01\bar{I}] \ [011] \\ [101] \ [101] \end{matrix} \right\} $	



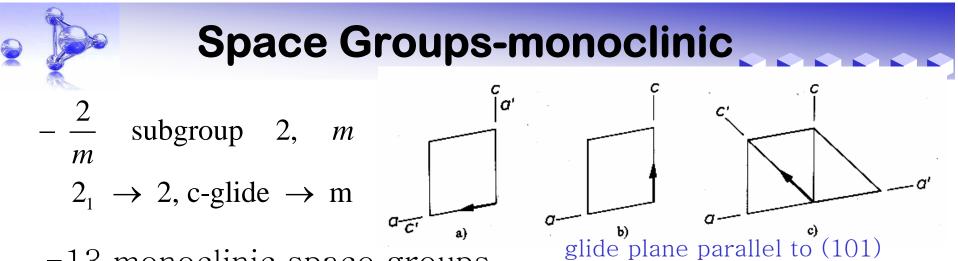


monoclinic system- highest symmetry

$$P\frac{2}{m}, \qquad C\frac{2}{m} \text{ (a-glide at } x, \frac{1}{4}, z, \ x, \frac{3}{4}, z \\ 2_1 \text{ screw axis at } \frac{1}{4}, y, 0, \ \frac{1}{4}, y, \frac{1}{2}, \ \frac{3}{4}, y, 0, \ \frac{3}{4}, y, \frac{1}{2})$$



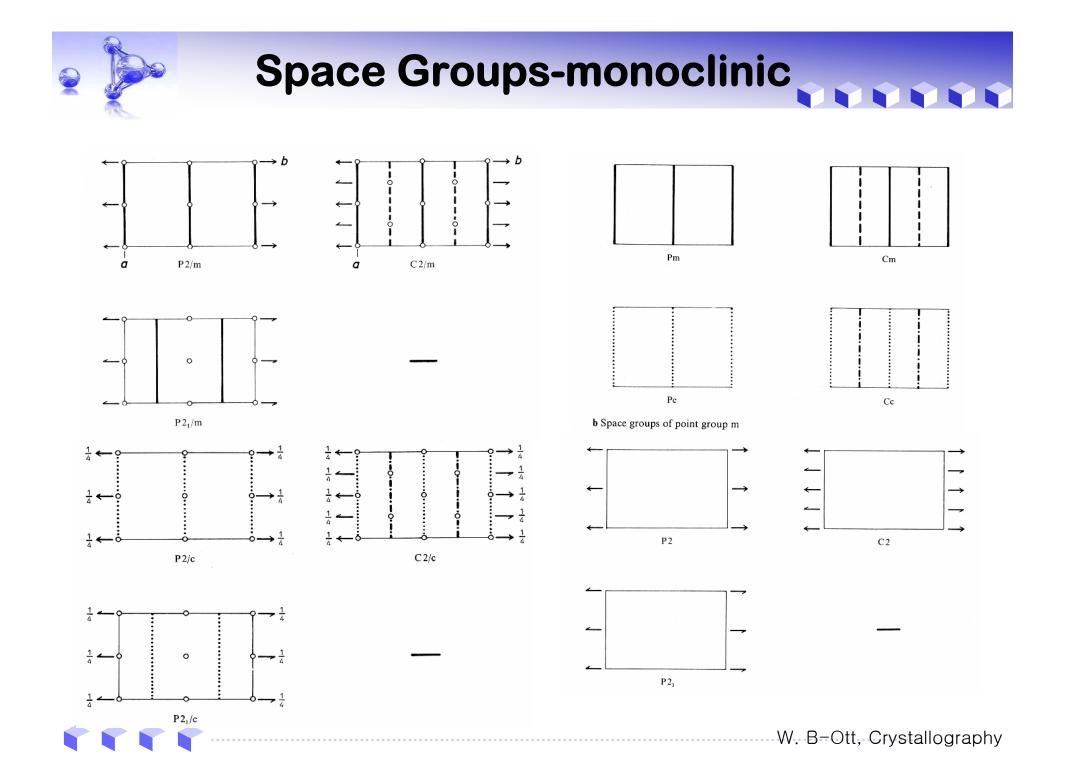




-13 monoclinic space groups

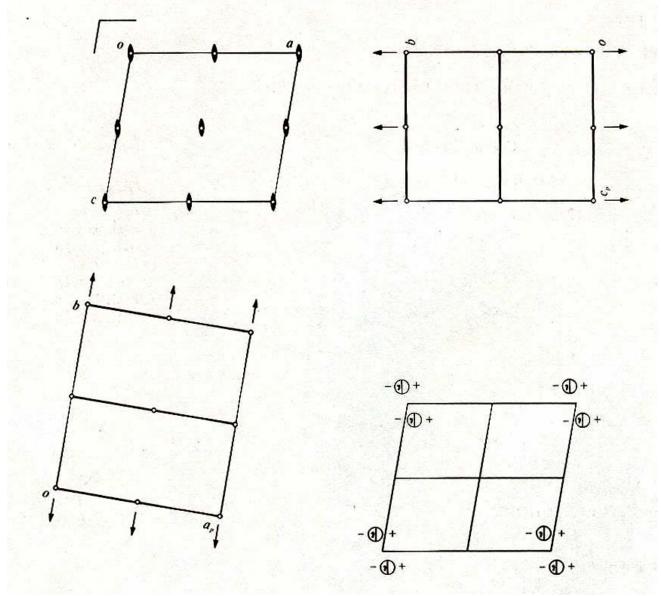
Point groups	Space groups		
2/m	$\begin{array}{c} P2/m\\ P2_1/m\\ P2/c\\ P2_1/c \end{array}$	C2/m _ ^a C2/c _ ^b	
m	Pm Pc	Cm Cc	
2	P2 P2 ₁	C2 _°	
$C2_1/m \equiv C2/m,$	^b C2 ₁ /c = C2	$c_{\rm c}$ , $c_{\rm C2_1} = C_{\rm C2_2}$	









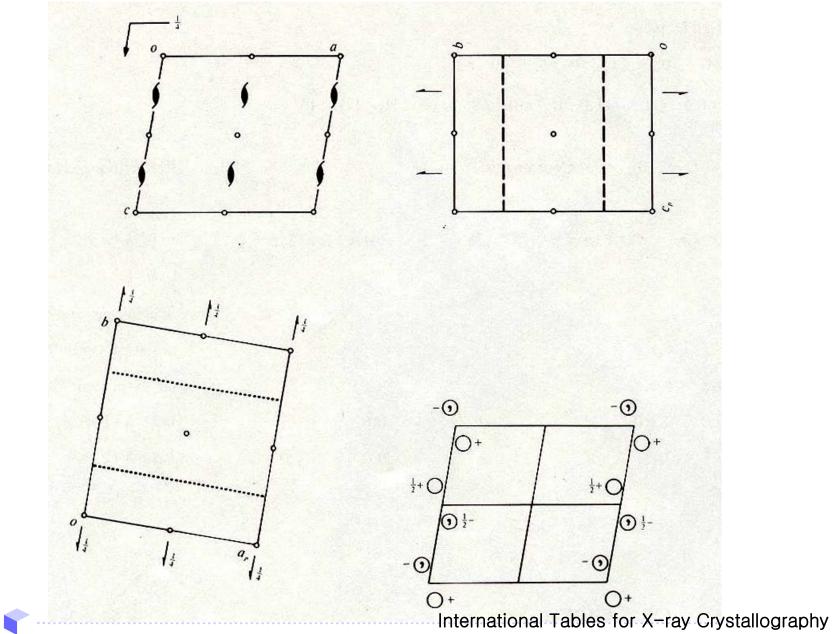


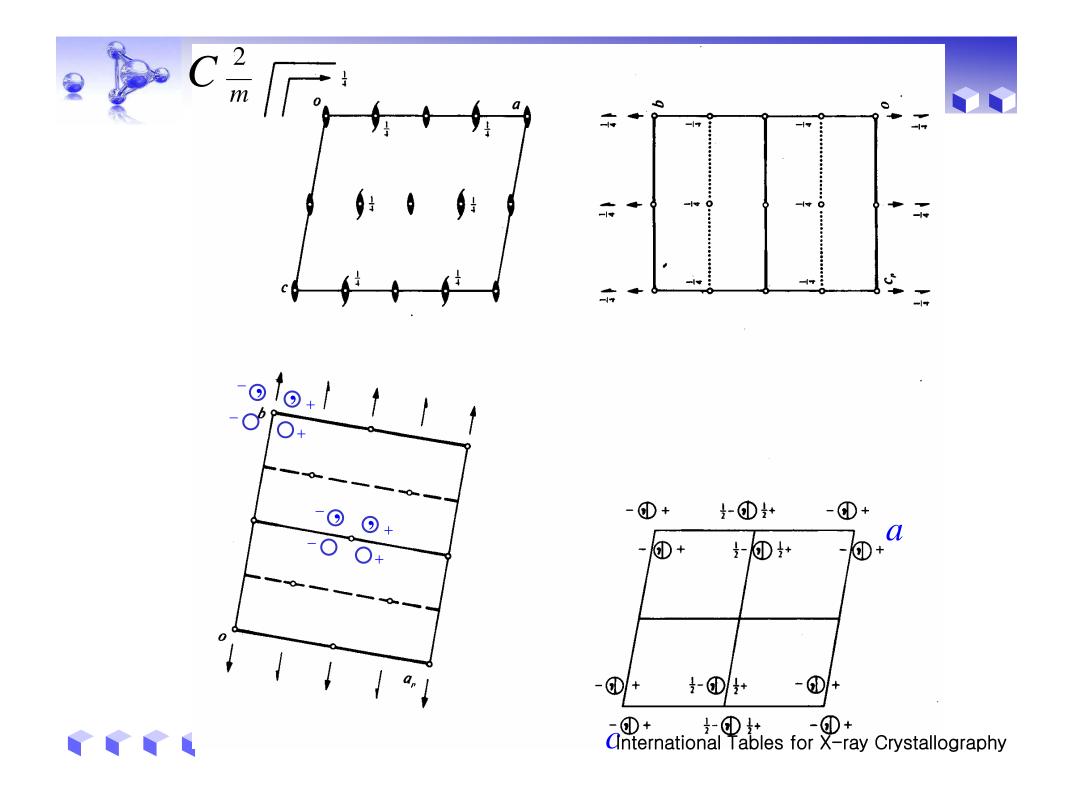


International Tables for X-ray Crystallography











#### 1.4. Graphical symbols for symmetry elements in one, two, and three dimensions

(a) Symmetry planes normal to the plane of projection (three dimensions) and symmetry lines in the plane of the figure (two dimensions)

