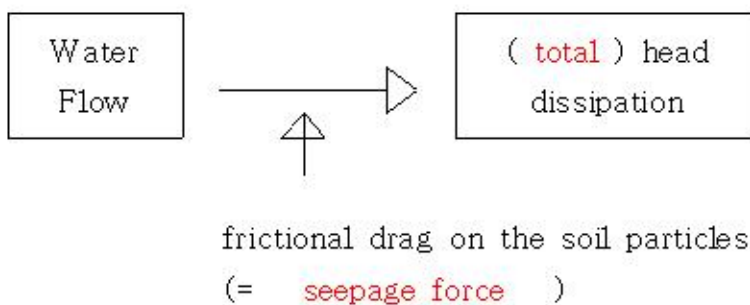


• What to be learned :

- ① Seepage force
- ② Quick condition
- ③ Frost heave

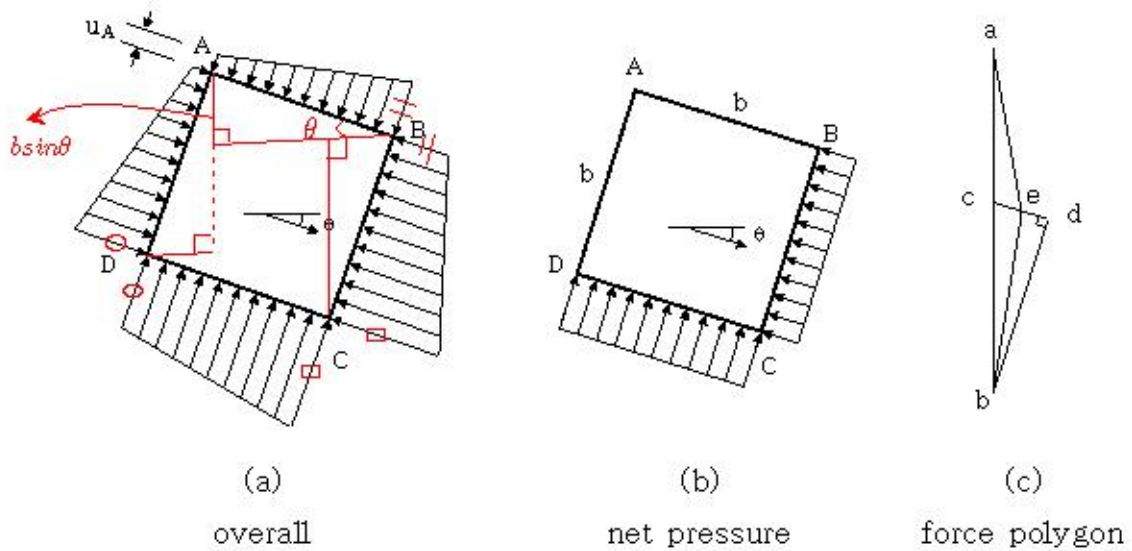
1. Seepage Force

○ Def. : The force corresponding to the energy transfer taking place from water to solid particles (due to **viscous friction**) during the water flow thru the pores of soil.



- Resultant body force (= **gravitational force + seepage force**)
↓
governs the effective normal force

2. Forces Under Seepage Conditions



- \overline{AD} & \overline{BC} : Equipotential line
- \overline{AB} & \overline{DC} : Flow line

○ $\overline{AB} = \overline{BC} = \overline{AD} = \overline{DC} = b$

○ the head drop between \overline{AD} & $\overline{BC} = \Delta h$

○ pore water pressures at pt. A, B, C, & D = u_A, u_B, u_C, u_D

between pts. A&B



Thus,

$$u_B = u_A + v_w (b \sin \theta - \Delta h) \quad \underbrace{\Delta h_e}_{\text{between pts B\&C}}$$

$$u_C = u_A + v_w (b \sin \theta - \Delta h + b \cos \theta)$$

$$u_D = u_A + v_w \underbrace{(b \cos \theta)}_{\Delta h_e \text{ between pts A\&D}}$$

and,

$$u_B - u_A = u_C - u_D = \gamma_w (b \sin \theta - \Delta h)$$

$$u_D - u_A = u_C - u_B = \gamma_w b \cos \theta$$

In terms of boundary water force

$$\begin{aligned} \text{on } \overline{BC} : \quad & \gamma_w (b \sin \theta - \Delta h) \cdot b \\ & = \gamma_w b^2 \sin \theta - \Delta h \gamma_w b \end{aligned}$$

$$\text{on } \overline{CD} : \quad \gamma_w b \cos \theta \cdot b$$

If there is no seepage, ($\Delta h = 0$)

$$\text{on } \overline{BC} : \quad \gamma_w b^2 \sin \theta$$

$$\text{on } \overline{CD} : \quad \gamma_w b^2 \cos \theta$$

The resultant
= $\gamma_w b^2$

\therefore ($\Delta h \gamma_w b$) is the only difference between the static & seepage cases, and is called the seepage force(J), acting in the direction of (flow)

