

2009 fall

Advanced Physical Metallurgy
“Phase Equilibria in Materials”

09.22.2009

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Office hours: by an appointment

Contents for previous class

- **Binary System** mixture/ solution / compound
- **Gibbs Free Energy in Binary System**

$$G_1 = X_A G_A + X_B G_B \quad J/mol$$

$$G_2 = G_1 + \Delta G_{mix} \quad J/mol$$

Ideal solution ($\Delta H_{mix} = 0$)

$$G = X_A G_A + X_B G_B + RT(X_A \ln X_A + X_B \ln X_B)$$

Regular solution

$$\Delta H_{mix} = P_{AB} \epsilon$$

$$\Delta G^{mix} = RT(X_A \ln X_A + X_B \ln X_B)$$

where $\epsilon = \epsilon_{AB} - \frac{1}{2}(\epsilon_{AA} + \epsilon_{BB})$

$$G = X_A G_A + X_B G_B + \Omega X_A X_B + RT(X_A \ln X_A + X_B \ln X_B)$$

- Chemical potential and Activity

$$\mu_A = \left(\frac{\partial G'}{\partial n_A} \right)_{T, P, n_B}$$

- $\mu_A = G_A + RT \ln a_A$ $\ln \left(\frac{a_A}{X_A} \right) = \frac{\Omega}{RT} (1 - X_A)^2$
- $\frac{a_A}{X_A} = \gamma_A = \text{activity coefficient}$

Contents for today's class

- **Binary System** mixture/ solution / compound

Ideal solution ($\Delta H_{\text{mix}} = 0$)

Random distribution

Regular solution

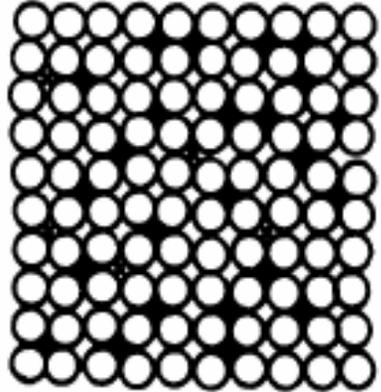
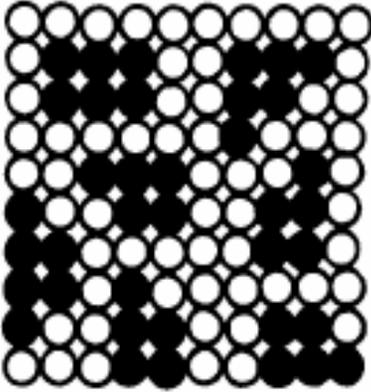
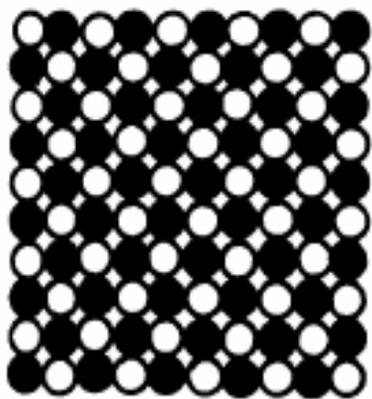
$$\Delta H_{\text{mix}} = P_{AB}\epsilon$$

where $\epsilon = \epsilon_{AB} - \frac{1}{2}(\epsilon_{AA} + \epsilon_{BB})$ $\epsilon \approx 0$

$\Delta H_{\text{mix}} > 0$ or $\Delta H_{\text{mix}} < 0$

Real solution

Ordered structure



(a) $\epsilon < 0, \Delta H_{\text{mix}} < 0$

(b) $\epsilon > 0, \Delta H_{\text{mix}} > 0$

(c) when the size difference is large
strain effect

Ordered alloys

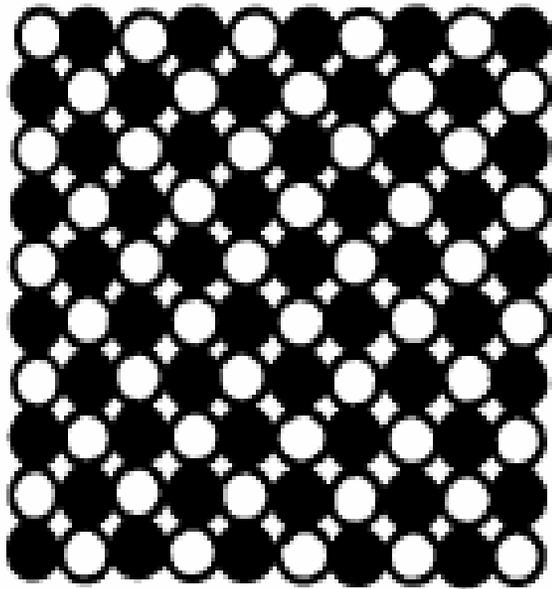
Clustering

Interstitial solution

Real solution: $\Delta G_{mix} = \Delta H_{mix} - T\Delta S_{mix}$

Ideal or Regular solution : over simplification of reality

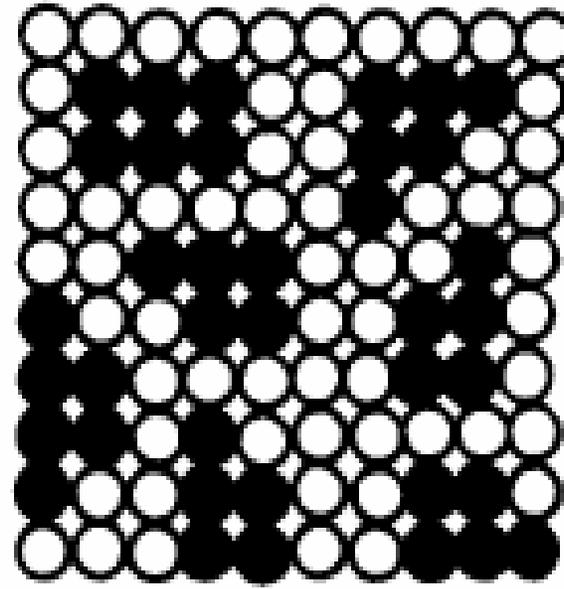
Entropy $S = k \ln w$ + $\Delta H_{mix} = \Omega X_A X_B$ where $\Omega = N_a z \epsilon$ $\epsilon \approx 0$



Ordered alloys

$\epsilon < 0, \Delta H_{mix} < 0$

$P_{AB} \uparrow \longrightarrow \text{Internal } E \downarrow$



elastic strain

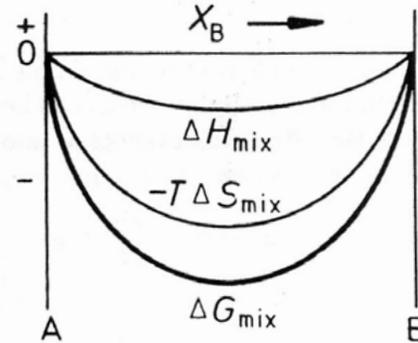
Clustering

$\epsilon > 0, \Delta H_{mix} > 0$

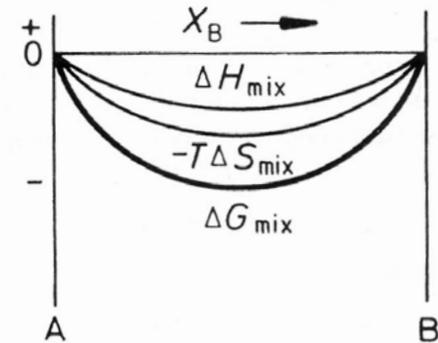
$P_{AA'}, P_{BB} \uparrow$

* The degree of **ordering or clustering** will **decrease** as **temp. increases** due to the increasing importance of **entropy**.

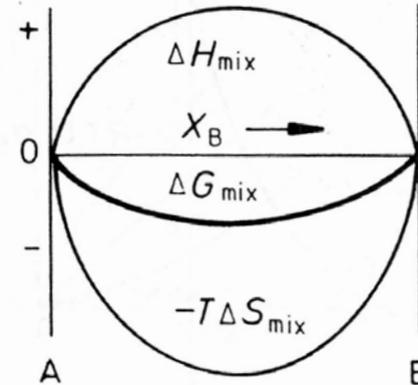
$$\Delta G_{mix} = \Delta H_{mix} - T\Delta S_{mix}$$



