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# Chapter 9

## Medical Imaging

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# Motivation and Overview

- Question:

**“How can we measure the density of atoms of interest in a certain position from the subject, that is, make 3D image of atom densities?”**

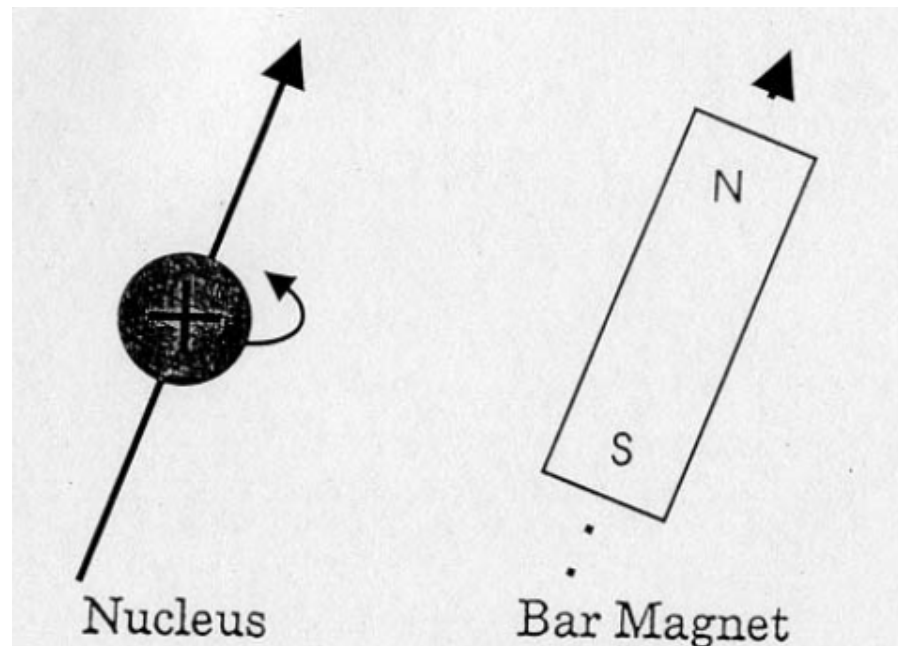
- Solution:

- (1) Choose a species of atom of interest.
- (2) Find an atom-specific physical quantity: the gyromagnetic ratio due to the spin of the nucleus.
- (3) Apply an external gradient magnetic field in order to make the magnetic resonant frequency of nuclei depend on its position.
- (4) Apply RF pulses (electromagnetic waves) for exciting spins in the position of which resonant frequency is same to one of the applied pulses.
- (5) Turn off the pulses then spins are relaxed with emitting electromagnetic waves.
- (6) Detect the emitted waves and calculate the atom density in the position.