Symmetry plane or symmetry line	Graphical symbol	Glide vector in units of lattice translation vectors parallel and normal to the projection plane	Printed symbol
Reflection plane, mirror plane Reflection line, mirror line (two dimensions)		None	т
'Axial' glide plane Glide line (two dimensions)		$\frac{1}{2}$ along line parallel to projection plane $\frac{1}{2}$ along line in plane	a,b or c g
'Axial' glide plane 'Diagonal' glide plane		$\frac{1}{2}$ normal to projection plane $\frac{1}{2}$ along line parallel to projection plane, combined with $\frac{1}{2}$ normal to projection plane	a,b or c n
'Diamond' glide plane (pair of planes; in centred cells only)		$\frac{1}{4}$ along line parallel to projection plane, combined with $\frac{1}{4}$ normal to projection plane (arrow indicates direction parallel to the projection plane for which the normal component is positive)	d



International Tables for X-ray Crystallography



Orthorhombic

Patterson symmetry Pmmm



*Pmm* 2

Pmm2

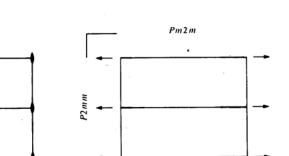
No. 25



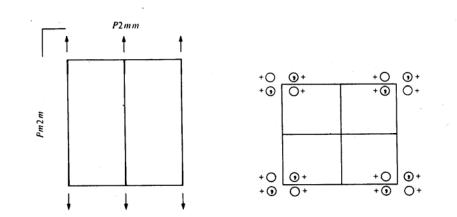
Pmm2

 $C_{2v}^1$ 

*m m* 2



short space group symbol Schoenflies symbol point group crystal system number of space group full space group symbol



projection of symmetry elements projection of general position

Origin on mm2

Asymmetric unit  $0 \le x \le \frac{1}{2}; \quad 0 \le y \le \frac{1}{2}; \quad 0 \le z \le 1$ 

Symmetry operations

(1) 1 (2) 2 0,0,z (3) m x,0,z (4) m 0,y,z

eeee.

International Tables for X-ray Crystallography



Positions

**Generators selected** (1); t(1,0,0); t(0,1,0); t(0,0,1); (2); (3)

Wy		letter,		C	oordinates		Reflection conditions
		netry 1 (1)	x,y,z	(2) $\bar{x}, \bar{y}, z$	(3) $x, \bar{y}, z$	(4) $\bar{x}, y, z$	General: no conditions
							Special: no extra conditions
2	h	<i>m</i>	$\frac{1}{2}$ , y, z	$\frac{1}{2}, \overline{y}, z$			۲.
2	8	<i>m</i>	0, y, z	$0, \bar{y}, z$			
2	f	. <i>m</i> .	$x, \frac{1}{2}, z$	$\bar{x}, \frac{1}{2}, z$			
2	е	. <i>m</i> .	x,0,z	<i>x</i> ,0, <i>z</i>			
1	d	<i>m m</i> 2	$\frac{1}{2}, \frac{1}{2}, Z$				
1	с	<i>m m</i> 2	$\frac{1}{2}, 0, z$				
1	b	<i>m m</i> 2	$0, \frac{1}{2}, z$				
1	а	<i>m m</i> 2	0,0, <i>z</i>				

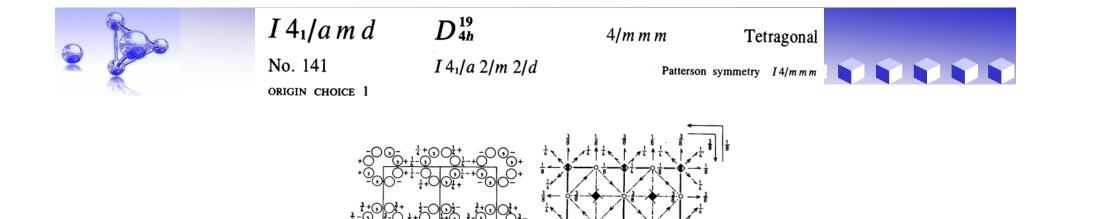
International Tables for X-ray Crystallography



- origin

- (i) all centrosymmetric space groups are described with an inversion centers as origin.a second description is given if a space group contains points of high site symmetry that do not coincide with a center of symmetry
- (ii) for non-centrosymmetric space groups, the origin is at a point of highest site symmetry. if no site symmetry is higher than 1, the origin is placed on a screw axis or a glide plane, or at the intersection of several such symmetry elements





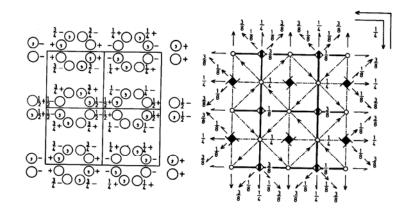
**Origin** at  $\bar{4}m2$ , at  $0, \frac{1}{4}, -\frac{1}{4}$  from centre (2/m)

 $I 4_1/a m d$  $D_{4h}^{19}$ 4/m m mNo. 141  $I 4_1/a 2/m 2/d$ 

Patterson symmetry I4/mmm

Tetragonal

ORIGIN CHOICE 2





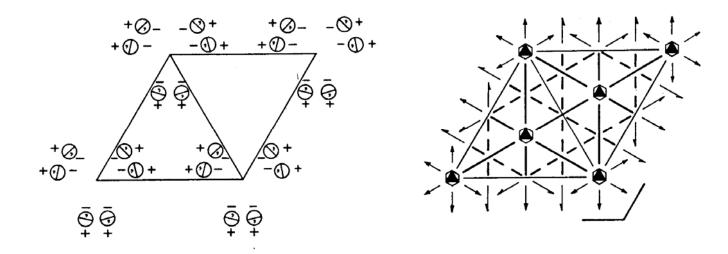
International Tables for X-ray Crystallography





 $\overline{6}m2$  Hexagonal

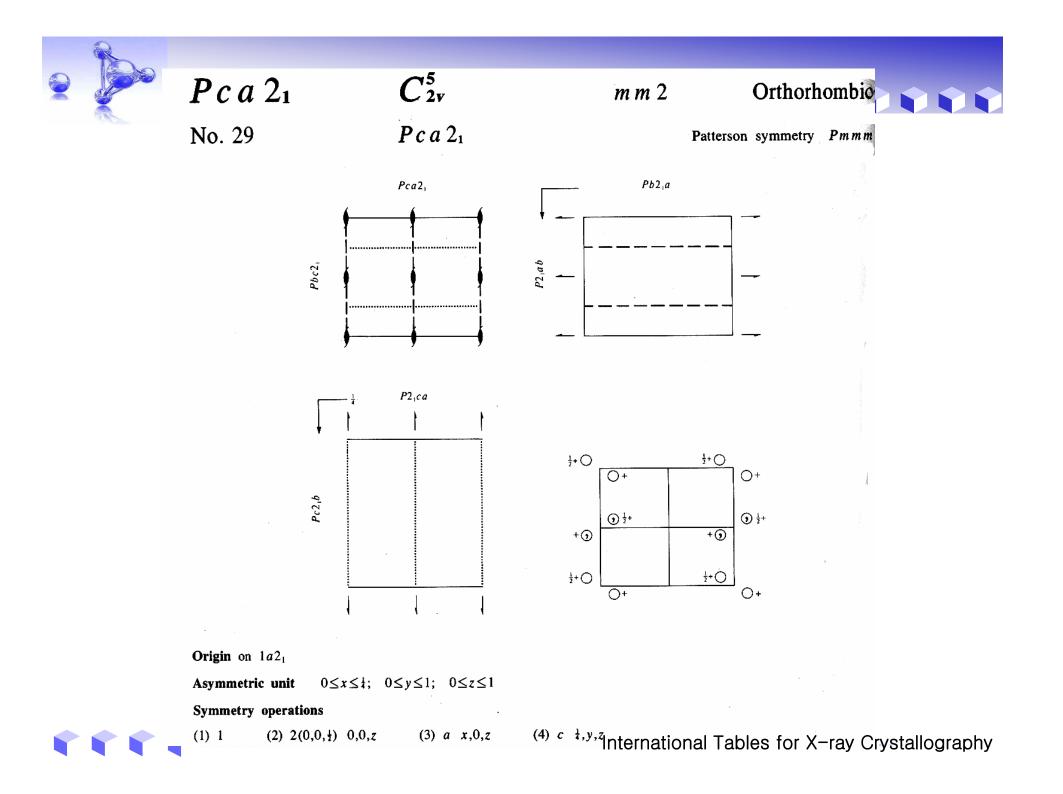
Patterson symmetry P6/mmm



**Origin** at  $\bar{6}m$  2

Asymmetric unit $0 \le x \le \frac{2}{3}$ ; $0 \le y \le \frac{2}{3}$ ; $0 \le z \le \frac{1}{2}$ ; $x \le 2y$ ; $y \le \min(1-x,2x)$ Vertices0,0,0 $\frac{2}{3},\frac{1}{3},0$  $\frac{1}{3},\frac{2}{3},0$  $\frac{1}{3},\frac{2}{3},\frac{1}{3},\frac{1}{2}$ 

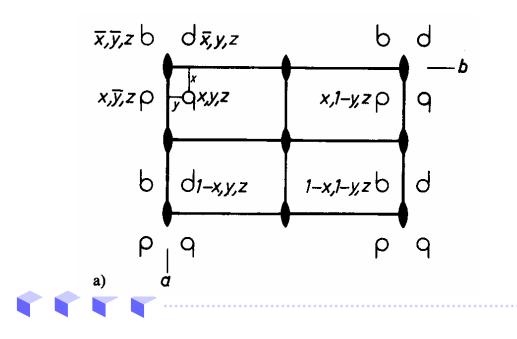








- Pmm2- for a point x, y, z (general point) symmetry element generates x, y, z; x, y, z; x, y, z x, y, z; x, y, z; x, y, z; x, y, z are equivalent (multiplicity of 4)
- The number of equivalent points in the unit cell is called its multiplicity.
- A general position is a set of equivalent points with point symmetry (site symmetry) 1.



W. B-Ott, Crystallography



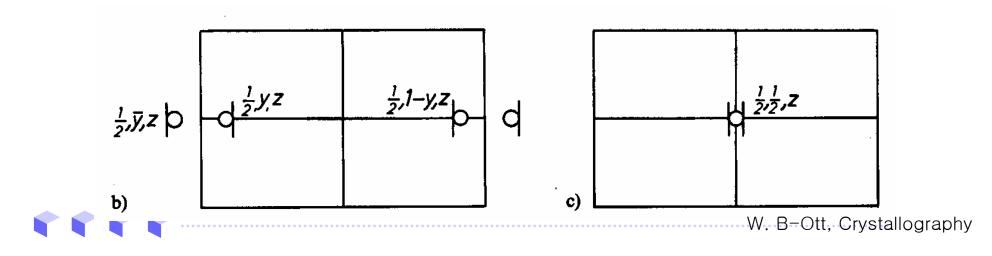
- move a point x, y, z on to mirror plane at  $\frac{1}{2}$ , y, z

x, y, z and 1-x, y, z coalesce to 
$$\frac{1}{2}$$
, y, z

$$x, 1-y, z$$
 and  $1-x, 1-y, z$  coalesce to  $\frac{1}{2}, 1-y, z$ 

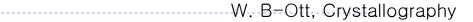
multiplicity of 2
as long as the point remains on the mirror plane,
its multiplicity is unchanged- degree of freedom 2
A special position is a set of equivalent points with

point symmetry (site symmetry) higher than 1.