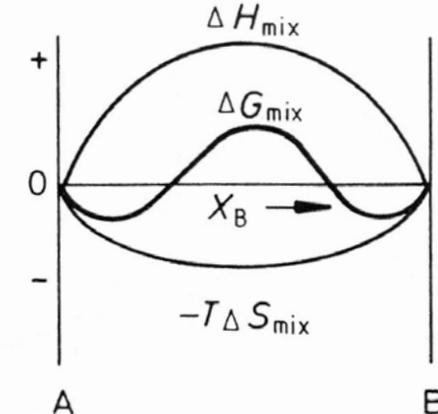
(a) $\Omega < 0$, high T



(b) $\Omega < 0$, low T



(c) $\Omega > 0$, high T

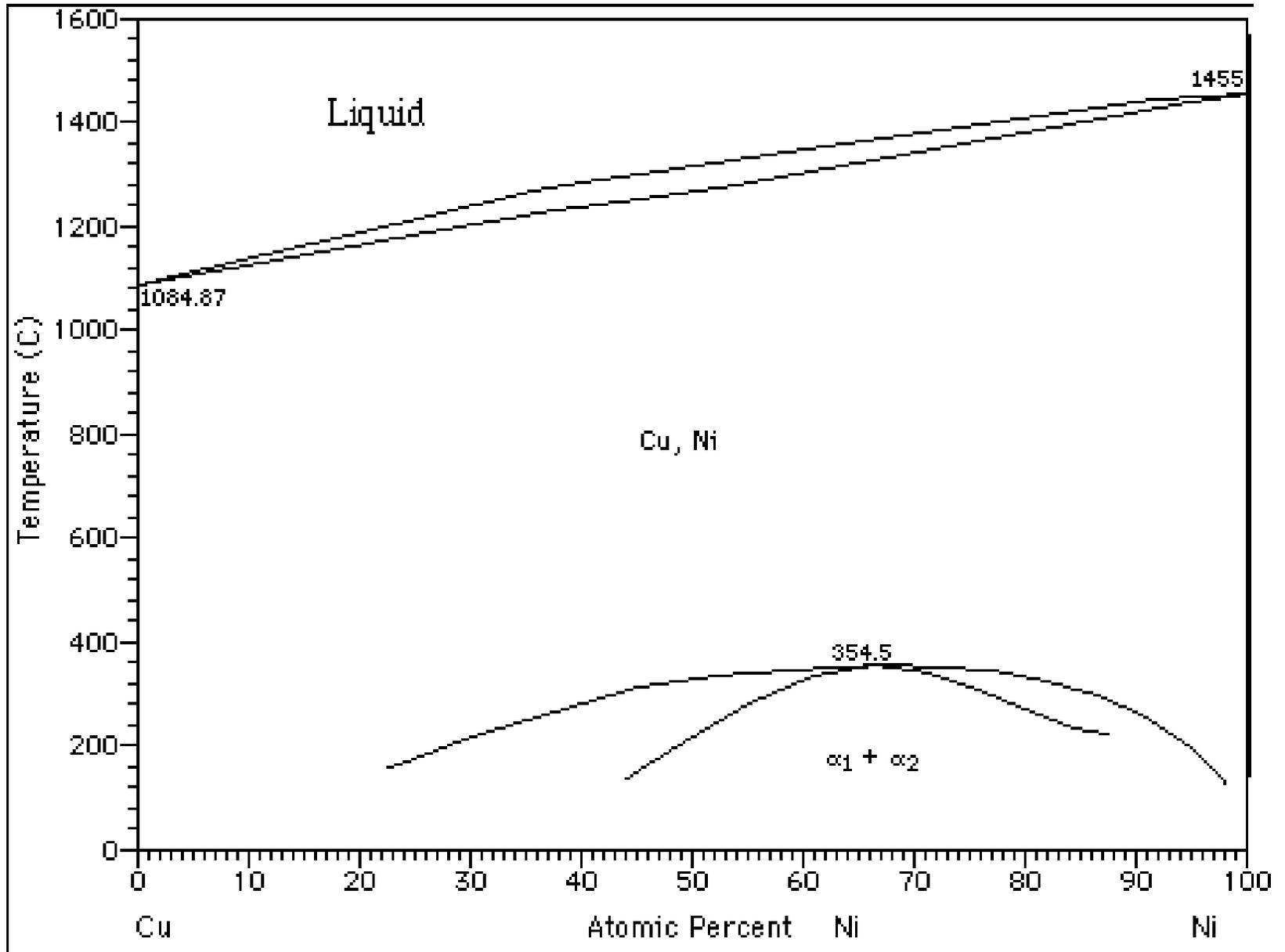


(d), $\Omega > 0$ low T

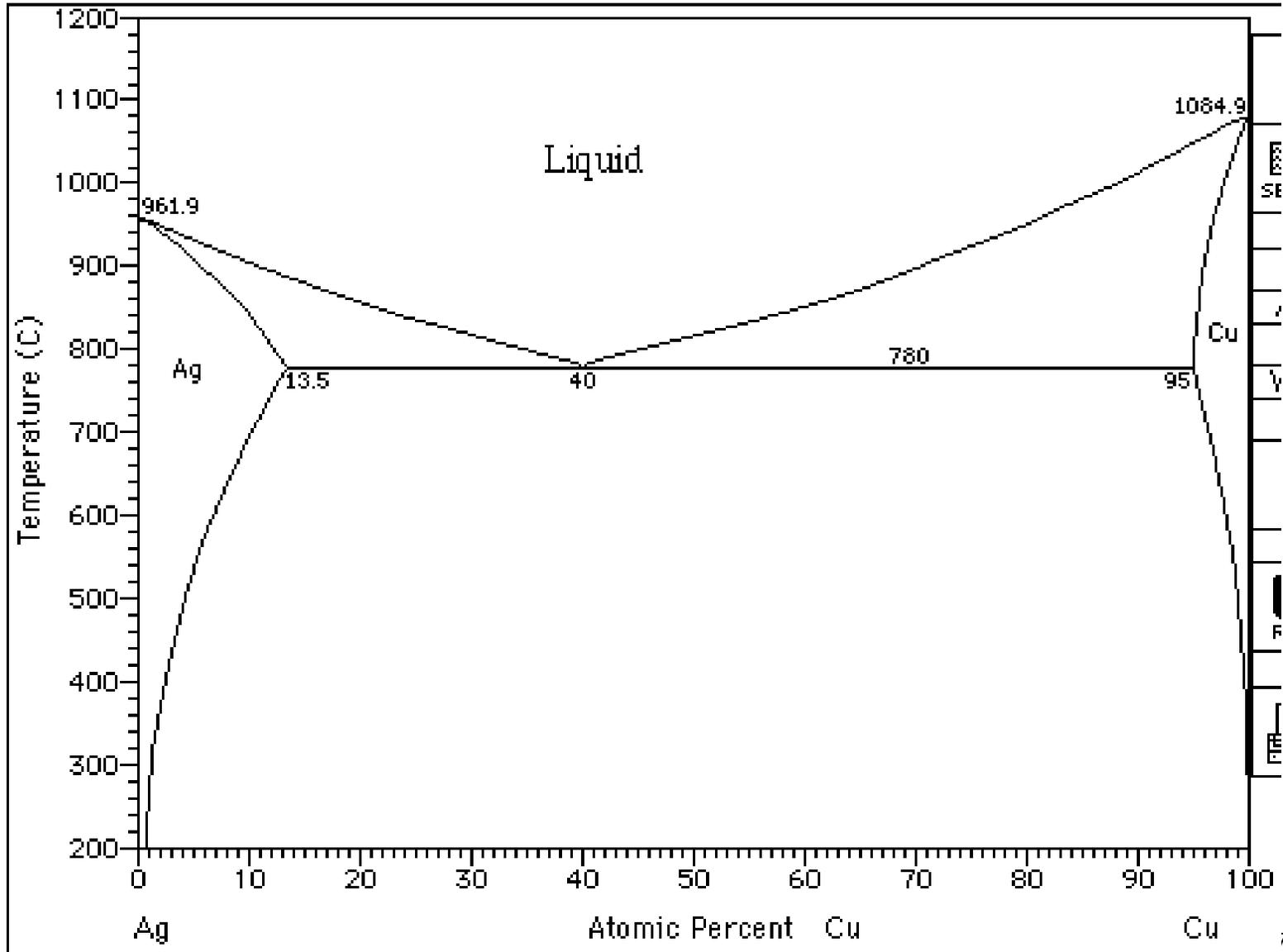
* In systems where there is a size difference between the atom,

$$\Delta E = \Delta H_{mix} + \text{elastic strain}$$

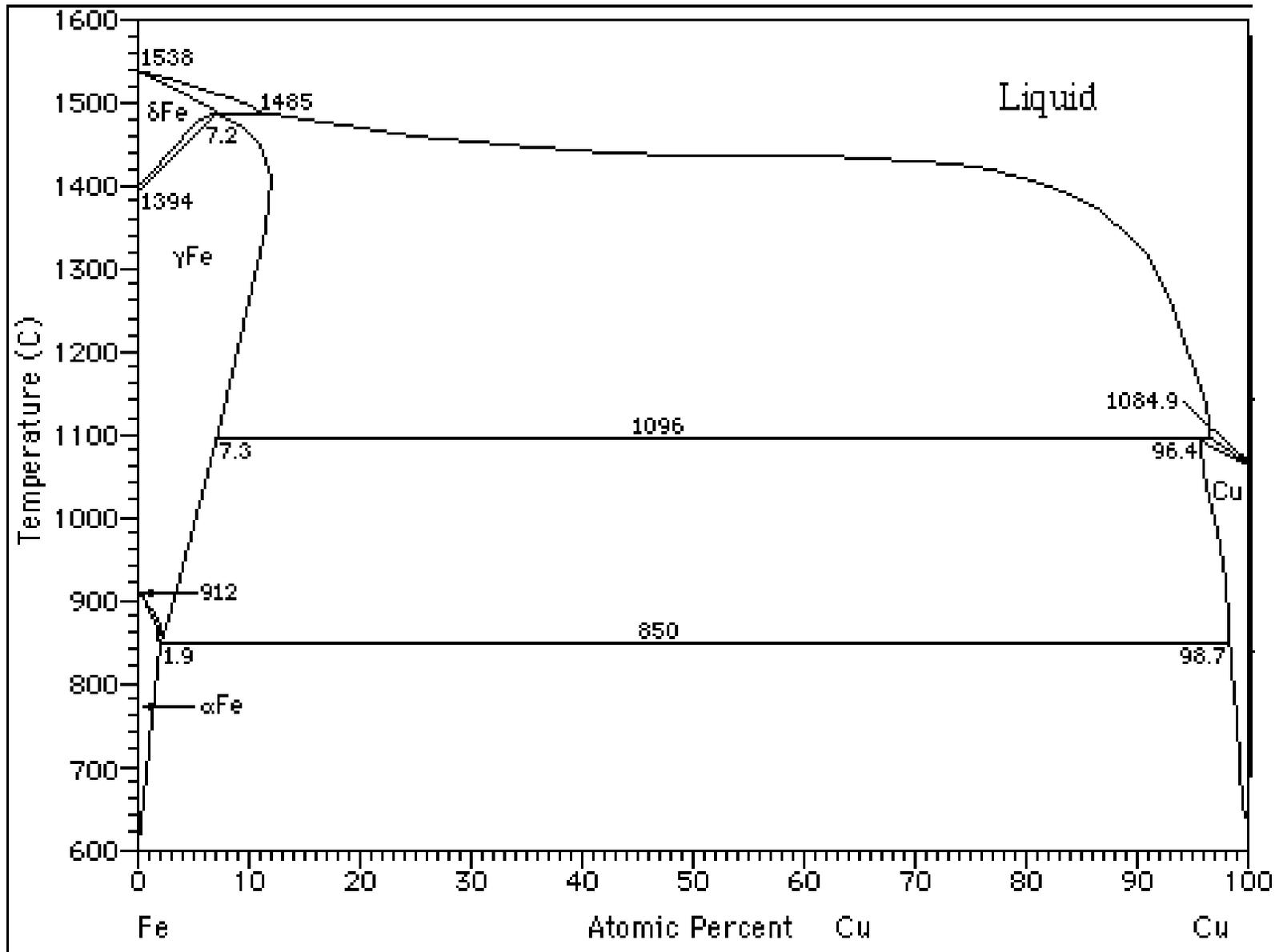
$$\epsilon > 0, \Delta H_{\text{mix}} > 0 / \Delta H_{\text{mix}} \sim +26 \text{ kJ/mol}$$