Let the average hydraulic gradient across the element be $i = \left(\frac{\Delta h}{b}\right)$

then,

$$J = \Delta h \gamma_w b = \frac{\Delta h}{b} \gamma_w b^2 = i \gamma_w b^2 = i \gamma_w V$$

the seepage pressure (j) (= seepage force per unit volume),

$$j = i \gamma_w$$

* note that the seepage pressure depends only on

(the value of hydraulic gradient, i)

○ (Refer to Fig. (c) : force polygon)

i) Total wt. of element : $\gamma_{sat} \cdot b^2 = \overrightarrow{ab}$

ii) Boundary water force on CD (Seepage & Static case) :

$$\gamma_w \cdot b^2 \cos \theta = \overrightarrow{bd}$$

iii) Boundary water force on BC :

- Seepage case

$$\gamma_w b^2 \sin \theta - \Delta h \gamma_w b = \overrightarrow{de}$$

- Static case

$$\gamma_w b^2 \sin \theta = \overrightarrow{dc}$$

iv) Resultant boundary water force

- Seepage case : \overrightarrow{be}

- Static case : \overrightarrow{bc}

v) Seepage force :

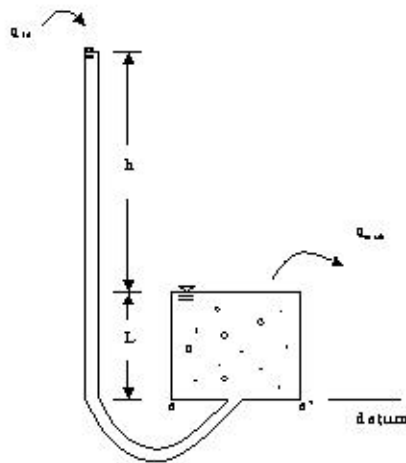
$$\Delta h \gamma_w b = \overrightarrow{ce}$$

vi) Resultant body force

- Seepage case : $\overrightarrow{ae} = \overrightarrow{ab} + \overrightarrow{be} = \overrightarrow{ac} + \overrightarrow{ce}$

- Static case : $\overrightarrow{ac} = \gamma_b \cdot b^2$

3. Quick condition (quick sand, boiling, piping)



- total upward water force at $\overrightarrow{aa'}$
 $= (h + L) \gamma_w A$ ①

- wt. of saturated soil above $\overrightarrow{aa'}$
 $= \gamma_t LA = \frac{G+e}{1+e} \gamma_w LA$ ②

- quick condition occurs if ① \geq ②, i.e.,

$$\left((h+L) \gamma_w A \geq \frac{G+e}{1+e} \gamma_w LA \right)$$

$$\downarrow$$

$$\frac{h}{L} (=i) \geq \frac{G-1}{1+e}$$

* In terms of seepage pressure :

$$\left(J = i \gamma_w V \geq \gamma_b V \rightarrow i \geq \frac{\gamma_b}{\gamma_w} (= \frac{G-1}{1+e}) \right)$$

4. Frost Heave

○ Def. : the rise of the ground surface due to frost action

○ Freezing of water

- 9% of volume increase for water
- (2.5 ~ 5 %) for soil

○ much greater volume increase possible

- soils having a high percentage of silt-size particles

(∴ have a network of small pores & permeability not too low)

- well-graded soil w/ more than 3% of fines(<0.02 mm)

- Poorly-graded soil w/ more than 10%

○ mechanism :

Ice lenses created in large pores → suction of water by capillary →
Excessive water in the upper soil which is frozen.

○ Remedies :

- i) Replacement of frost susceptible soils

- ii) Lowering the freezing pt. of pore water
 - the addition of salt regularly

- iii) Restricting the water supply
 - install a cut-off blanket in the subsoil

- iv) Use of chemical additives
 - make the subsoils more/or less permeable
(melt or restricted in size)

- v) Adding a surcharge load
 - make the water table be located more than
6' below the G.S.
 - counteracts the heaving pressure

- vi) Use of thermal blanket
 - e.g., foam plastic