Position	Degrees of freedom	Multi- plicity	Site symmetry	Coordinates of equivalent points
general	3	4	1	x,y,z; x̄,ȳ,z; x,ȳ,z; x̄,y,z
		2	m	$\frac{1}{2}$ , y, z; $\frac{1}{2}$ , $\overline{y}$ , z
	2	2	m	0, y, z; 0, <u>y</u> , z
		2	m	$x, \frac{1}{2}, z; \bar{x}, \frac{1}{2}, z$
special		2	m	x,0,z; x̄,0,z
special		1	mm2	$\frac{1}{2}, \frac{1}{2}, \mathbf{Z}$
	1	1	mm2	$\frac{1}{2}$ , 0, z
		1	mm2	$0, \frac{1}{2}, z$
		1	mm2	0, 0, z

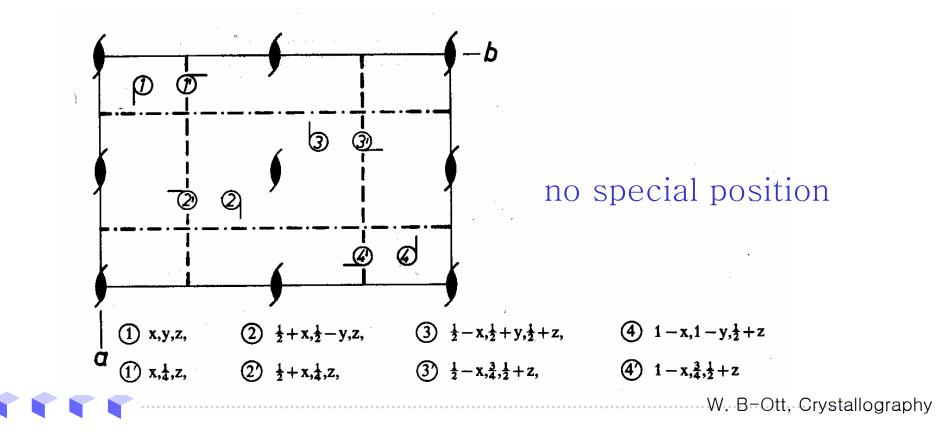






- screw axis and glide plane do not alter the multiplicity of a point
- $-Pna2_1$ : orthorhombic

n-glide normal to a-axis a-glide normal to b-axis 2₁ screw axis along c-axis





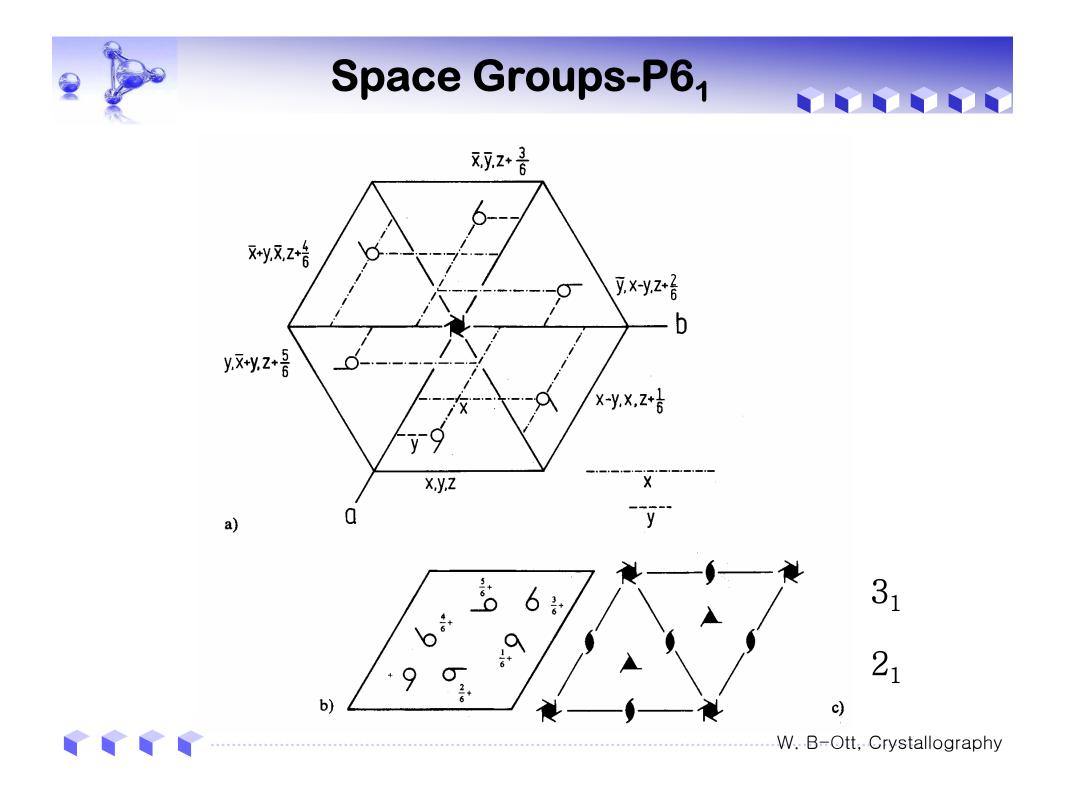
-The asymmetric unit of a space group is the smallest part of the unit cell from which the whole cell may be filled by the operation of all the symmetry operations. It volume is given by:

$$V_{\text{asymm.unit}} = \frac{V_{\text{unit cell}}}{\text{multiplicity of general position}}$$

ex) Pmm2- multiplicity of 4, vol. of asymm=1/4 unit cell  $0 \le x \le \frac{1}{2}, \ 0 \le y \le \frac{1}{2}, \ 0 \le z \le 1$ 

-An asymmetric unit contains all the information necessary for the complete descript of a crystal structure.

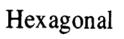






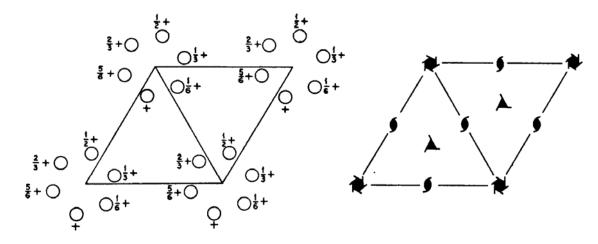


 $C_6^2$ 





Patterson symmetry P6/m



#### Origin on 61

Asymmetric unit	$0 \le x \le 1$	; $0 \leq y$	≤1; 0≤	≤z≤ł
Vertices	0,0,0	1,0,0	1,1,0	0,1,0
	0,0, <del>}</del>	1,0,‡	1,1,‡	0,1,1

#### Symmetry operations

(1) 1	0,0, <i>z</i>	(2) $3^+(0,0,\frac{1}{3})$ 0,0,z	(3) $3^{-}(0,0,\frac{2}{3})$ $0,0,z$
(4) $2(0,0,\frac{1}{2})$		(5) $6^-(0,0,\frac{1}{3})$ 0,0,z	(6) $6^{+}(0,0,\frac{2}{3})$ $0,0,z$
$\langle \cdot \rangle = \langle \cdot \rangle \cdot \langle \cdot \rangle$	-,-,-	(-) - (-)-)0) -)0,0	(0) 0 (0,0,0) 0,0,2

Generators selected (1); t(1,0,0); t(0,1,0); t(0,0,1); (2); (4)

#### Positions

Multiplicity, Wyckoff letter Site symmetry	,	Coordinates	5	Reflection conditions
				General:
6 a 1	(1) $x, y, z$	(2) $\bar{y}, x-y, z+\frac{1}{3}$	(3) $\bar{x} + y, \bar{x}, z + \frac{2}{3}$	000l : l = 6n
	(4) $\bar{x}, \bar{y}, z + \frac{1}{2}$	(5) $y, \bar{x} + y, z + \frac{2}{6}$	(6) $x-y, x, z+\frac{1}{6}$	International Tables for X-ray Crystallography