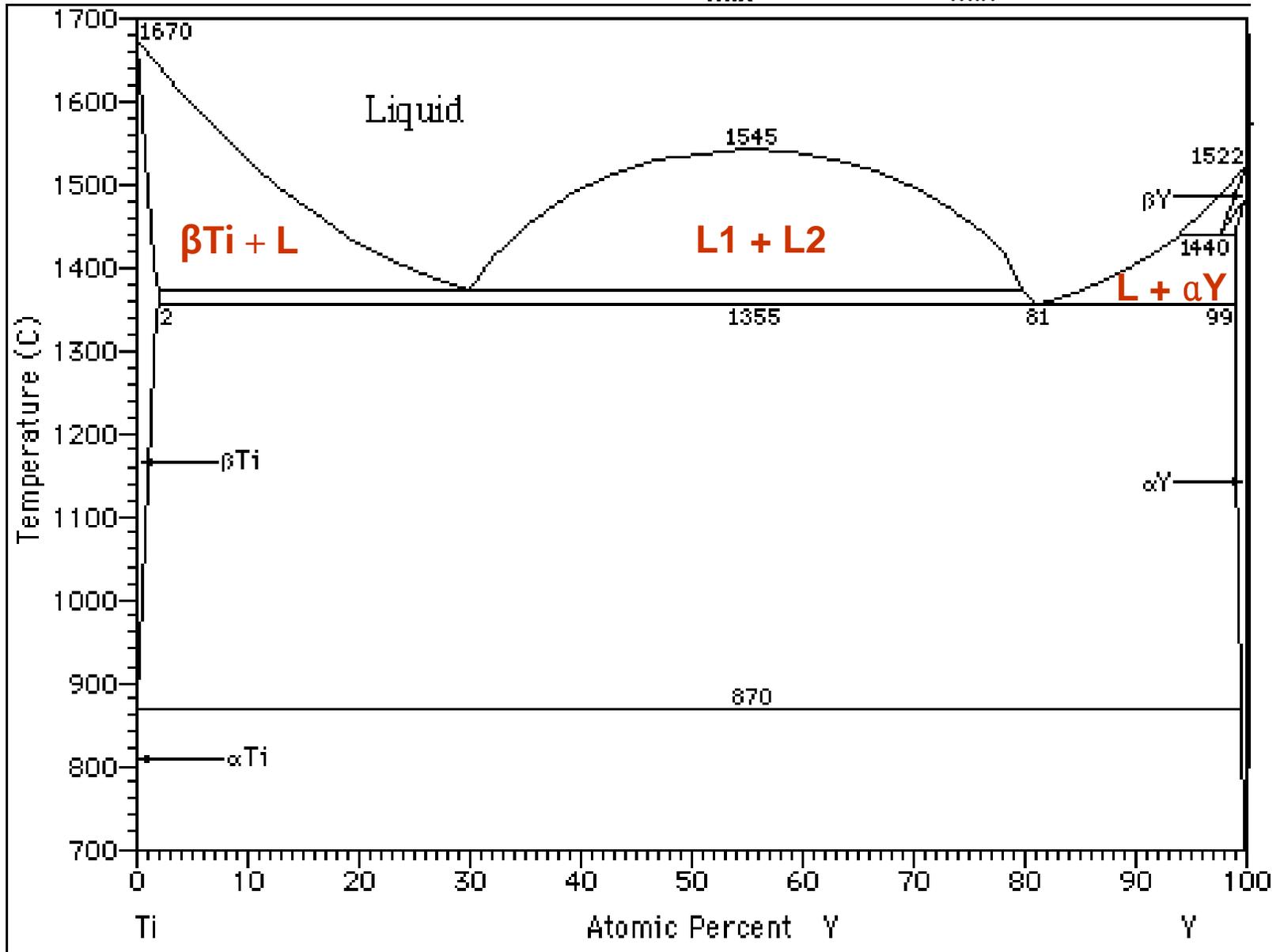
$\epsilon > 0$, $\Delta H_{\text{mix}} > 0$ / $\Delta H_{\text{mix}} \sim +5 \text{ kJ/mol}$



$\epsilon \gg 0$, $\Delta H_{\text{mix}} \gg 0$ / $\Delta H_{\text{mix}} \sim +60$ kJ/mol



$\epsilon \gg 0, \Delta H_{\text{mix}} \gg 0 / \Delta H_{\text{mix}} \sim +58 \text{ kJ/mol}$

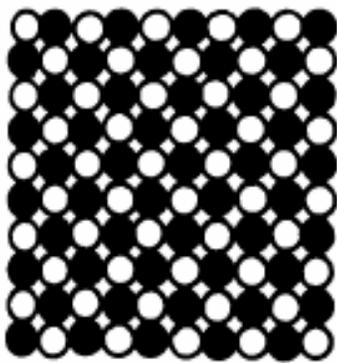


Ordered phase $\varepsilon < 0, \Delta H_{\text{mix}} < 0$

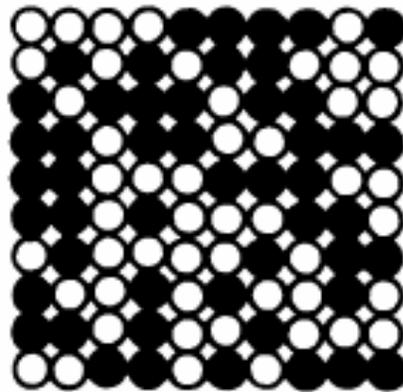
- $\Omega < 0 \Rightarrow$ contain short-range order (SRO) = s

$$\Delta\Omega = N_a z \varepsilon$$

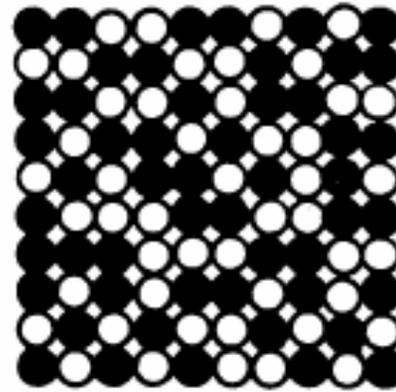
$$s = \frac{P_{AB} - P_{AB}(\text{random})}{P_{AB}(\text{max}) - P_{AB}(\text{random})}$$