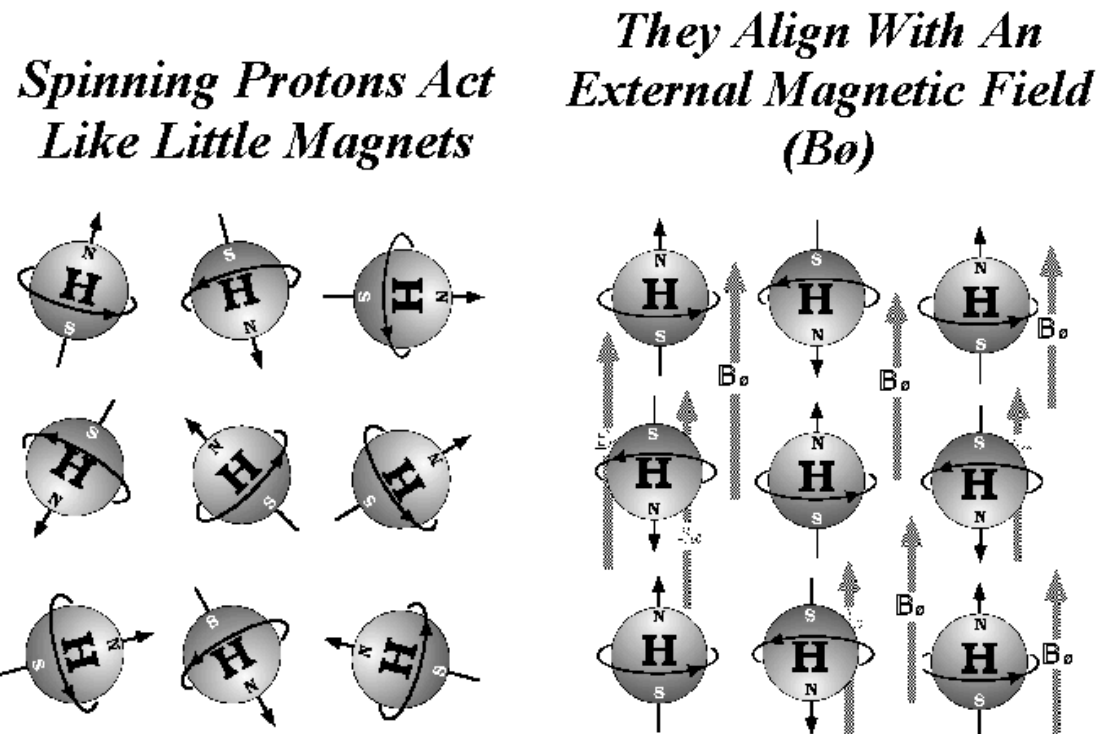
# Spins of the Nucleus

- The intrinsic spin of the nucleus depends on how it is composed of protons and neutrons.
- The nucleus of  $^1\text{H}$  atom (proton) is mostly employed in MRI.
- Z-axis spins of the proton ( $s_z$ ) can have only two values:  $\pm\frac{1}{2}\hbar$



# Spins in an External Uniform Magnetic Field

- Spins of protons align parallel to the field (low energy) or antiparallel to it (high energy).
- The population of two states follows Boltzmann distribution.

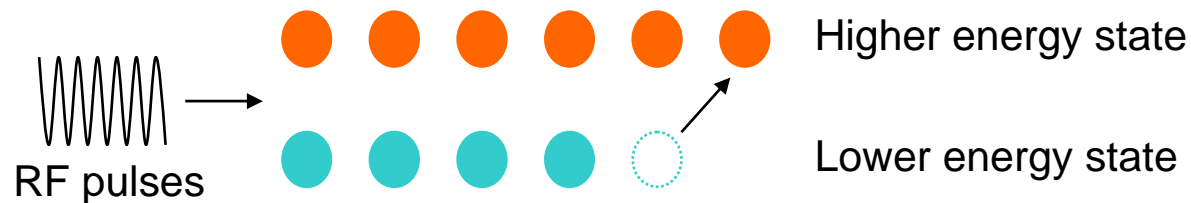


*From James Voyvodic*



# Excitation by RF pulses

- RF pulses = electromagnetic waves
- Apply RF pulses of the resonant frequency to spins at equilibrium.
- Some spins at the lower state go up to the higher state by absorbing energy of the same energy.
- The resonant frequency is nuclei-specific: **Larmor frequency**.



$$\Delta E = 2\mu_z B_o = h\nu$$

$$\nu = \frac{\gamma}{2\pi} B_o : \text{Larmor frequency}$$

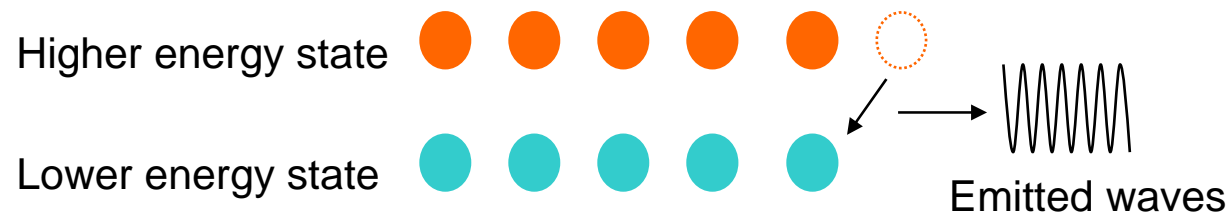
$\gamma$  : gyromagnetic ratio (nuclei - specific constant)

e.g.  $\gamma/2\pi = 42.57\text{MHz}/\text{Tesla}$  for 1H atom (proton)