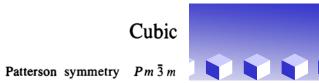


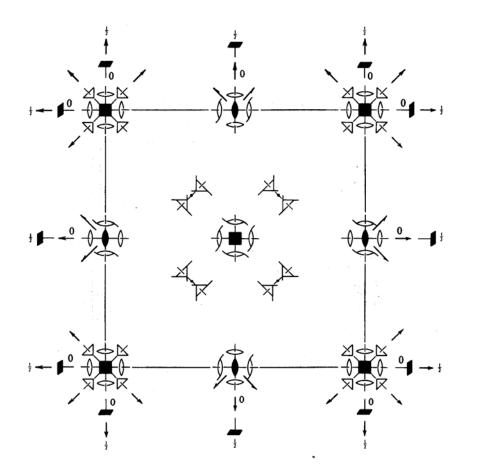
P432

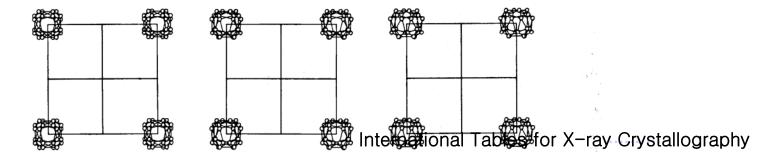


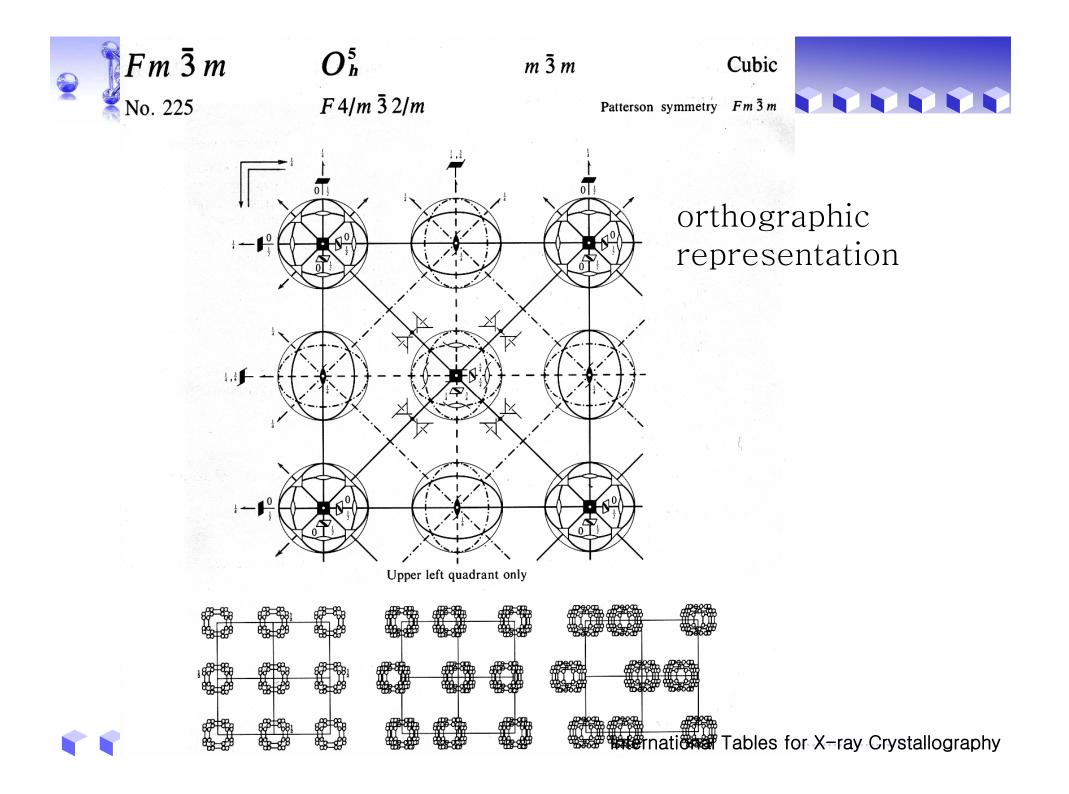
P432

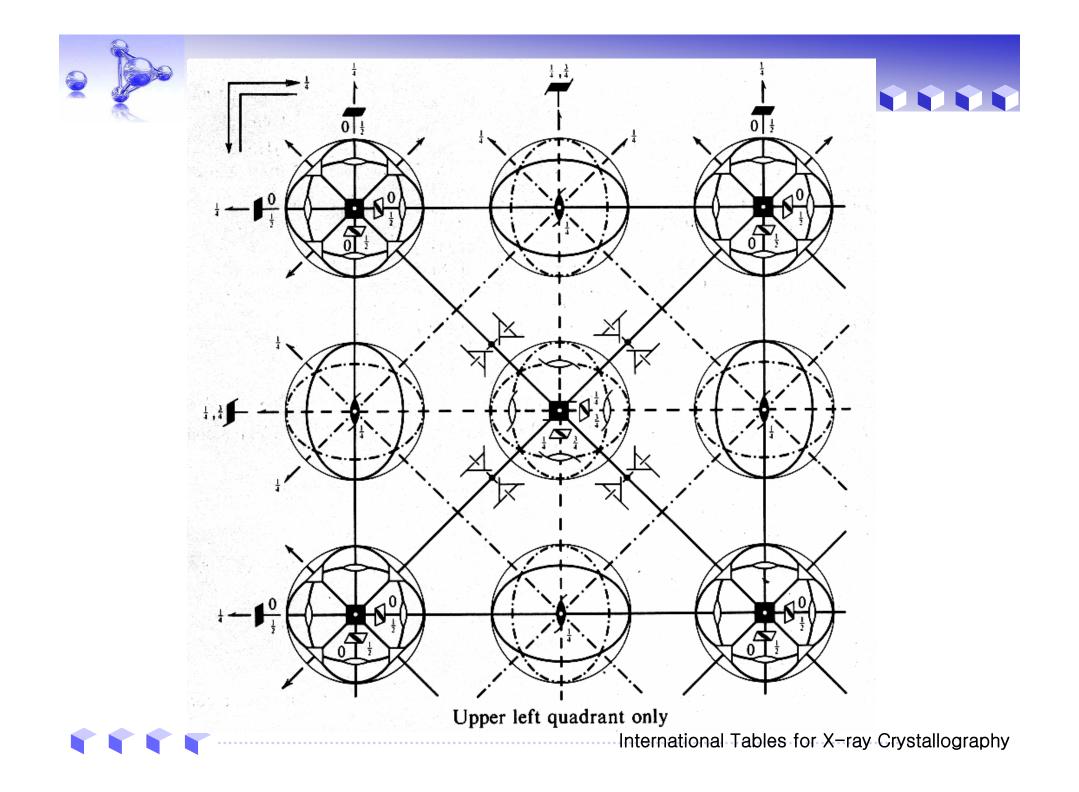
 $O^1$ 













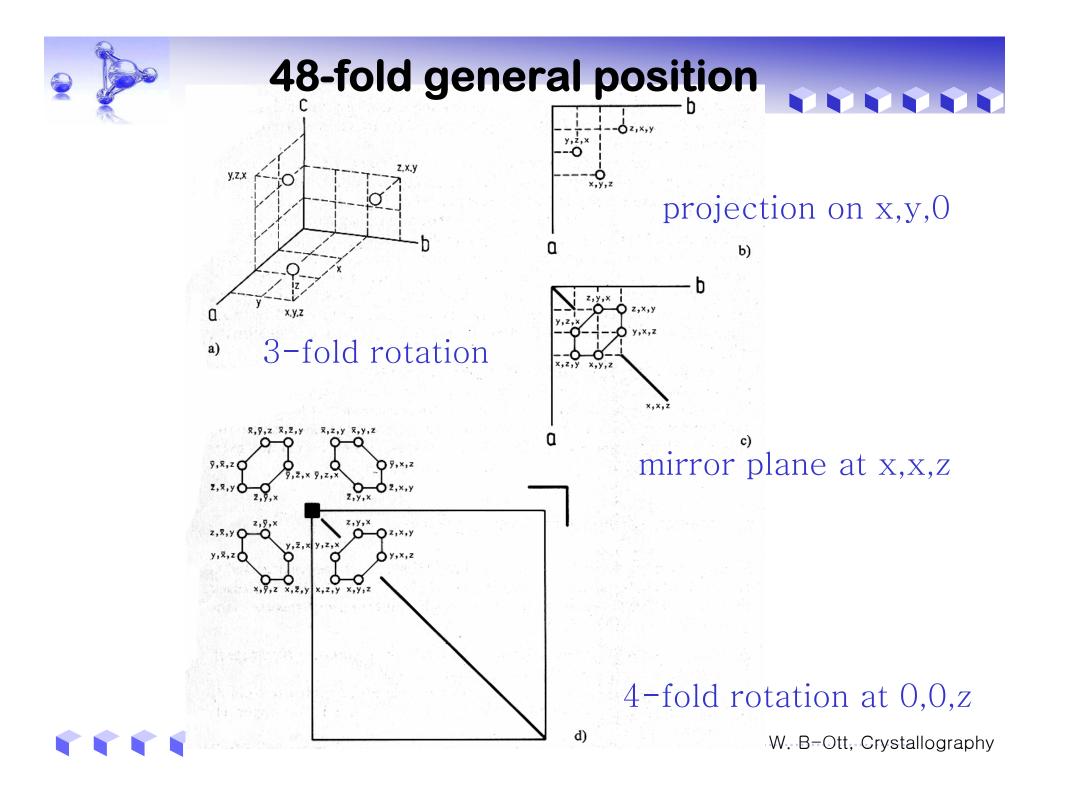
#### (e) Symmetry axes parallel to the plane of projection

Symmetry axis	Graphical symbol	Screw vector of a right-handed screw rotation in units of the shortest lattice translation vector parallel to the axis	Printed symbol
Twofold rotation axis	<ul><li>← →</li></ul>	None	2
Twofold screw axis: '2 sub 1'	4 <del>-</del>	$\frac{1}{2}$	2,
Fourfold rotation axis	▶ -	None	4
Fourfold screw axis: '4 sub 1'	₱ ₱	$\frac{1}{4}$	4,
Fourfold screw axis: '4 sub 2'	J⊢ –J	$\frac{1}{2}$	42
Fourfold screw axis: '4 sub 3'	j f − j f	<u>3</u> 4	43
Inversion axis: '4 bar'	<b></b>	None	4

#### (f) Symmetry axes inclined to the plane of projection (in cubic space groups only)

ymmetry axis	Graphical symbol	Screw vector of a right-handed screw rotation in units of the shortest lattice translation vector parallel to the axis	Printed symbol
fold rotation axis	•-(;	None	2
old screw axis: '2 sub 1'		$\frac{1}{2}$	2,
fold rotation axis	K	None	3
fold screw axis: '3 sub 1'	Ж	$\frac{1}{3}$	31
fold screw axis: '3 sub 2'	¥	<u>2</u> 3	32
ion axis: '3 bar'	×.	International Tables f	or X-ray Crv



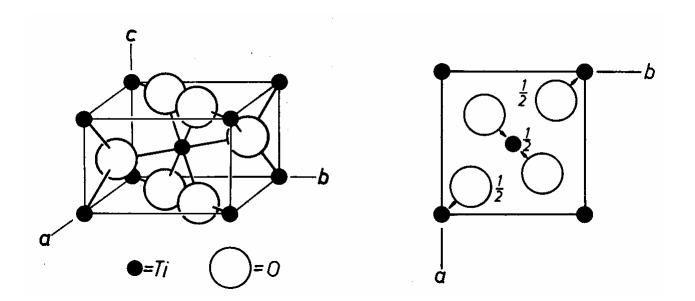




# Rutile, TiO₂



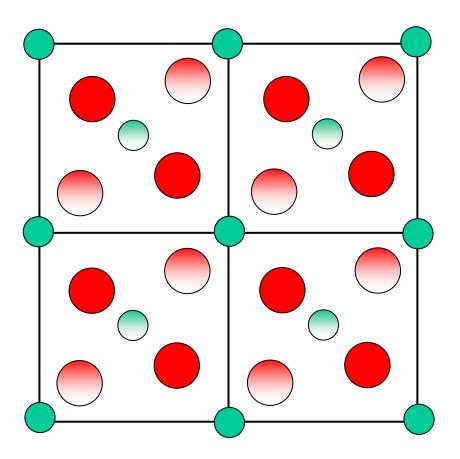
·	A			В		
Lattice Basis		Space group		Positions of the atoms		
tetragonal P	Ti: 0, 0, 0 $\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$	P 4 ₂ /mnm	а	Ti: 0,0,0 $\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$		
$a_0 = 4.59 \text{ Å}$ $c_0 = 2.96 \text{ Å}$	O: 0.3, 0.3, 0 0.8, 0.2, $\frac{1}{2}$ 0.2, 0.8, $\frac{1}{2}$ 0.7, 0.7, 0	$a_0 = 4.59 \text{ Å}$ $c_0 = 2.96 \text{ Å}$	f	O: x, x, 0 $\frac{1}{2} + x, \frac{1}{2} - x, \frac{1}{2}$ $\frac{1}{2} - x, \frac{1}{2} + x, \frac{1}{2}$ $\bar{x}, \bar{x}, 0$ x = 0.3		