$P_{AB}(\text{max})$

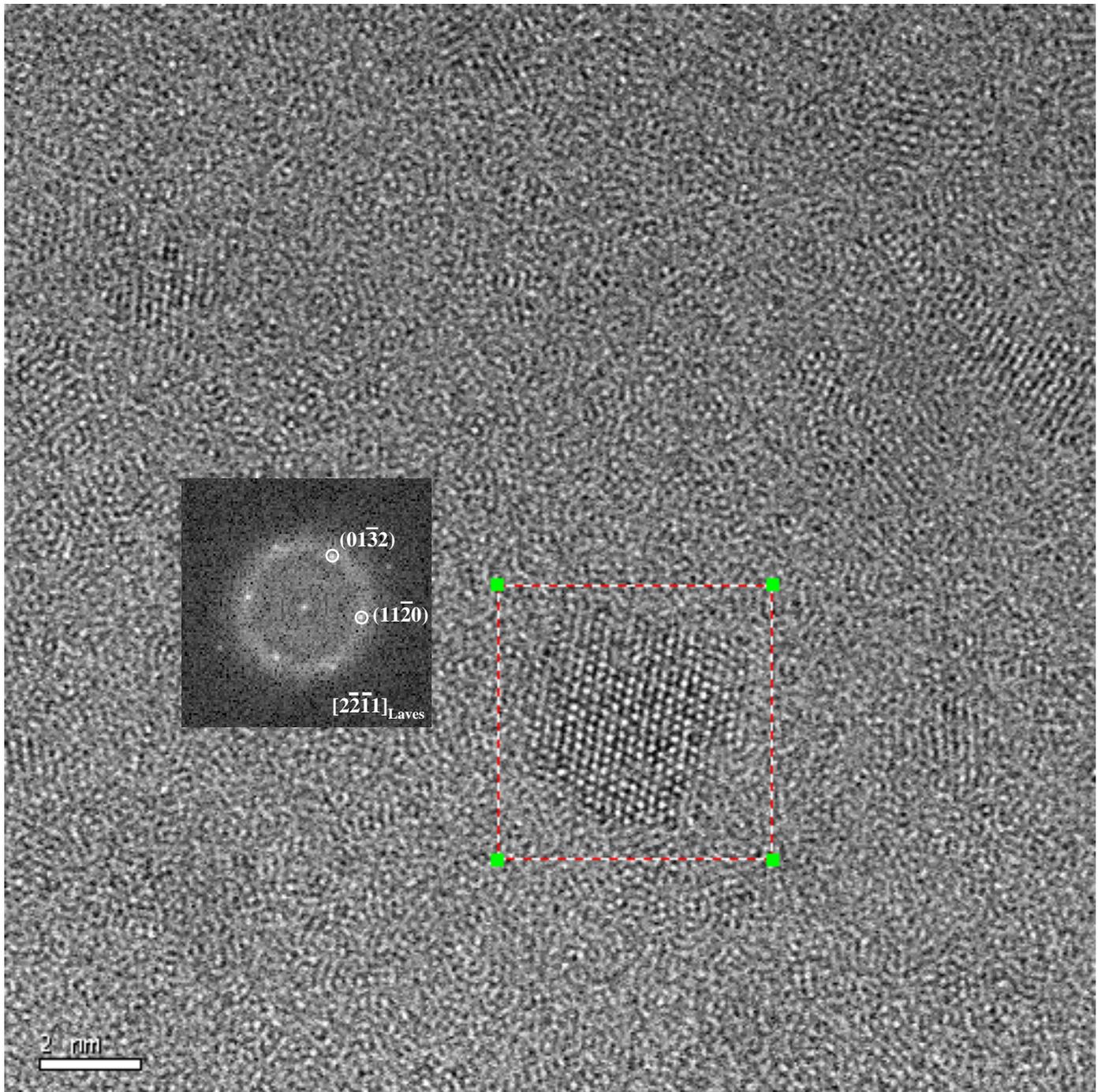


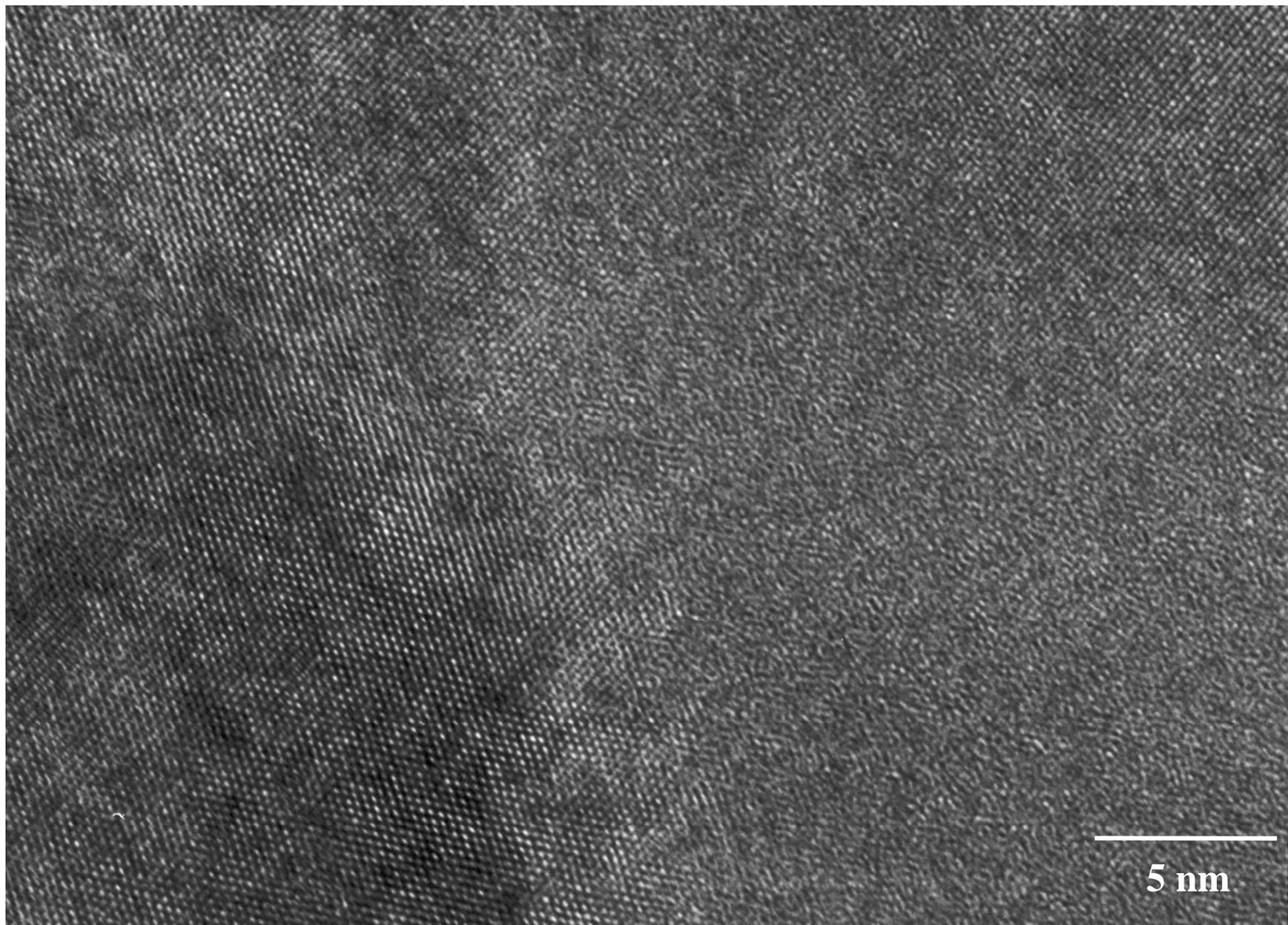
(a) $P_{AB}(\text{random})$



(b) P_{AB} with SRO

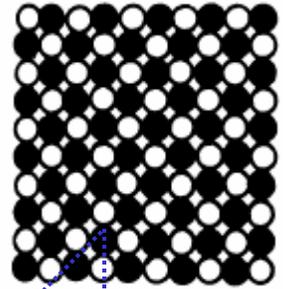
Fig. 1.19 (a) Random A-B solution with a total of 100 atoms and $X_A = X_B = 0.5$, $P_{AB} \sim 100$, $S = 0$. (b) Same alloy with short-range order $P_{AB} = 132$, $P_{AB(\text{max})} \sim 200$, $S = (132 - 100) / (200 - 100) = 0.32$



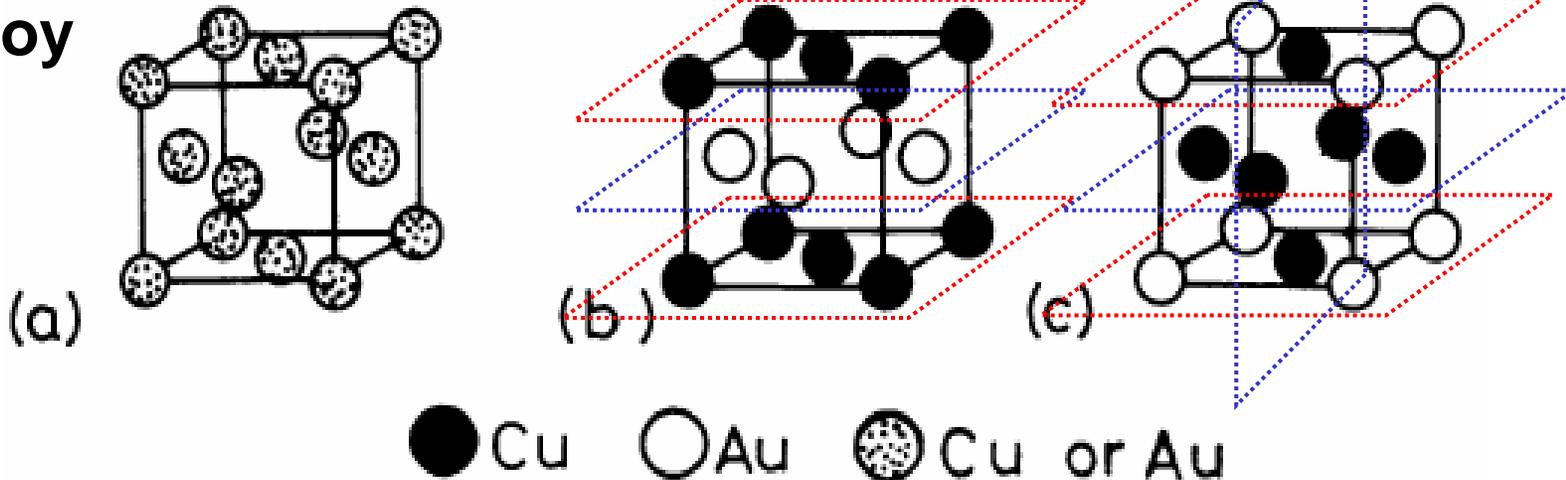


Ordered phase $\varepsilon < 0, \Delta H_{\text{mix}} < 0$

- * In solutions with compositions that are close to a simple **ratio of A:B atoms** another type of order can be found.
- * This is known as **long-range order (LRO)** CuAu, Cu₃Au and many other intermetallics show LRO.
- * A **superlattice** forms in materials with LRO



Cu–Au alloy



High temp.

Disordered Structure

Low temp.