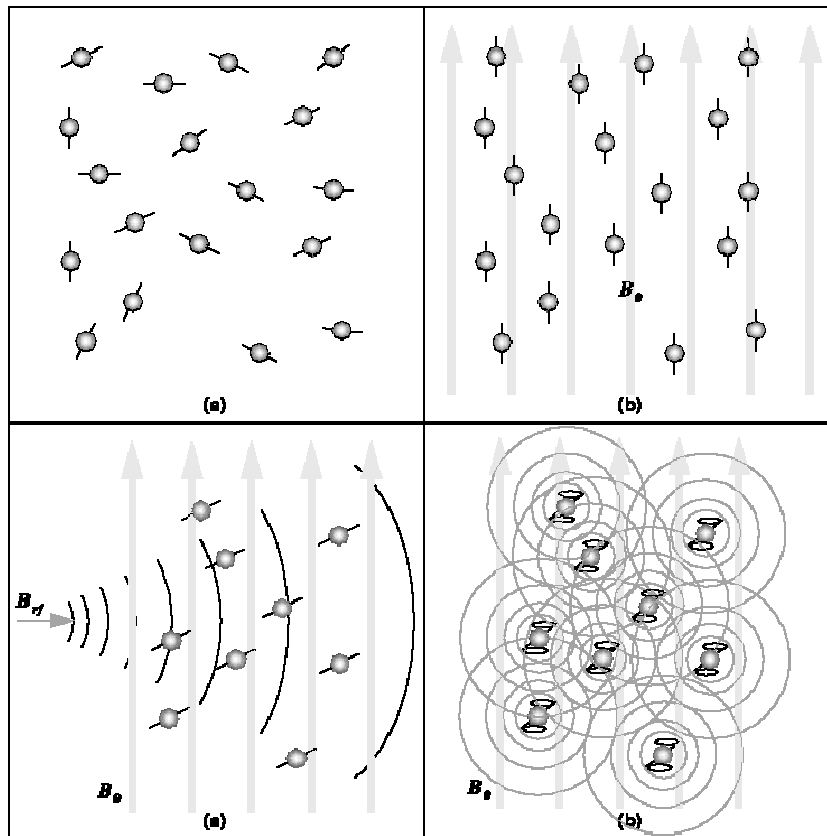
# Relaxation

- Turn off the RF pulses.
- The spin population returns to its original equilibrium: **relaxation**.
- During relaxation, the nuclei lose energy by emitting electromagnetic waves of which frequency is same to the resonant one.



# Net Magnetization $M$ : Macroscopic View

- $M(r,t)$ : sum of magnetic moments of all spins in a small volume (voxel)
- Changes in  $M$  during each process:



- (1) **Thermal equilibrium.** Without  $B_0$  (external uniform magnetic field): the net magnetic moments ( $M$ ) in random fashion
- (2) **Alignment.** Apply  $B_0$ :  $M$  align parallel or antiparallel to  $B_0$ .
- (3) **Excitation.** Apply RF pulses:  $M$  tilt away.
- (4) **Relaxation.** Turn off RF pulses:  $M$  relax (realign) with emitting electromagnetic waves.

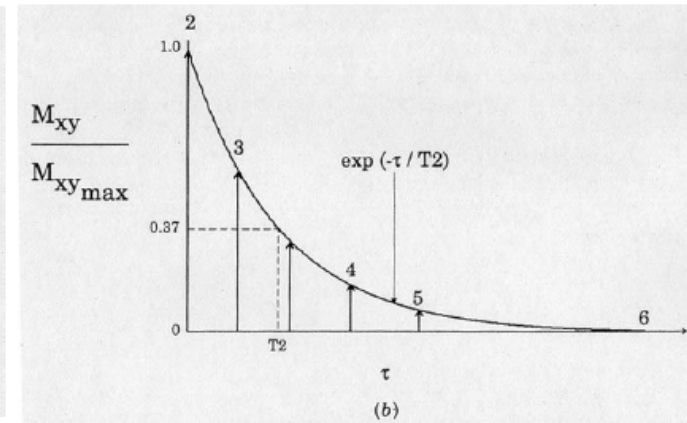
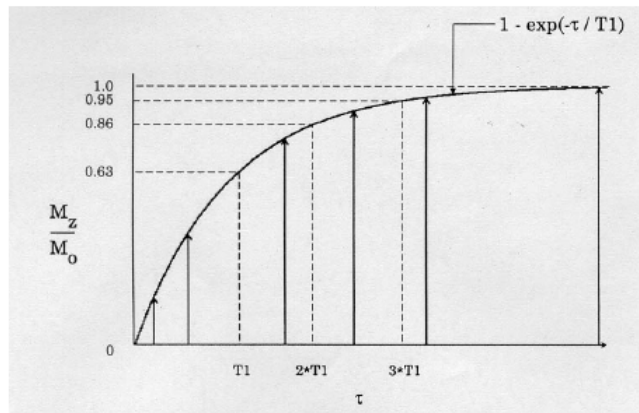
*From Blair Mackiewicz*





# Relaxation of $M$ : FID Response Signal

- Relaxation of  $M$  has two types of decay time.
  - (1) Longitudinal relaxation( spin-lattice interaction) ( $M_z$ ): spins return to its equilibrium at the decay time of  $T1$ .
  - (2) Transverse relaxation(spin-spin interaction) ( $M_{xy}$ ): the coherence in  $M_{xy}$  disappears due to dephasing at  $T2$ .