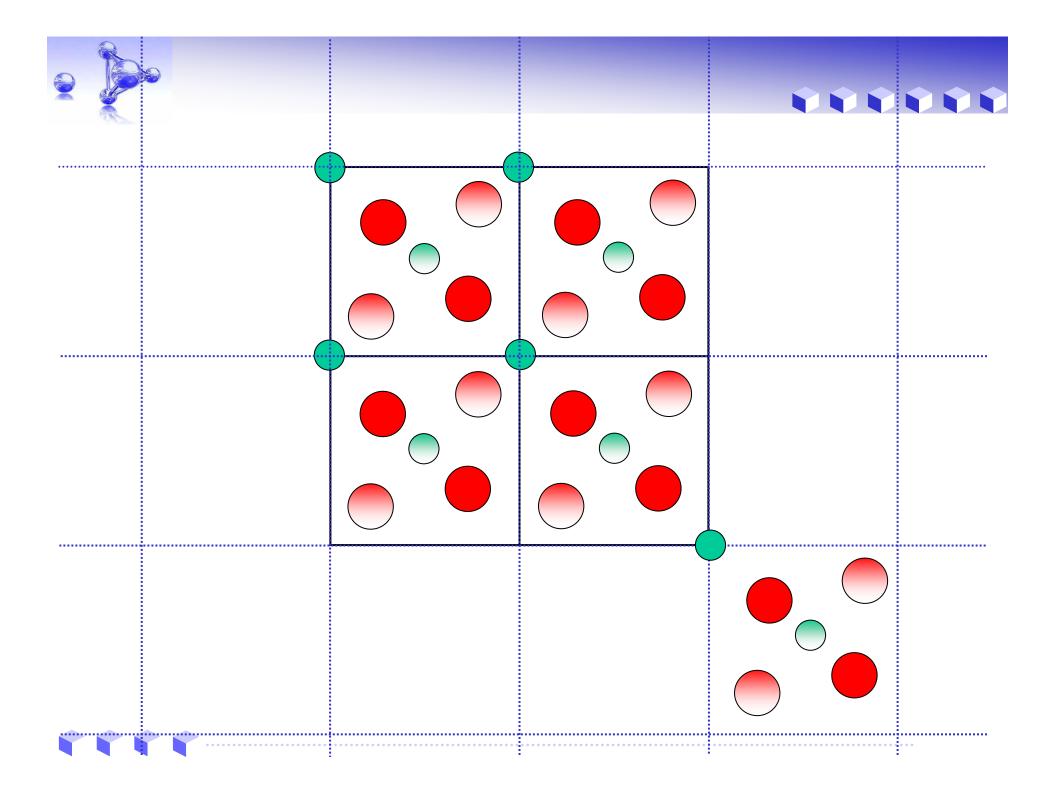


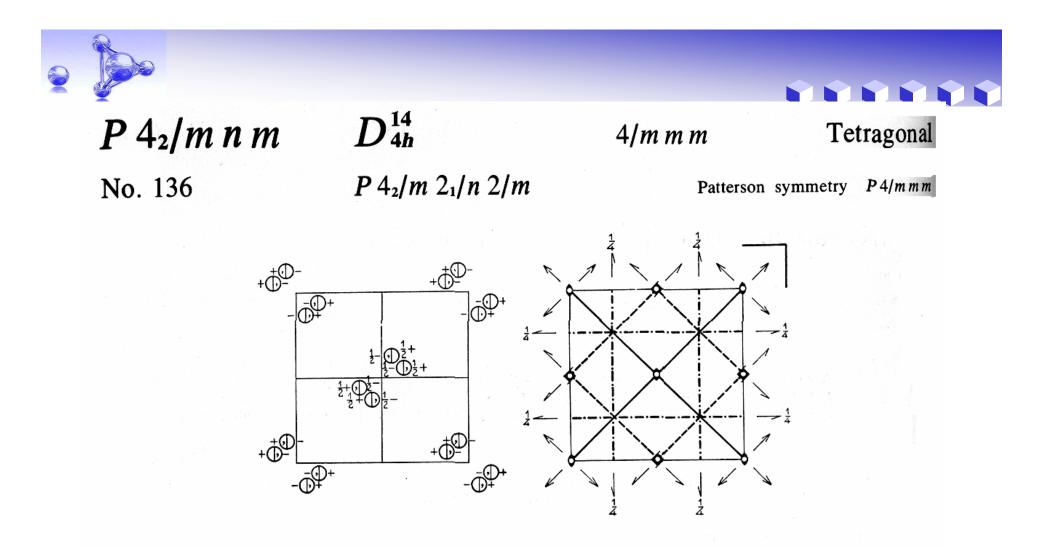
W. B-Ott, Crystallography











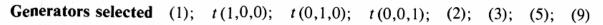
**Origin** at centre (mmm) at 2/m 12/m

Asymmetric unit  $0 \le x \le \frac{1}{2}$ ;  $0 \le y \le \frac{1}{2}$ ;  $0 \le z \le \frac{1}{2}$ ;  $x \le y$ 

#### Symmetry operations

(1) 1	(2) 2 $0,0,z$	(3) $4^+(0,0,\frac{1}{2})$ $0,\frac{1}{2},z$	$(4) \ 4^{-}(0,0,\frac{1}{2}) \ \frac{1}{2},0,z$
(5) $2(0, \frac{1}{2}, 0) = \frac{1}{4}, y, \frac{1}{4}$	(6) $2(\frac{1}{2}, 0, 0) = x, \frac{1}{4}, \frac{1}{4}$	(7) 2 x, x, 0	(8) $\frac{2}{2} x, \bar{x}, 0$
$(9)$ $\bar{1}$ 0.0.0	(10) m x, y, 0	(11) $\bar{4}^+$ $\frac{1}{2},0,z; \frac{1}{2},0,\frac{1}{4}$	(12) $\bar{4}^-$ 0, $\frac{1}{2}$ ,z; 0, $\frac{1}{2}$ , $\frac{1}{4}$
(13) $n(\frac{1}{2}, 0, \frac{1}{2}) x, \frac{1}{4}, z$	(14) $n(0,\frac{1}{2},\frac{1}{2}) = \frac{1}{4}, y, z$	(15) $m x, \bar{x}, z$	(16) $m  x, x, z$
		Internatio	onal Tables for X-ray Crystallography





Coordinates

Positions

Multiplicity, Wyckoff letter, Site symmetry Reflection conditions

					General:
16 k 1	(1) $x, y, z$	(2) $\bar{x}, \bar{y}, z$	(3) $\bar{y} + \frac{1}{2}, x + \frac{1}{2}, z + \frac{1}{2}$	(4) $y + \frac{1}{2}, \bar{x} + \frac{1}{2}, z + \frac{1}{2}$	0kl: k+l = 2n
	(5) $\bar{x} + \frac{1}{2}, y + \frac{1}{2}, \bar{z} + \frac{1}{2}$		(7) $y, x, \overline{z}$	(8) $\bar{y}, \bar{x}, \bar{z}$	00l: l = 2n
	(9) $\bar{x}, \bar{y}, \bar{z}$	(10) $x, y, \overline{z}$	(11) $y + \frac{1}{2}, \bar{x} + \frac{1}{2}, \bar{z} + \frac{1}{2}$	(12) $\bar{y} + \frac{1}{2}, x + \frac{1}{2}, \bar{z} + \frac{1}{2}$	h00: h = 2n
	(13) $x + \frac{1}{2}, \bar{y} + \frac{1}{2}, z + \frac{1}{2}$	(14) $\bar{x} + \frac{1}{2}, y + \frac{1}{2}, z + \frac{1}{2}$	(15) $\bar{y}, \bar{x}, z$	(16) $y, x, z$	

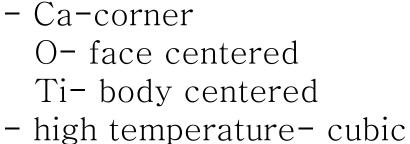
Special: as above, plus

8	j	<i>m</i>	x, x, z $\bar{x} + \frac{1}{2}, x + \frac{1}{2}, \bar{z} + \frac{1}{2}$	$\bar{x}, \bar{x}, z$ $x + \frac{1}{2}, \bar{x} + \frac{1}{2}, \bar{z} + \frac{1}{2}$	$\bar{x} + \frac{1}{2}, x + \frac{1}{2}, z + \frac{1}{2}$ $x, x, \bar{z}$	$x + \frac{1}{2}, \overline{x} + \frac{1}{2}, z + \frac{1}{2}$ $\overline{x}, \overline{x}, \overline{z}$	no extra conditions
8	i	<i>m</i>	$\begin{array}{ccc} x, y, 0 & \bar{x} \\ \bar{x} + \frac{1}{2}, y + \frac{1}{2}, \frac{1}{2} & x \end{array}$	$\bar{y}, \bar{y}, 0$ $\bar{y} + \frac{1}{2}, \bar{y} + \frac{1}{2}, \frac{1}{2}$ $y, x, \bar{y}, $	$\begin{array}{ccc} x + \frac{1}{2}, \frac{1}{2} & y + \frac{1}{2}, \bar{x} \\ 0 & \bar{y}, \bar{x}, 0 \end{array}$	+ ½, ½	no extra conditions
8	h	2	$\begin{array}{ccc} 0, \frac{1}{2}, z & 0, \frac{1}{2}, z + \\ 0, \frac{1}{2}, \overline{z} & 0, \frac{1}{2}, \overline{z} + \end{array}$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0, <i>ī</i> 0, <i>z</i>		hkl: h+k, l=2n
4	g	<i>m</i> .2 <i>m</i>	$x, \overline{x}, 0$ $\overline{x}, x, 0$	$x + \frac{1}{2}, x + \frac{1}{2}, \frac{1}{2}$ $\bar{x}$	$(\bar{x}+\frac{1}{2},\bar{x}+\frac{1}{2},\frac{1}{2})$		no extra conditions
4	f	<i>m</i> .2 <i>m</i>	$x, x, 0$ $\overline{x}, \overline{x}, 0$	$\bar{x} + \frac{1}{2}, x + \frac{1}{2}, \frac{1}{2}$ x	$(+\frac{1}{2}, \bar{x}+\frac{1}{2}, \frac{1}{2})$		no extra conditions
4	е	2. <i>m</i> m	$0,0,z$ $\frac{1}{2},\frac{1}{2},z+z$	$\frac{1}{2}$ $\frac{1}{2}, \frac{1}{2}, \overline{z} + \frac{1}{2}$ 0,	0, <i>ī</i>		hkl: h+k+l=2n
4	d	<b>4</b>	$0,\frac{1}{2},\frac{1}{4}$ $0,\frac{1}{2},\frac{3}{4}$	$\frac{1}{2}, 0, \frac{1}{4}$ $\frac{1}{2}, 0, \frac{3}{4}$			hkl: h+k, l=2n
4	с	2/m	$0,\frac{1}{2},0$ $0,\frac{1}{2},\frac{1}{2}$	$\frac{1}{2},0,\frac{1}{2}$ $\frac{1}{2},0,0$			hkl: h+k, l=2n
2	b	<i>m</i> . <i>m m</i>	$0,0,\frac{1}{2}$ $\frac{1}{2},\frac{1}{2},0$				hkl: h+k+l=2n
2	а	<i>m</i> . <i>m m</i>	$0,0,0$ $\frac{1}{2},\frac{1}{2},\frac{1}{2}$				hkl: h+k+l=2n
		<b>.</b>				nternational T	ables for X–ray Crysta