CuAu superlattice

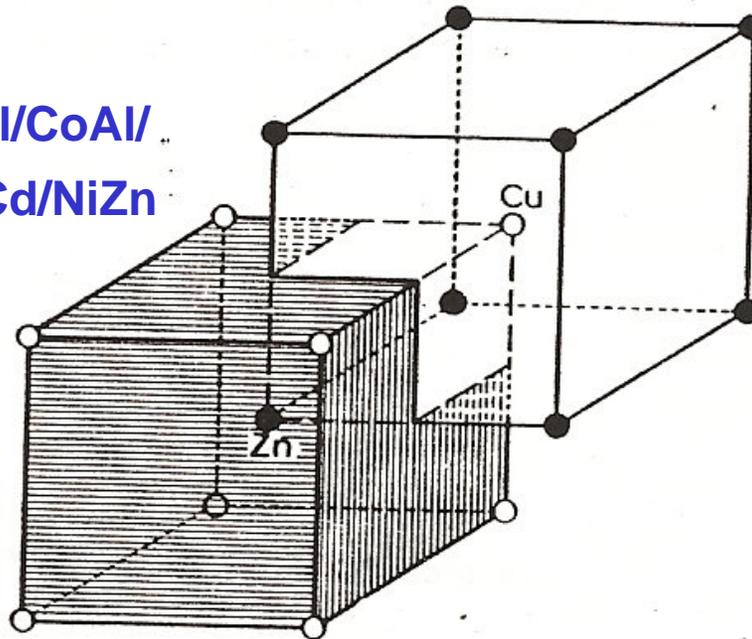
Cu₃Au superlattice

Superlattice formation: order-disorder transformation

- $\epsilon < 0$, $\Delta H_{\text{mix}} < 0$
- **between dissimilar atoms** than between similar atoms
- **large electrochemical factor**: tendency for the solute atoms to avoid each other and to associate with the solvent atoms
- **Size factor just within the favorable limit**: lead to atomic rearrangement so as to relieve the lattice distortion imposed by the solute atoms

(a) $L2_0$:

CuZn/FeCo/NiAl/CoAl/
FeAl/AgMg/AuCd/NiZn

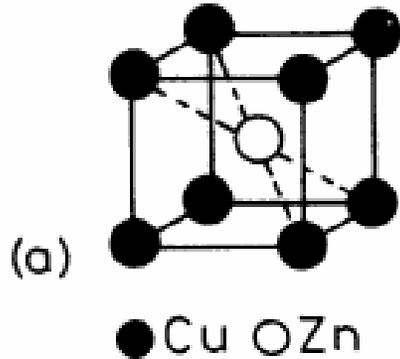


β brass superlattice viewed as two inter-penetrating cubic lattices

Five common ordered lattices

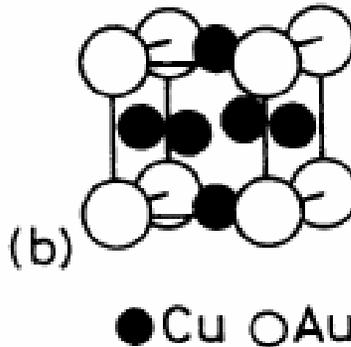
(a) $L2_0$:

CuZn/FeCo/NiAl/CoAl/
FeAl/AgMg/AuCd/NiZn



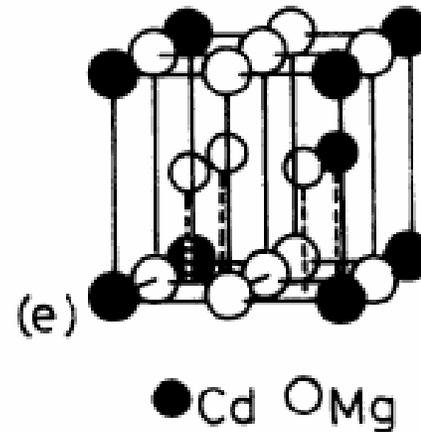
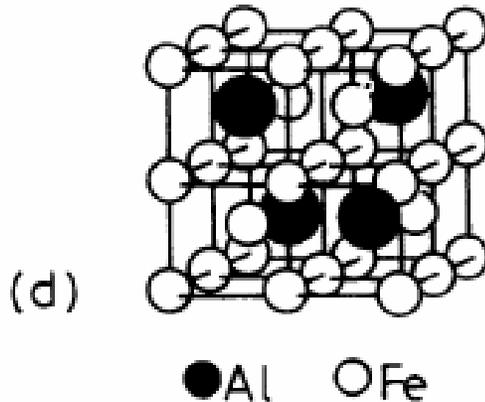
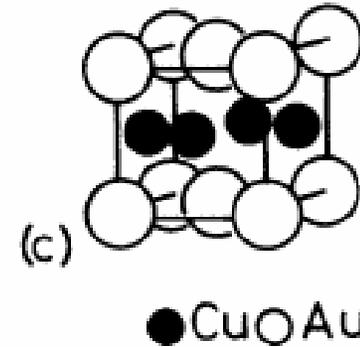
(b) $L1_2$:

Cu_3Au /Ni₃Mn/Ni₃Fe/Ni₃Al/
Pt₃Fe/Au₃Cd/Co₃V/TiZn₃



(c) $L1_0$:

CuAu/CoPt/FePt



(d) $D0_3$:

Fe_3Al /Cu₃Sb/Mg₃Li/ Fe_3Al /
 Fe_3Si / Fe_3Be /Cu₃Al

(e) $D0_{19}$:

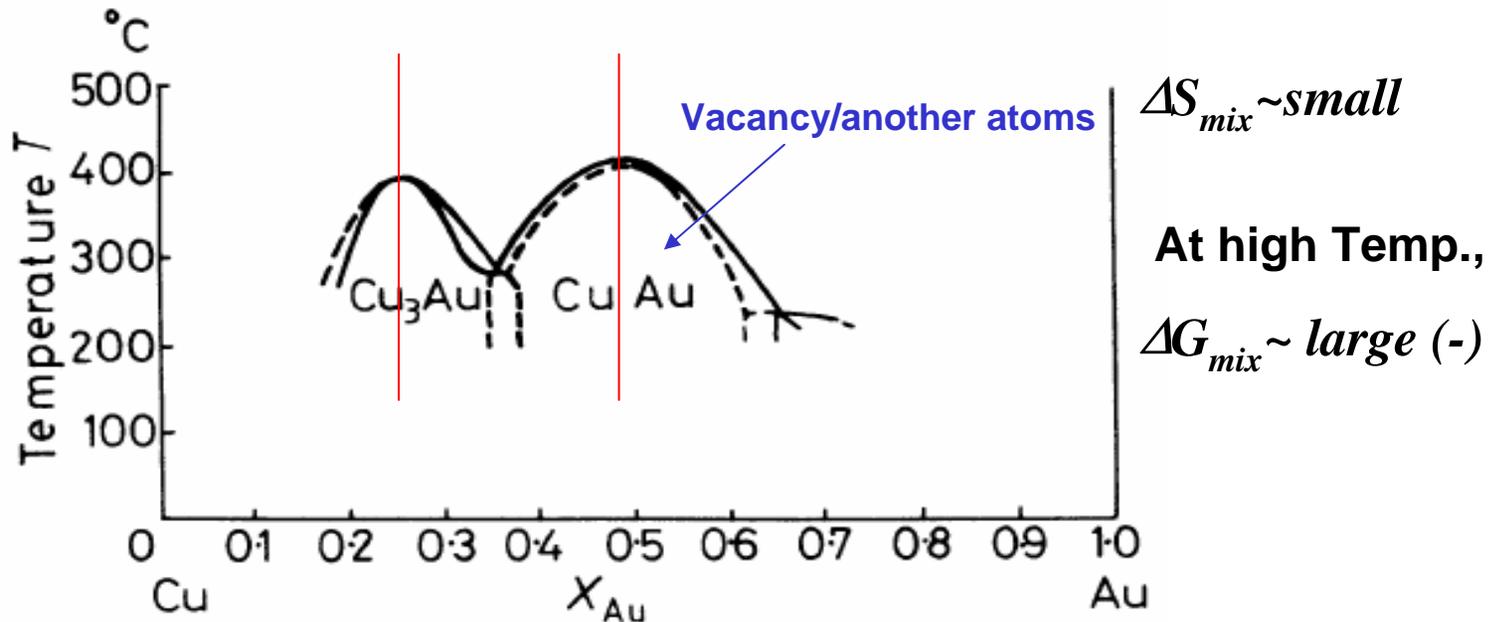
Mg₃Cd/Cd₃Mg/Ti₃Al/Ni₃Sn/Ag₃In/
Co₃Mo/Co₃W/ Fe_3Sn /Ni₃In/Ti₃Sn