- Electromagnetic waves emitted during relaxation also have two types of decay time: **free induction decay (FID) response signal**.



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# Image Contrast and 3D Imaging

- Image contrast
  - Without relaxation time: the intensity of the FID signal represents the proton density.
  - T1, T2, T2\* imaging: the relaxation time represents various properties such as chemical environment, magnetic susceptibility, magnetic inhomogeneity, and so on.
  - Diffusion tensor imaging (DTI): diffusion can be measured in multiple directions and the fractional anisotropy in each direction is calculated for each voxel.
- 3D imaging
  - By applying the gradient magnetic field of which amplitudes depend on the position, each voxel can have different Larmor frequency.



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# Conventional MRI: Brain Anatomy

- T1-weighted imaging: gray / white matter
- T2-weighted imaging: tissue / cerebrospinal fluid

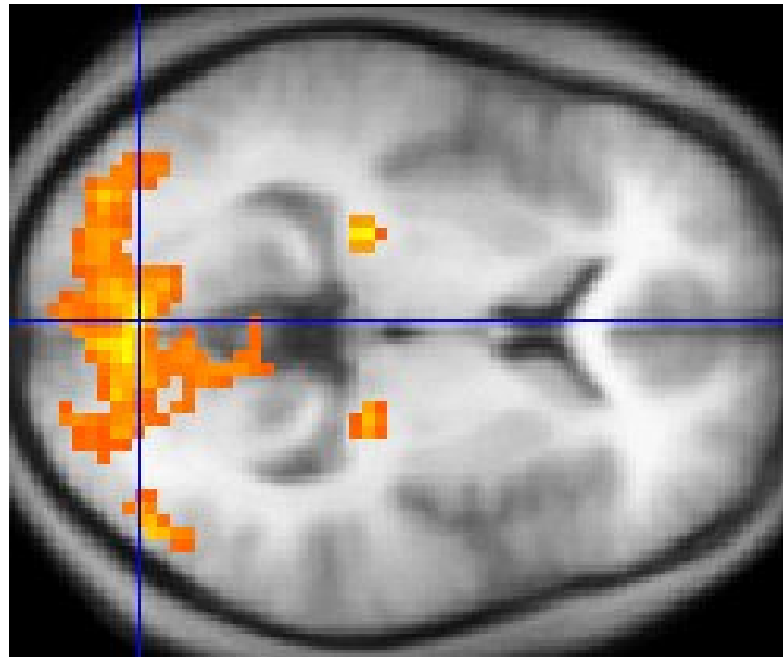


*From Andrew Kucher*



# Functional MRI: Brain Activity

- T2\* imaging: cerebral blood flow, cerebral blood volume and blood oxygenation
- Blood-oxygen-level dependent (BOLD) effect: increased neural activity causes an increased demand for oxygen, increasing the amount of oxygenated hemoglobin relative to deoxygenated hemoglobin.