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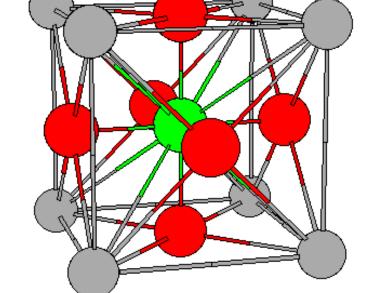
# **Perovskite, CaTiO₃**



high temperature – cubic
 Pm3m (No.221)

*Ca*: 1*a*,  $m\bar{3}m$ , 0,0,0

*Ti*: 1b, 
$$m\bar{3}m$$
,  $\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$ 

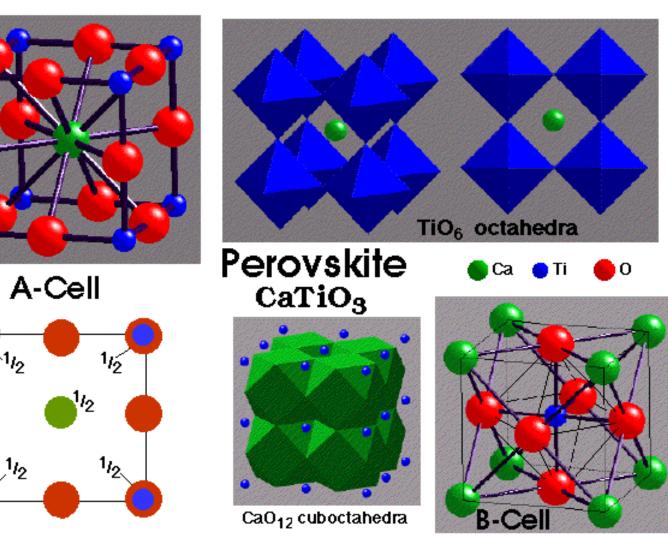


*O*: 3*c*, 4/*mmm*, 
$$0, \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, 0, \frac{1}{2}, \frac{$$



