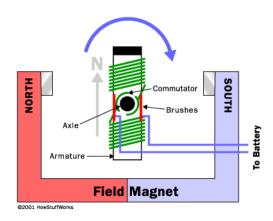
# **Electrical Systems III**

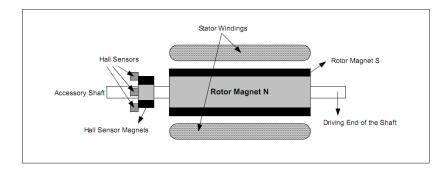


### **DC Motors**

### **Brushed DC Motor**



### **Brushless DC (BLDC) Motor**



#### Two wire control

Low cost of construction/ Simple and inexpensive control No controller is required for fixed speeds

At higher speeds, brush friction increases, thus reducing useful torque

Poor heat dissipation due to internal rotor contsruction Higher rotor inertia which limits the dynamic characteristics Brush Arcing will generate noise causing EMI

High efficiency, no voltage drop across brushes High output power/frame size.

Because BLDC has the windings on the stator, which is connected to the case, the heat disipation is better

Higher speed range – no mechanical limitation imposed by brushes/commutator

Higher cost of construction

Electric Controller is required to keep the motor running

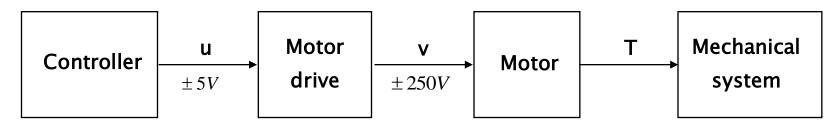
### **Other Motors:**



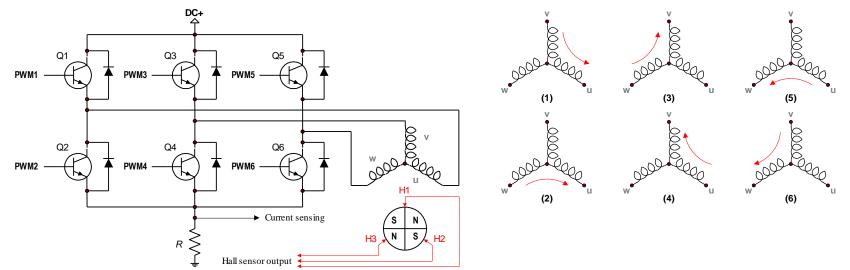
**Seoul National Univ.** School of Mechanical and Aerospace Engineering

# **Constitution of DC Servomotor System**

Motor drive system :



3 phase BLDC motor driver :





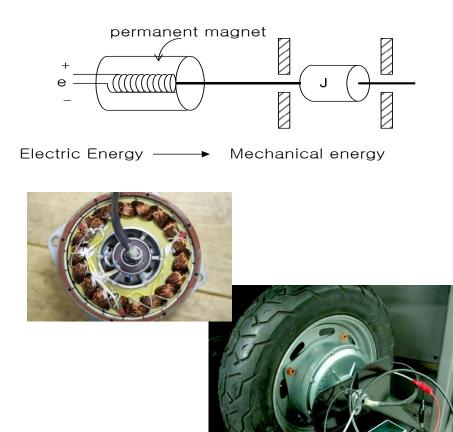
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# **Constitution of DC Servomotor System**

ex)

Elevator structure :

#### DC servo motor :



Motor Controller Guide rail Elevator cage Tail code Counter weight Shock absorber

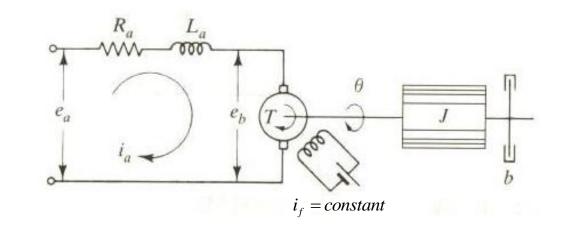


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## **Armature Control of DC Servomotors**