$$\Delta G_{mix} = \Delta H_{mix} - T\Delta S_{mix}$$

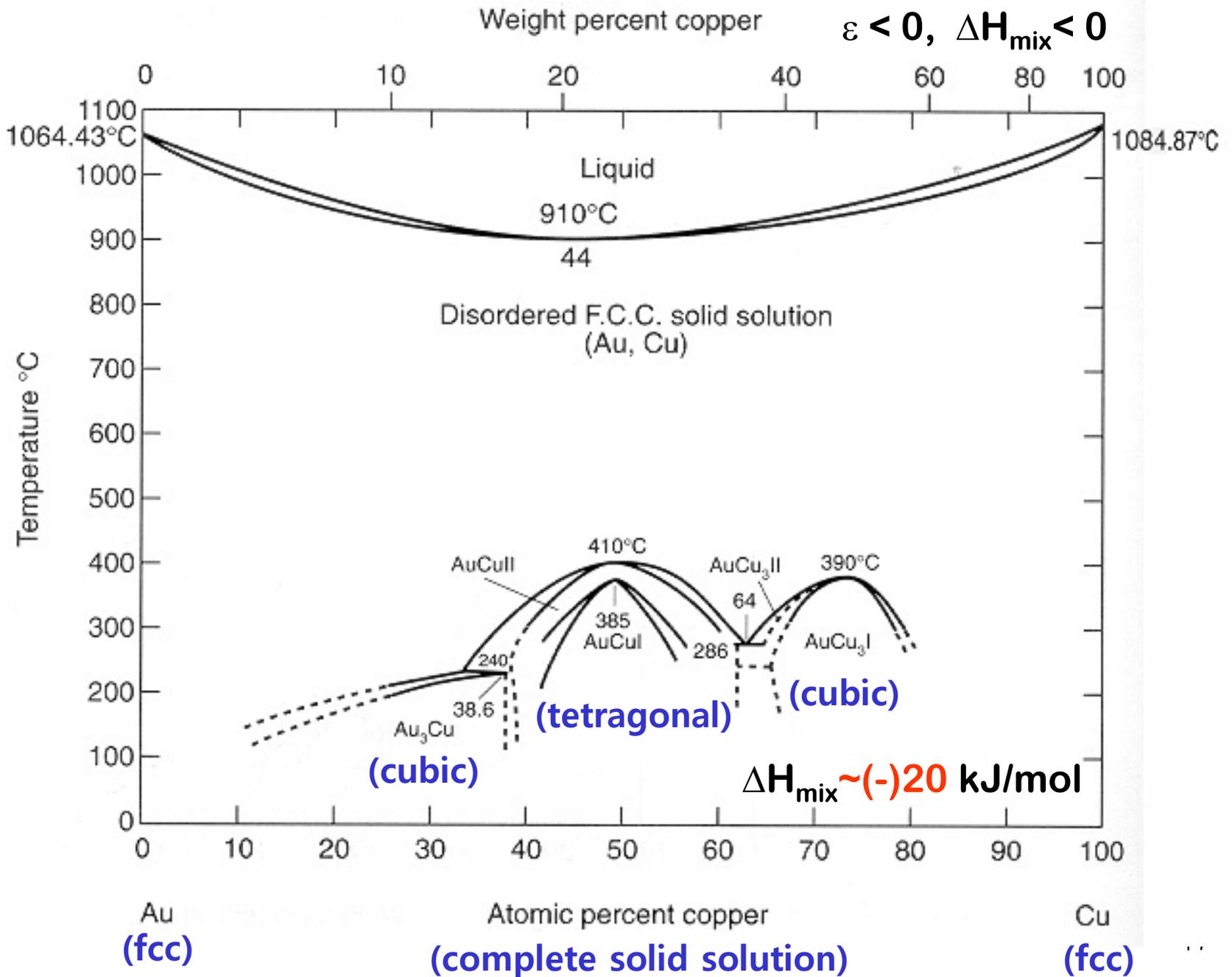
Ordered phase

$$\varepsilon < 0, \Delta H_{mix} < 0$$

Fig. 1.21. Part of the Cu-Au phase diagram showing the regions where the Cu_3Au and CuAu superlattices are stable.



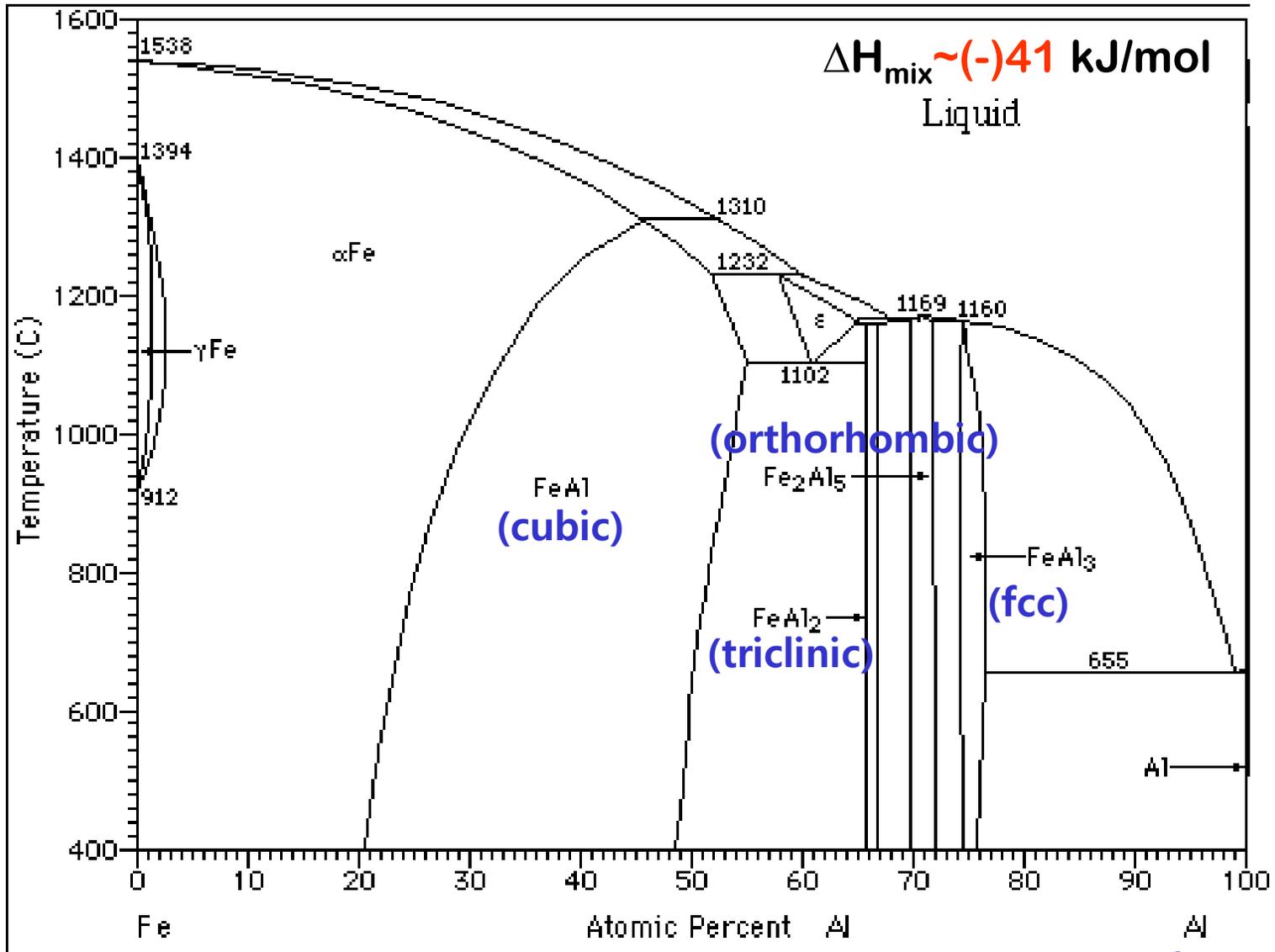
- The **entropy** of mixing of structure with LRO is **extremely small** and the **degree of order decrease** with **increasing temperature** until above some **critical temperature** there is no LRO at all.
- This temperature is a maximum when the composition is the ideal required for the superlattice.
- The critical temperature for loss of LRO increases with increasing Ω or ΔH_{mix} , and in many systems the ordered phase is stable up to the melting point.



$$\epsilon < 0, \Delta H_{\text{mix}} < 0$$

$$\Delta H_{\text{mix}} \sim (-)41 \text{ kJ/mol}$$

Liquid



(bcc)

(fcc)

Intermediate Phase

- * Often the configuration of atoms that has the **minimum free energy after mixing** **does not have the same crystal structure** as either of the pure components. In such cases the new structure is known as an **intermediate phase**.
- * **Intermediate phase** has crystal structure different from that of either element in pure state. For example, **CuZn (bcc)** has an ordered body centered structure, different from either **Cu (fcc)** or **Zn (hcp)**. This particular intermediate phase has some solubility range whereas other intermediate phases may have a very narrow solubility range for the solute element.

Ordered Alloys

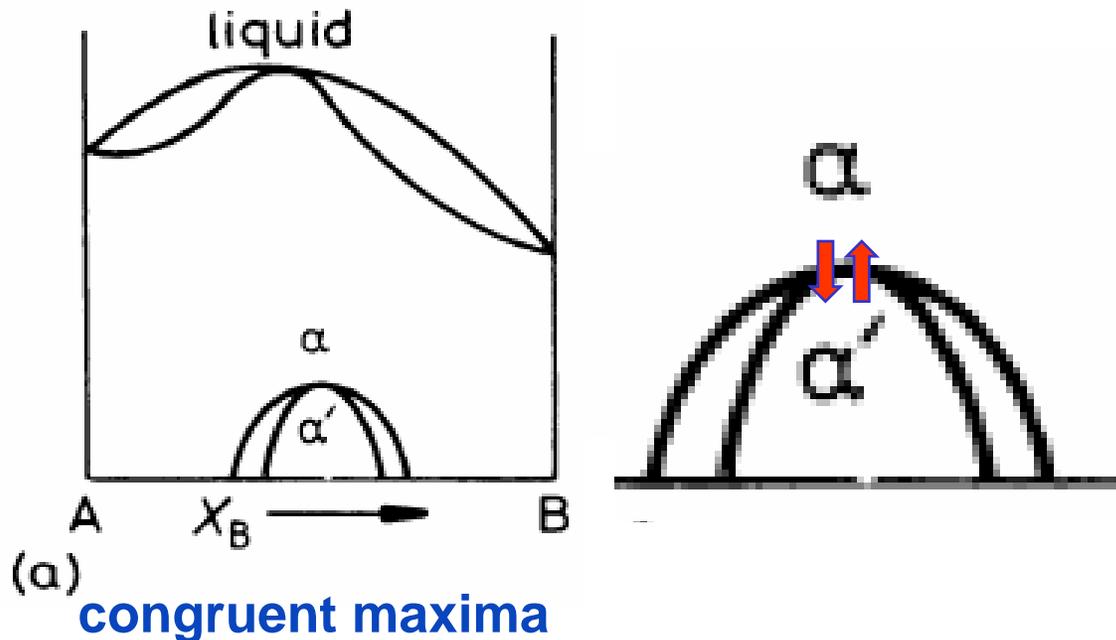
$$\Delta H_{mix}^L = 0 \quad \Delta H_{mix}^S < 0$$

- a. $\Delta H_{mix} < 0 \rightarrow$ A atoms and B atoms like each other.

How does the phase diagram differ from the previous case?