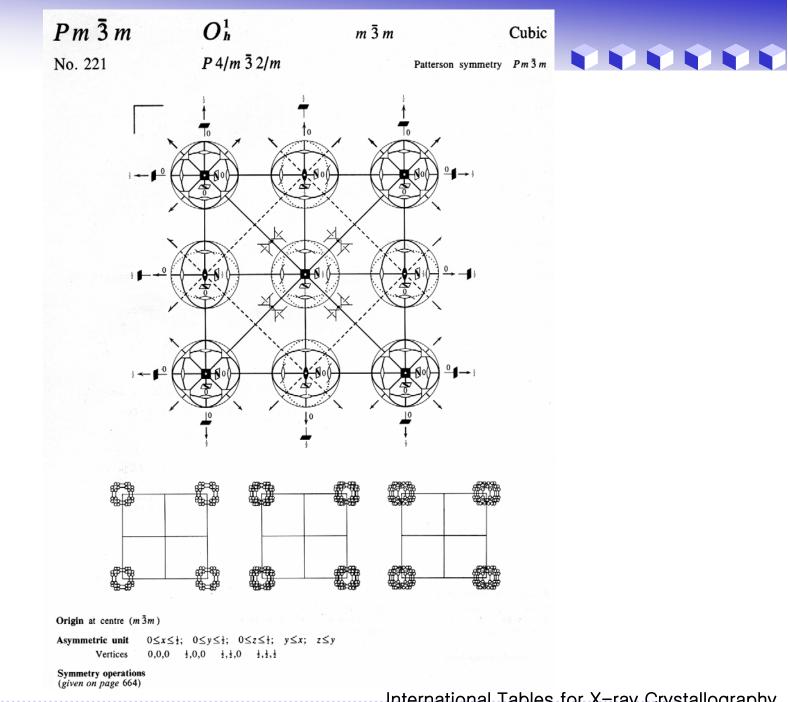






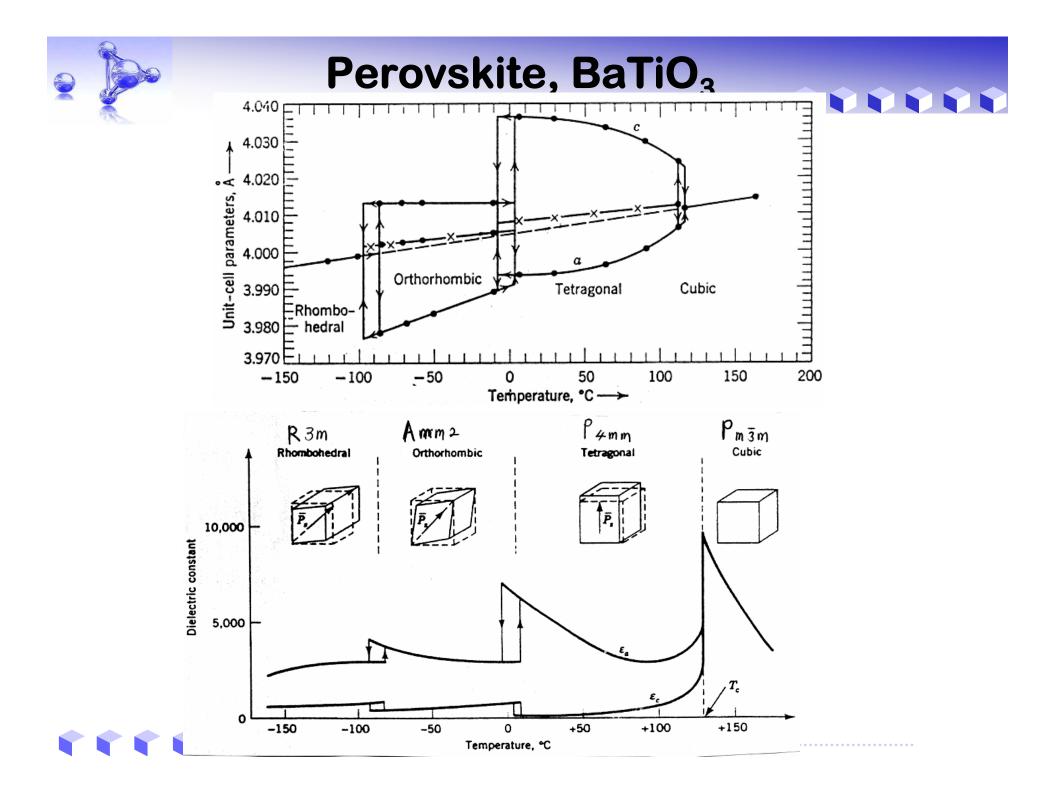


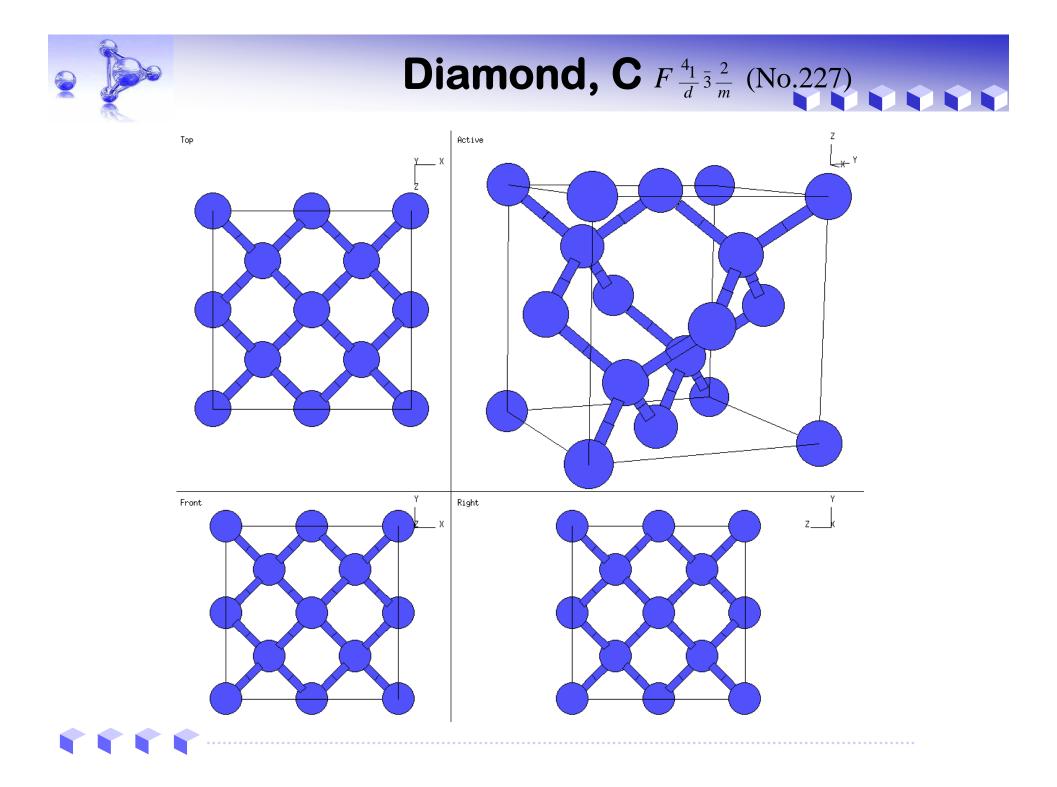






	со	NTI	NUED						No. 2	221			Pm 3m			
	Ger	nera	tors selecte	d (1);	t(1,0,0);	t (0,1,0	D); t(0,	0,1); (2	); (3); (5);	(13);	(25)					
ā.	Positions															
	Mult Wycl Site	iplicity koff le symm	city, Coordinates								Reflectio	on conditions	5			
											h,k,l per General:					
	48	n	1 (1) x (5) z (9) y (13) y (17) x (21) z (25) x (29) z (33) y (37) y (41) x	,x,y ,z,x ,x,z ,y,x ,y,x ,y,z ,x,y ,z,x ,z,z	(2) x, y, z (6) z, x, y (10) y, z, x (14) y, x, z (18) x, z, y (22) z, y, z (26) x, y, z (30) z, x, y (34) y, z, x (42) x, z, y	(11 (15 (19) (23) (27) (31) (35) (39)	) x, y, z ) z, x, y ) y, z, x ) y, x, z ) x, x, y ) z, y, x ) z, x, y ) y, z, x ) y, z, x ) y, z, x ) y, z, x ) y, z, y	(4) 2 (8) 2 (12) 5 (16) 5 (20) 2 (24) 2 (28) 3 (32) 2 (36) 5 (40) 5 (44) 5	, ž, x , x, z , ž, y , y, x , y, z , x, y , z, x , x, ž		no condi					
			(45) <i>ž</i>	, ÿ, x	(46) <i>z</i> , y, <i>x</i>	č (47	) z,ÿ,x	(48) z			Special:	no extra co	nditions			
	24	m	<i>m</i>	x,x,z	x,x,z	<i>x</i> , <i>x</i> , <i>ž</i>	x, x, z	z,x,x	z, <b>x</b> , x		-					
				z,x,x x,x,z x,z,x	z,x,x x,x,z x,z,x	x,z,x x,X,z z,x,X	x,z,x x,x,z z,x,x	x,Z,X x,Z,X Z,X,X	x,z,x x,z,x z,x,x							
	24	1	<i>m</i>	1, y, z z, 1, y y, 1, z 1, z, y	1/2, y, z z, 1/2, y y, 1/2, z 1/2, z, y	1/2, y, Z y, z, 1/2 y, 1/2, z z, y, 1/2	1/2, ỹ, Ĩ ỹ, z, 1/2 ỹ, 1/2, z z, ỹ, 1/2	z, ±, y y, z, ± ±, z, y z, y, ±	z, ½, ỹ ỹ, ž, ½ ½, z, y ž, ỹ, ½							
	24	k	<i>m</i>	0,y,z ž,0,y y,0,ž 0,ž,ỹ	0, ÿ, z ž, 0, ÿ ÿ, 0, ž 0, ž, y	0, y, ž y, z, 0 y, 0, z z, y, 0	0, y, ž y, z, 0 y, 0, z z, y, 0	z,0,y y,ž,0 0,z,y ž,y,0	z,0,ÿ ÿ,ž,0 0,z,y ž,ÿ,0		3	d	4/ <i>m</i> m .m	$\frac{1}{2},0,0$	$0, \frac{1}{2}, 0$	$0, 0, \frac{1}{2}$
	12	j	<i>m</i> . <i>m</i> 2	1, y, y 9, 1, y	1/2, ÿ, y ÿ, 1/2, ÿ	1/2, y, y y, y, 1/2	1/2, ÿ, ÿ ÿ, y, 1/2	у, <u>‡</u> ,у у,ӯ,±	y, ±, ÿ ÿ, ÿ, ±							
	12	i	<i>m</i> . <i>m</i> 2	0,y,y	0,ÿ,y	0,y,ÿ	0, <u>9</u> , <u>9</u>	y,0,y	y,0,y		3	С	4/mm.m	$0, \frac{1}{2}, \frac{1}{2}$	$\frac{1}{2}, 0, \frac{1}{2}$	$\frac{1}{2}, \frac{1}{2}, 0$
		,		ÿ,0,y	ğ,0, <u>ğ</u>	y,y,0	<u></u> y,y,0	у, <u></u> ,0	y,y,0				,	- , . , .	.,.,.	2,2,0
	12	n	m m 2	$x, \frac{1}{2}, 0$ $\frac{1}{2}, x, 0$	<i>x</i> , <u>↓</u> ,0 <u>↓</u> , <i>x</i> ,0	$0, x, \frac{1}{2}$ $x, 0, \frac{1}{2}$	0,\$,\$ \$,0,\$	$\frac{1}{2},0,x$ $0,\frac{1}{2},x$	$\frac{1}{2}, 0, \vec{x}$ $0, \frac{1}{2}, x$		1	L		5 1 1		
	8	8	. 3 <i>m</i>	x,x,x x,x,x	x,x,x x,x,x	x,x,x x,x,x	x,\$,\$ \$,x,x				1	b	тĪт	$\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$		
	6	f	4 <i>m</i> . <i>m</i>	x, ±, ±	x, ±, ±	1,x,1	1,x,1	$\frac{1}{2}, \frac{1}{2}, x$	$\frac{1}{2}, \frac{1}{2}, \vec{x}$				_			
	6	е	4 <i>m</i> . <i>m</i>	x,0,0	x,0,0	0,x,0	0, <b>x</b> ,0	0,0,x	0,0, <i>x</i>		1	а	m 3m	0,0,0		
	3	d	4/ <i>m m .m</i>	±,0,0	0, <del>1</del> ,0	0,0, <del>1</del>								0,0,0		
	3	с	4/ <i>m</i> m .m	0, ½, ½	±,0,±	±,±,0										
		Ь	m 3m -	1,1,1												
		a	m 3m	0,0,0												
			ry of speci DO1] p4m			long [1]	1] p6n	n m			Along	[110] p 2n				
	<b>a</b> '=	8	b' = b t 0,0,z		8	$f = \frac{1}{3}(2a - rigin at$	<b>b</b> - <b>c</b> )		a+2 <b>b</b> -c)		a' = 1/2.	(110) p 2n -a+b) lat x,x,0	$\mathbf{c}' = \mathbf{c}$			







 $Fd\bar{3}m$ 

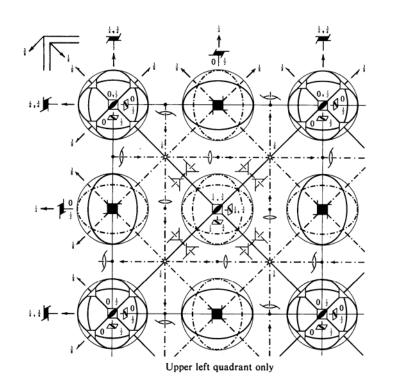
 $O_h^7$  $F 4_1/d \,\overline{3} \, 2/m$ 

m 3 m

Cubic

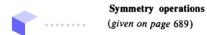
Patterson symmetry  $Fm\bar{3}m$ 

No. 227 origin choice 1



**Origin** at  $\overline{4}3m$ , at  $-\frac{1}{4}$ ,  $-\frac{1}{4}$ ,  $-\frac{1}{4}$  from centre  $(\overline{3}m)$ 

Asymmetric unit $0 \le x \le \frac{1}{2}$ ; $0 \le y \le \frac{1}{2}$ ; $-\frac{1}{2} \le z \le \frac{1}{2}$ ; $y \le \min(\frac{1}{2} - x, x)$ ; $-y \le z \le y$ Vertices $0, 0, 0, \frac{1}{2}, 0, 0, \frac{1}{2}, \frac{1$ 





### No. 227

Fd3m



Generators selected (1); t(1,0,0); t(0,1,0); t(0,0,1);  $t(0,\frac{1}{2},\frac{1}{2})$ ;  $t(\frac{1}{2},0,\frac{1}{2})$ ; (2); (3); (5); (13); (25)

Positions

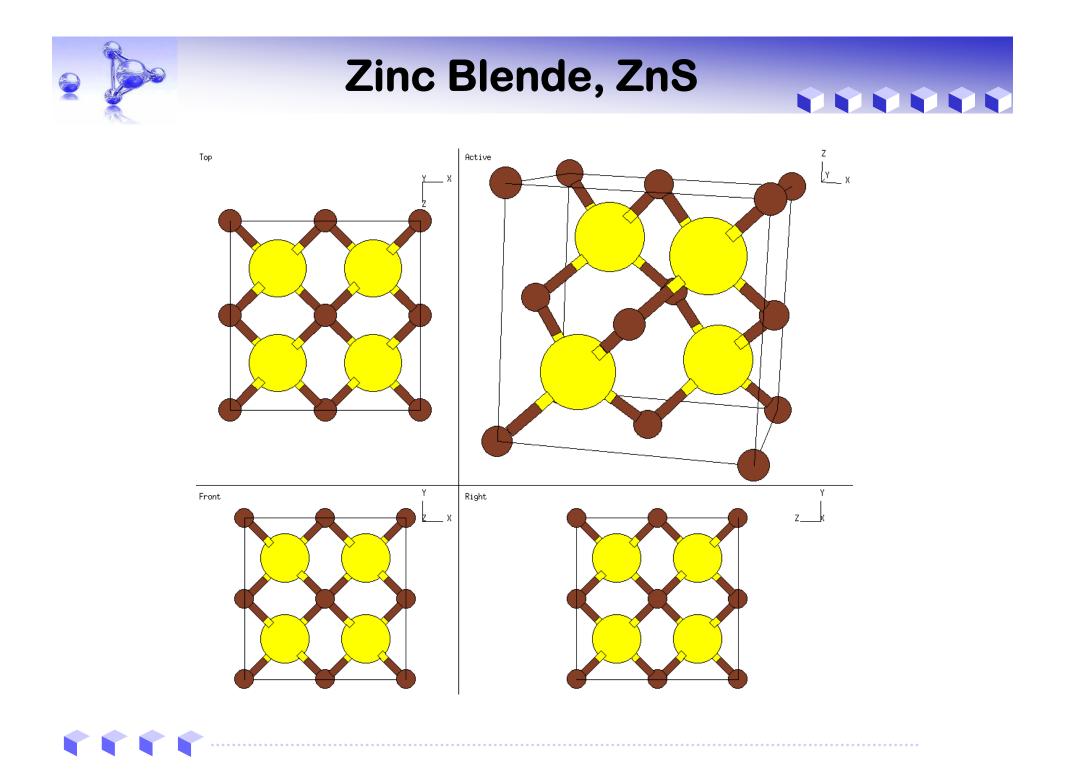
	Positi	ions	5																	
Multiplicity, Wyckoff letter,					(	Coord	inate	es										Reflection conditions		
	Site syr	nmet	ry		(0,0,0	0)+	(0,	ł, <u>ł</u> )+		( <del>1</del> ,0,	<del>1</del> )+	(	±,±,0	)+						<i>h,k,l</i> permutable General:
	192	i	ł	(5) (9) (13) (17) (21) (25) (29) (33) (37) (41)	$x + \frac{1}{2}, x +$	,		(6) z 10) y 14) y 18) x 22) z 26) x 30) z 34) y 38) y 42) x	$+\frac{1}{2},$ $+\frac{1}{2},$ $+\frac{1}{2},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ $+\frac{1}{4},$ +1		2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	(7) (11) (15) (19) (23) (27) (31) (35) (39) (43)	$\overline{z}, \overline{x}^+$ $y + \frac{1}{2}$ $\overline{x} + \frac{1}{2}$ $\overline{z} + \frac{1}{2}$ $\overline{z} + \frac{1}{2}$ $\overline{y} + \frac{1}{2}$ $\overline{y} + \frac{1}{2}$ $\overline{y} - \frac{1}{2}$	$, y + \frac{1}{2}, y + \frac{1}{2}, y + \frac{1}{2}, y + \frac{1}{2}, \frac{1}{2}, \frac{1}{2} + \frac{1}{2}, \frac{1}{2}, \frac{1}{2} + \frac{1}{2}, \frac{1}{2}, \frac{1}{2} + \frac{1}{2}, \frac{1}{2$	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}$	(8) (12) (16) (20) (24) (28) (32) (36) (40) (44)	$x + \frac{1}{2}, z + \frac{1}{2}, y, z + \frac{1}{2}, y + \frac{1}{2}, z + $	x+1 x+1 x+1 x+1 x+1 x+1 x+1 x+1	$ \frac{1}{y} $ $ 1$	hkl: h+k=2n  and  h+l, k+l=2n $0kl: k+l=4n  and  k, l=2n$ $hhl: h+l=2n$ $h00: h=4n$
																			Specia	al: as above, plus
	96	h	2		\$,y,j y+\$, y,y+ \$,y+ y,\$,j y+\$,j y+\$,	, ŧ, y - ŧ, ŧ - ŧ, y v+ ŧ	ÿ+ ‡ ÿ+ ½ ≹, y+ y+ ½	+ ± , y + , i , y + , y + ± , t , y + , t , y + , y + ±		y+1 y+1 1,y- y+1	+ ½, y , 1, y , y+ + ½, ỹ , ỹ , ỹ+	$+\frac{1}{2}$	y+; ÿ,y ŧ,y ÿ,ŧ	, y + 1 + 1, 1 + 1, 1 + 1, 1 + 1, 1 y + 1 y + 1 y + 1 y + 1					no ex	tra conditions
	96	8	m		$x+\frac{1}{4}$	r	x+ł	z+ x+ x+ x+	1,z+	+ <u>1</u>	1		$\frac{1}{2}, x + \frac{1}{2}, x + 1$	$\frac{1}{2}$ $\frac{1}{2}$ $z + \frac{3}{4}$ $x + \frac{1}{4}$	₹+ ₹,2 ₹+ x+	1,2+	$\frac{1}{2}, \bar{x}$		no ext	tra conditions
	48	f	2. <i>m</i>	m	x,0,0 1,x+		$\vec{x}, \frac{1}{2}, \frac{1}{4}, \vec{x}+$			x,0 +1,1,		$\frac{1}{2}, \bar{x}, \frac{1}{2}, \bar{x}, \frac{1}$		0,0, 1,1,	,x , <del>x</del> + <del>1</del>		1,X 1,x+1			h = 2n + 1 h + k + l = 4n
	32	е	. 3 <i>m</i>		x+1,	x , $x + \frac{1}{2}$ , , $x + \frac{1}{4}$ , , $x + \frac{1}{4}$ , , $x + \frac{1}{4}$ ,	x+1	x+ x+											no ext	tra conditions
	16	d	. 3 <i>m</i>		ŧ,ŧ,i	ł ł	, <del>1</del> , <del>1</del>	<b>₽</b> , <b>₽</b> ,	ł	<b>i</b> ,i,i	ł									h = 2n + 1 h, k, l = 4n + 2
	16	с	. 3 <i>m</i>		ŧ,ŧ,i	7	, <b>i</b> , <b>i</b>	ł,ł,	7	ŧ,ł,i	)									k, k, l = 4n
	8	Ь	43m 43m		1,1,1		, <del>1</del> , <del>1</del>													h = 2n + 1 h + k + l = 4n
	8	а	4 3 m	l.	0,0,0	<i>j</i> 1	,±,₹)													