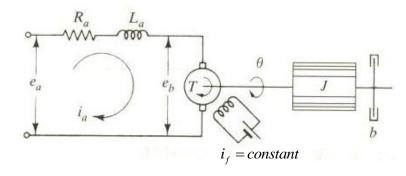
#### Variables :

- $R_a$ : armature resistance,  $\Omega$
- $L_a$ : armature inductance, H
- $i_a$ : armature current, A
- $i_f$ : field current, A
- $e_a$ : applied armature voltage, V
- $e_b$ : back emf, V
- $\theta\;$  : angular displacement of the motor shaft,  $\;$  rad
- T: torque developed by the motor, N-m
- J: equivalent moment of inertia of the motor and load referred to the motor shaft, kg-m<sup>2</sup>
- *b* : equivalent viscous- friction coefficient of the motor and load referred to the motor shaft, N-m/rad/s





### **Armature Control of DC Servomotors**



The torque of motor :

*K*:*motor*-*torque* constant

For a constant flux, the induced voltage :

 $K_b$ : back emf constant

Armature circuit D.E :

Inertia and friction :



### **Armature Control of DC Servomotors**

Laplace transforms of equations :

$$e_{b} = K_{b} \frac{d\theta}{dt} \qquad \qquad K_{b} S \Theta(s) = E_{b}(s)$$

$$L_{a} \frac{di_{a}}{dt} + R_{a} i_{a} + e_{b} = e_{a} \qquad \longrightarrow \qquad (L_{a} s + R_{a}) I_{a}(s) + E_{b}(s) = E_{a}(s)$$

$$J \frac{d^{2}\theta}{dt^{2}} + b \frac{d\theta}{dt} = T = K i_{a} \qquad (Js^{2} + bs) \Theta(s) = T(s) = K I_{a}(s)$$

$$T.F = \frac{\Theta(s)}{E_a(s)} = \frac{K}{s(R_a J s + R_a b + K K_b)} = \frac{\frac{R_a J}{R_a J}}{s\left(s + \frac{R_a b + K K_b}{R_a J}\right)}$$
$$= \frac{K_m}{s(T_m s + 1)}$$

$$K_m = K / (R_a b + K K_b) = motor gain constant$$
  
 $T_m = R_a J / (R_a b + K K_b) = motor time constant$ 

K





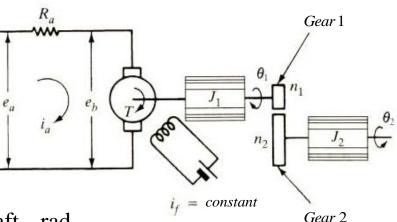
# **Example of a DC Servomotor System**

#### ex) servo-motor system

- $R_a$ : armature resistance,  $\Omega$
- $i_a$ : armature current, A
- $i_f$ : field current, A
- $e_a$ : applied armature voltage, V
- $e_h$ : back emf, V
- $\theta_1$ : angular displacement of the motor shaft, rad
- $\theta_2$ : angular displacement of the load shaft, rad
- T: torque developed by the motor, N-m
- $J_1$ : equivalent moment of inertia of the motor, kg-m<sup>2</sup>
- $J_2$ : equivalent moment of inertia of the load, kg-m<sup>2</sup>

The torque of motor :  $T = Ki_a$ 

For a constant flux, the induced voltage :  $e_b = K_b \frac{d\theta}{dt}$   $K_b$  : back emf constant





### **Example of a DC Servomotor System**

Armature circuit D.E :  $R_a i_a + e_b = e_a$  Inertia :

Laplace transforms of these equations :

 $K_{b}s\Theta(s) = E_{b}(s), \quad (L_{a}s + R_{a})I_{a}(s) + E_{b}(s) = E_{a}(s), \quad (Js^{2} + bs)\Theta(s) = T(s) = KI_{a}(s)$ 

$$T.F = \frac{\Theta(s)}{E_a(s)} = \frac{K}{s(R_a J s + R_a b + K K_b)} = \frac{\frac{K}{R_a J}}{s\left(s + \frac{R_a b + K K_b}{R_a J}\right)}$$
$$= \frac{K_m}{s(T_m s + 1)}$$