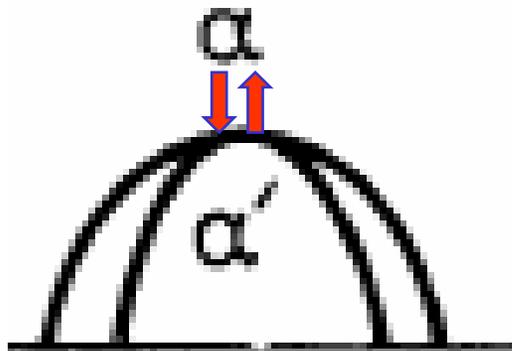
- b. What would happen when $\Delta H_{mix} \ll 0$?

\rightarrow The ordered state can extend to the melting temperature.



Order-disorder phase transformation

- Not classical phase change= \sim not depend on diffusion process
- **change of temperature allowed a continuous re-arrangement of atoms without changing the phase**
- **boundary: ordered lattice & disordered lattice/phase rule could not applied**
there are cases in which an ordered phase of one composition exists in equilibrium with a disordered phase of a different composition.
- Simple composition of the type AB or AB₃ can the transformation (i.e. at the temperature maximum) be considered diffusionless.



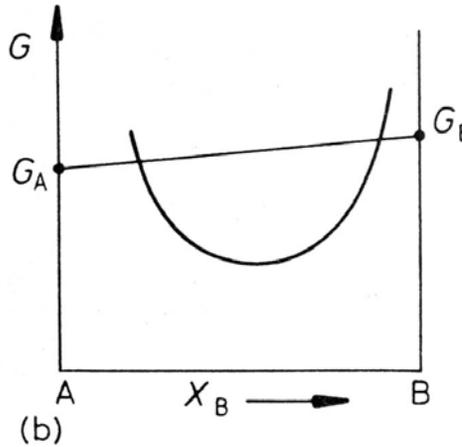
*** Solid solution**

- random mixing
- entropy ↑
- negative enthalpy ↓

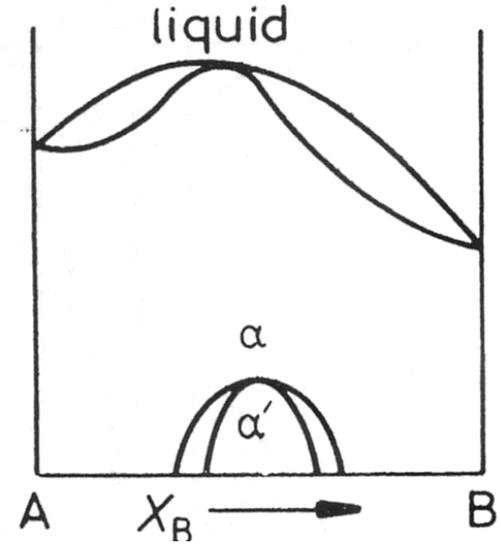
$$\Delta H_{mix}^S < 0$$

Large composition range

→ G ↓



diate phases: (a) for an intermetallic com-
(b) for an intermediate phase with a wide



*** Compound : AB, A₂B...**

- entropy ↓
- covalent, ionic contribution.
- enthalpy more negative ↓

$$\Delta H_{mix}^S \ll 0$$

Small composition range

→ G ↓

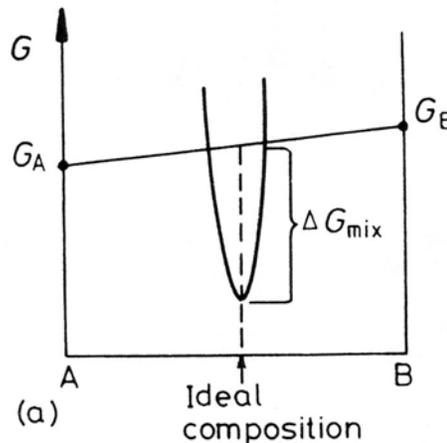
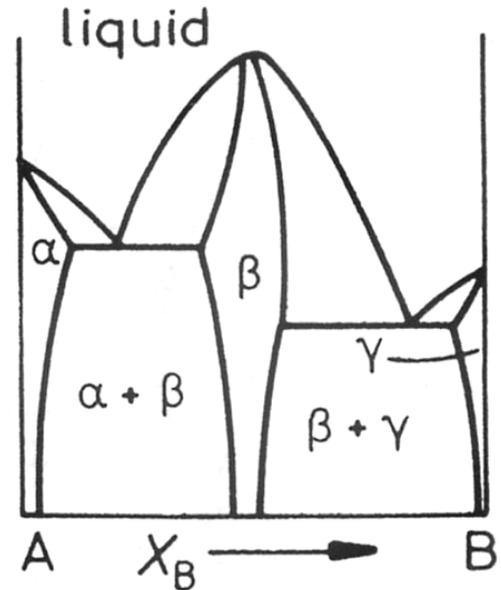
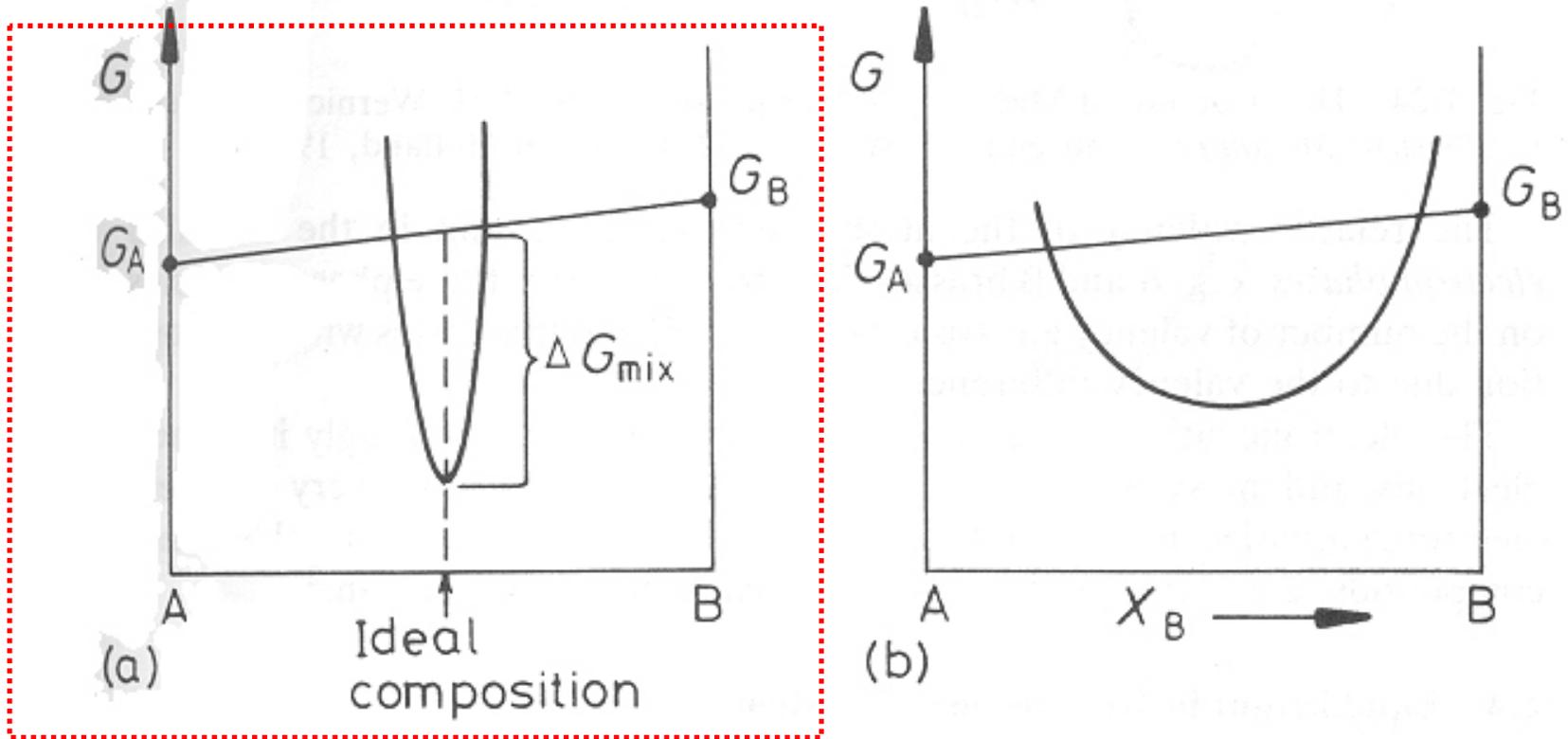


Fig. 1.23 Free energy curves for intermed
pound with a very narrow stability range, (