#### Symmetry of special projections



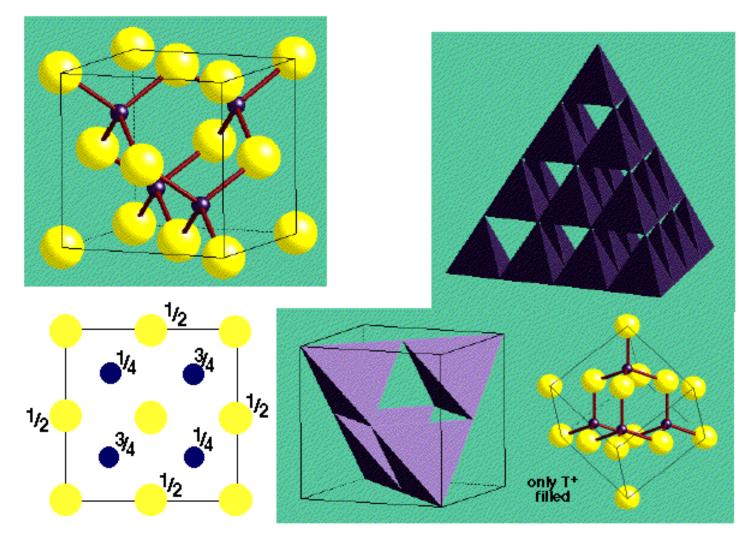
Along [110]  $c^{2mm}$  $a'=\frac{1}{2}(-a+b)$  b'=cInternational^x, Tables for X-ray Crystallography















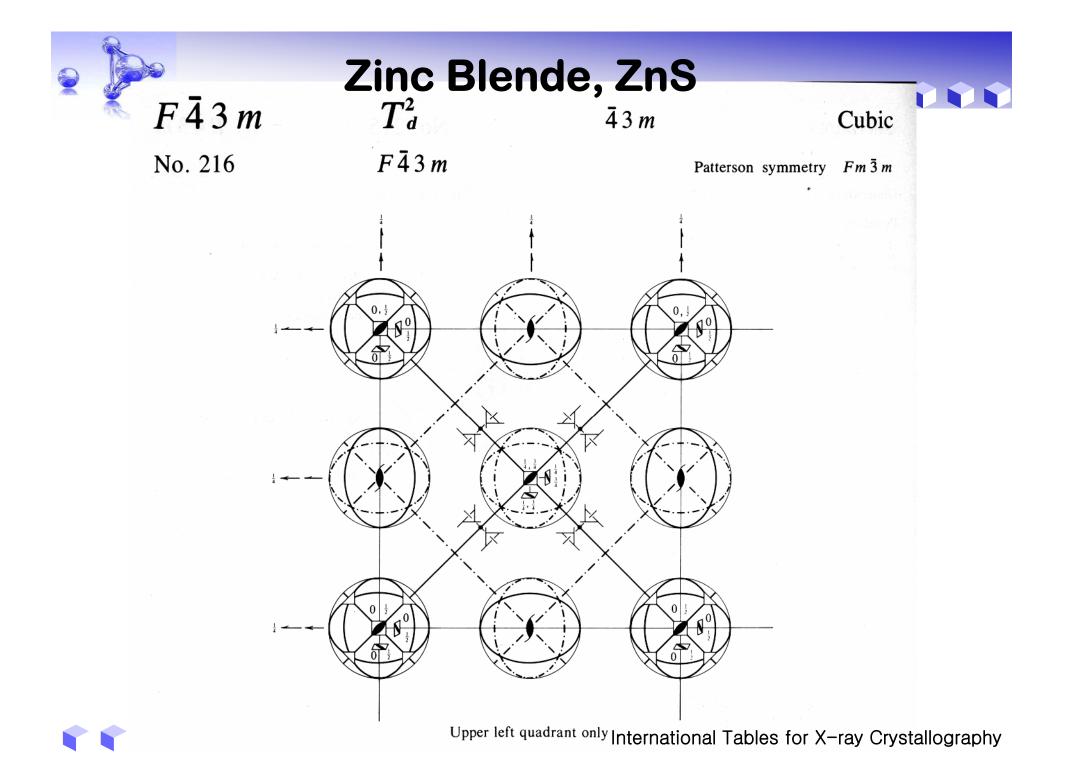




-diamond derivative structure
-Zn and S replace the C atoms
-Zn cubic close packing
S ½ tetrahedral site
-Zn and S cubic close packing displaced by 1/4, 1/4, 1/4
-Space group

 $F\overline{4}3m$  (No.216) Zn: 4a,  $\overline{4}3m$ , 0,0,0 Zn: 4c,  $\overline{4}3m$ ,  $\frac{1}{4}$ ,  $\frac{1}{4}$ ,  $\frac{1}{4}$ 







## Zinc Blende, ZnS

**Generators selected** (1); t(1,0,0); t(0,1,0); t(0,0,1);  $t(0,\frac{1}{2},\frac{1}{2})$ ;  $t(\frac{1}{2},0,\frac{1}{2})$ ; (2); (3); (5); (13)

## Positions

Multiplicity, Wyckoff letter,					Coordin	ates	Reflection conditions		
Site	symm	etry	(0,0,0)+	· (0,	, ½, ½)+	$(\frac{1}{2},0,\frac{1}{2})$	+ ( <del>]</del>	, <u>+</u> ,0)+	<i>h</i> , <i>k</i> , <i>l</i> permutable General:
96	i	(5 (9 (13) (17)	) x,y,z ) z,x,y ) y,z,x ) y,z,z ) y,x,z ) x,z,y ) z,y,x	(2) $\bar{x}$ , (6) $z$ , (10) $\bar{y}$ , (14) $\bar{y}$ , (18) $\bar{x}$ , (22) $z$ ,	$\bar{x}, \bar{y}$ $z, \bar{x}$ $\bar{x}, z$ $z, \bar{y}$	(3) $\bar{x}, y, \bar{z}$ (7) $\bar{z}, \bar{x}, y$ (11) $y, \bar{z}, \bar{x}$ (15) $y, \bar{x}, \bar{z}$ (19) $\bar{x}, \bar{z}, y$ (23) $\bar{z}, y, \bar{x}$	(12) (12) (16) (20)	4) x, y, z 8) z, x, y 2) y, z, x 6) y, x, z 1) x, z, y 4) z, y, x	hkl: h+k,h+l,k+l=2n 0kl: k,l=2n hhl: h+l=2n h00: h=2n
									Special: no extra conditions
48	h	<i>m</i>	x,x,z Ž,X,x	$ar{x},ar{x},z$ $ar{z},x,ar{x}$	x,x,z x,z,x	, , , -	z,x,x x, <del>z</del> , <del>x</del>	$z, \overline{x}, \overline{x}$ $\overline{x}, \overline{z}, x$	
24	8	2. <i>m</i> m	$x, \frac{1}{4}, \frac{1}{4}$	$\bar{x}, \frac{3}{4}, \frac{1}{4}$	1,x,1	$\frac{1}{4}, \overline{x}, \frac{3}{4}$	±,±,x	$\frac{3}{4}, \frac{1}{4}, \overline{x}$	
24	f	2. <i>m</i> m	x,0,0	<i>\$</i> ,0,0	0,x,0	0, <b>x</b> ,0	0,0, <i>x</i>	0,0, <i>x</i>	
16	е	. 3 <i>m</i>	<i>x</i> , <i>x</i> , <i>x</i>	$\bar{x}, \bar{x}, x$	<i>x</i> , <i>x</i> , <i>x</i>	x, x, x			
4	d	<b>ā</b> 3m	1,1,1						
4	с	<b>ā</b> 3m	¥,¥,¥						
4	b	<b>ā</b> 3m	$\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$						
4	а	<b>ā</b> 3m	0,0,0						