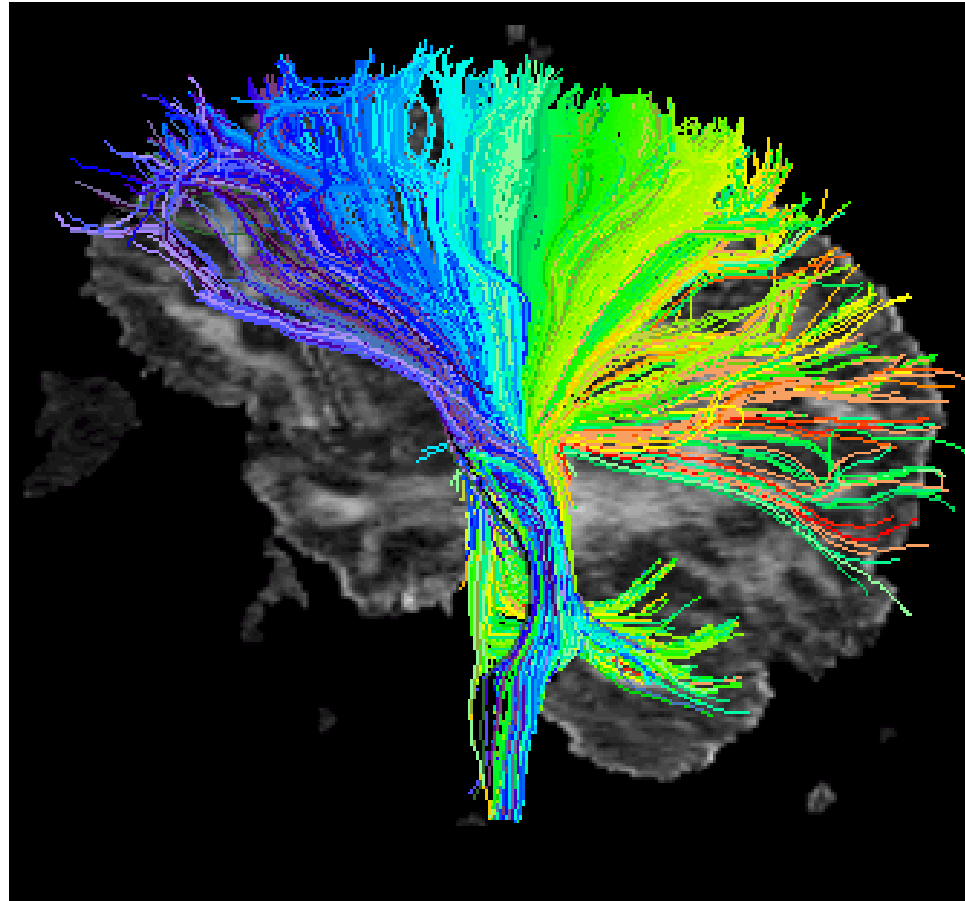
*From Washington Irving*



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# Diffusion Tensor Imaging (DTI): Brain Connectivity

- The fractional anisotropy shows fiber directions: tractography.



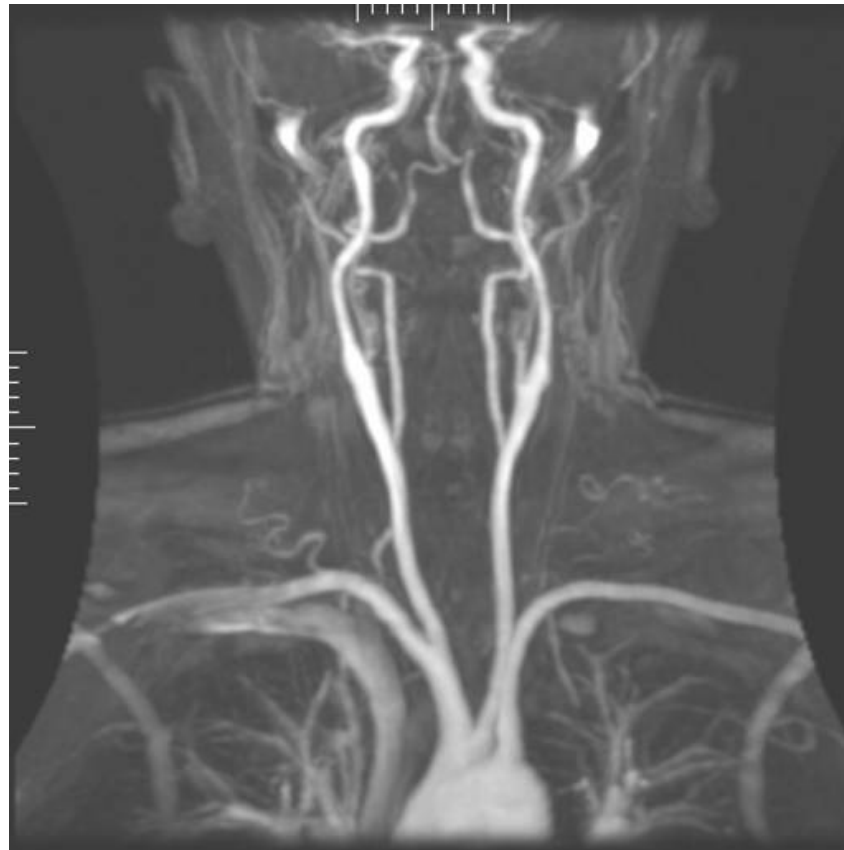
*From Mariana Lazar*



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# Magnetic Resonance Angiography (MRA)

- Image of the arteries in order to evaluate them for stenosis (abnormal narrowing) or aneurysms (vessel wall dilatations)



*From Ofir Glazer*