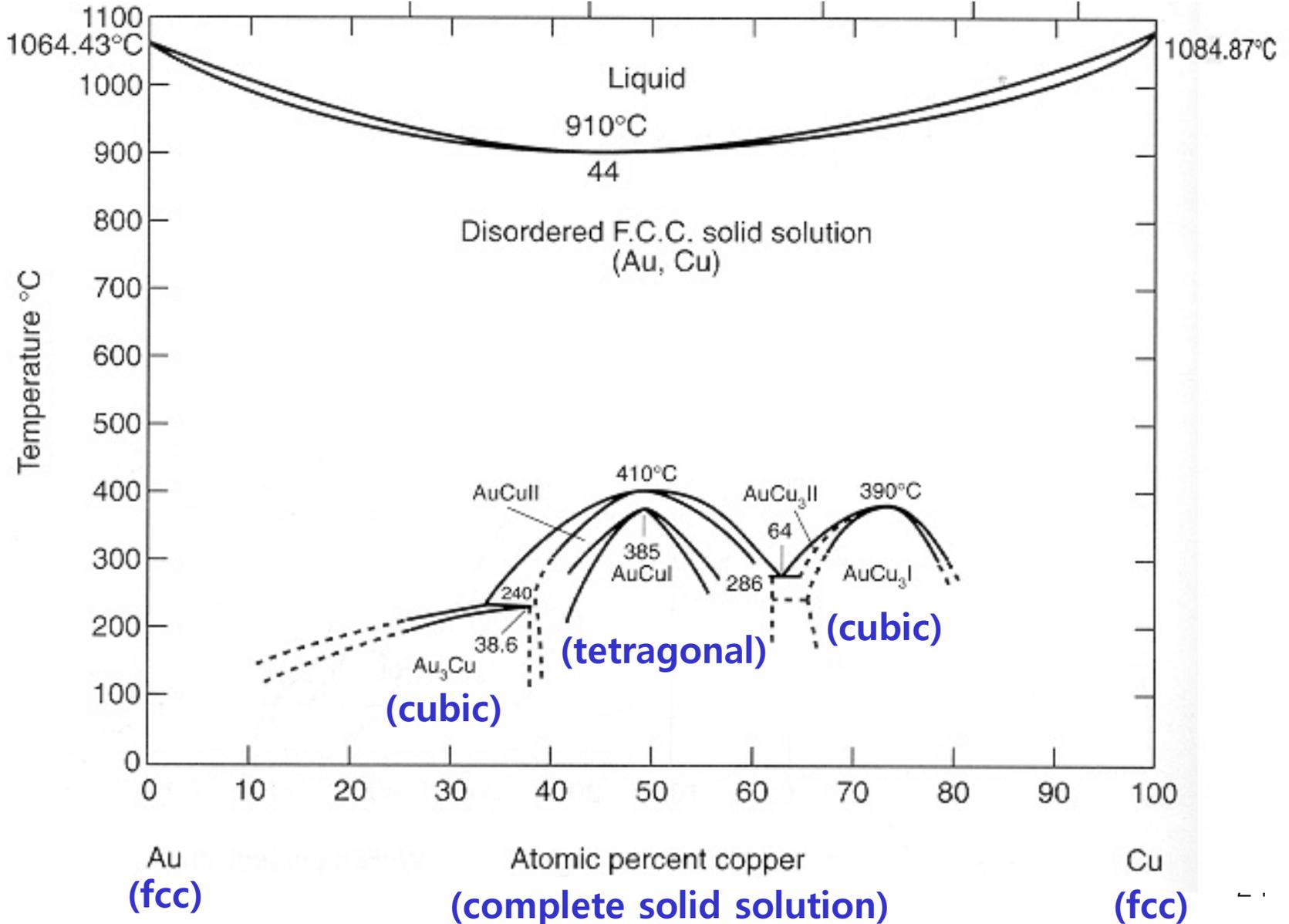
Intermediate Phase



- * **Many intermetallic compounds** have **stoichiometric composition** A_mB_n and a characteristic free energy curve as shown in Fig 1.23a.
- * In other structure, fluctuations in composition can be tolerated by **some atoms occupying 'wrong' position** or by **atom sites being left vacant**, and in these cases the **curvature** of the G curve is much less, Fig. 1.23b

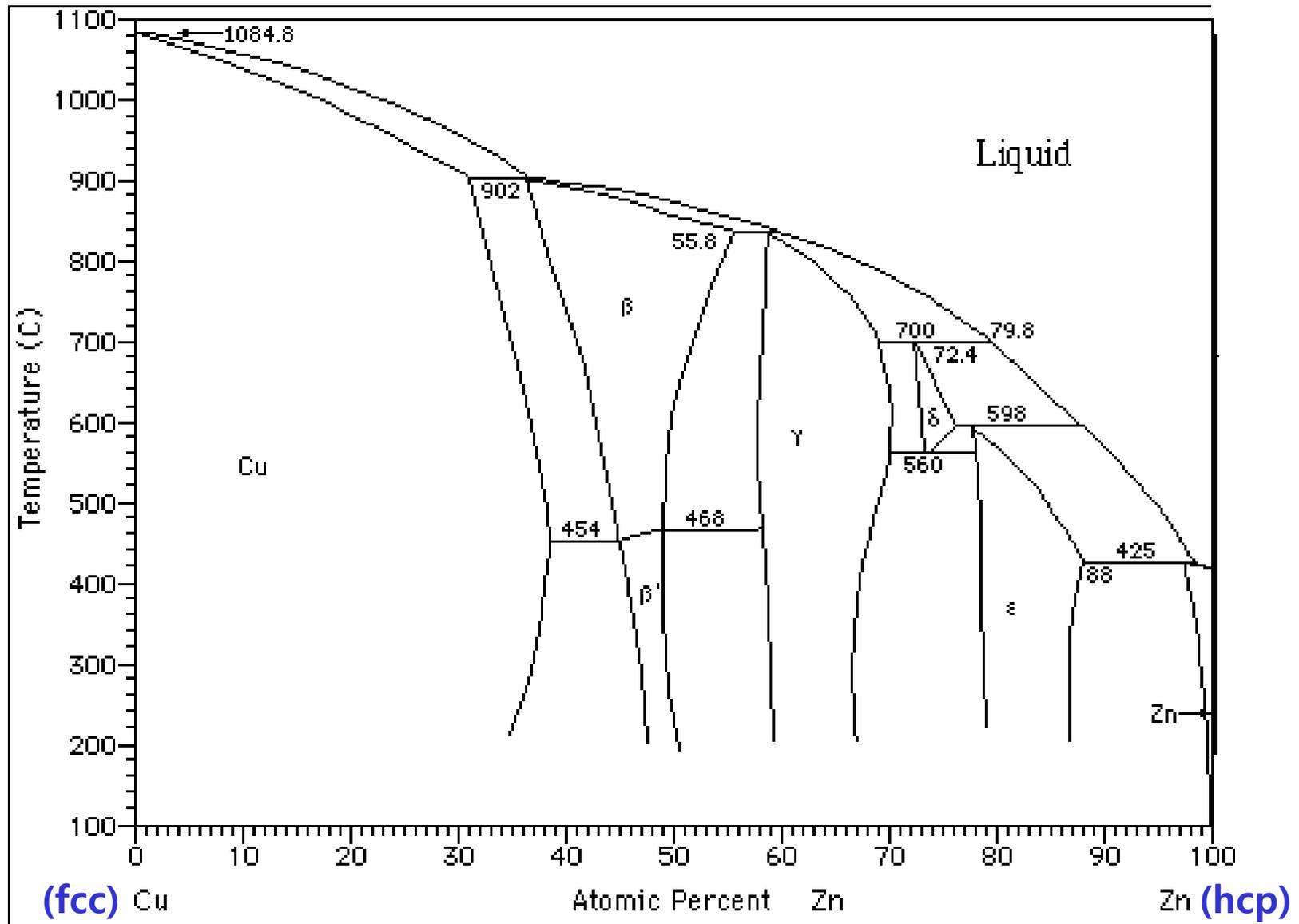
Ordered Phase

$$\varepsilon < 0, \Delta H_{\text{mix}} < 0 / \Delta H_{\text{mix}} \sim -20 \text{ kJ/mol}$$



Intermediate Phase

$$\varepsilon < 0, \Delta H_{\text{mix}} < 0 / \Delta H_{\text{mix}} \sim -21 \text{ kJ/mol}$$

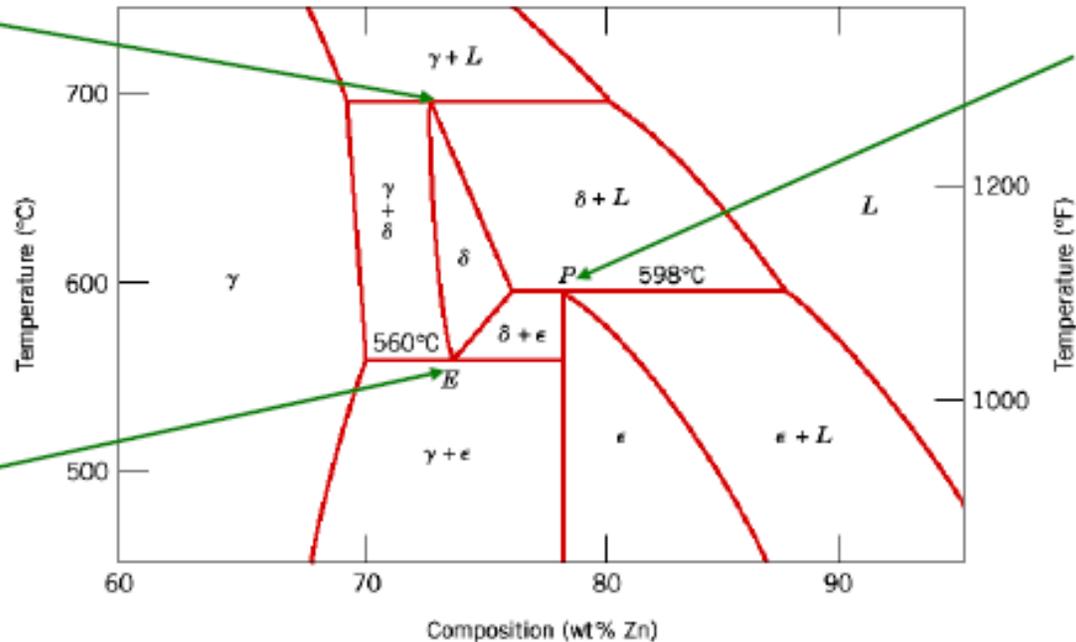


- α and η are terminal solid solutions
- β , β' , γ , δ and ε are intermediate solid solutions.

Cu-Zn Phase Diagram

Eutectoid and Peritectic Reactions

peritectic:
 $\gamma + L \rightleftharpoons \delta$



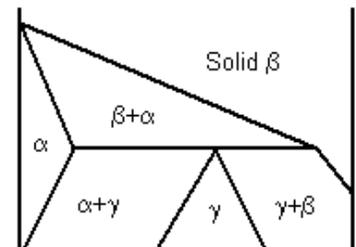
peritectic:
 $\delta + L \rightleftharpoons \epsilon$

eutectoid:
 $\delta \rightleftharpoons \gamma + \epsilon$

Eutectoid: one solid phase transforms into two other solid phases upon cooling

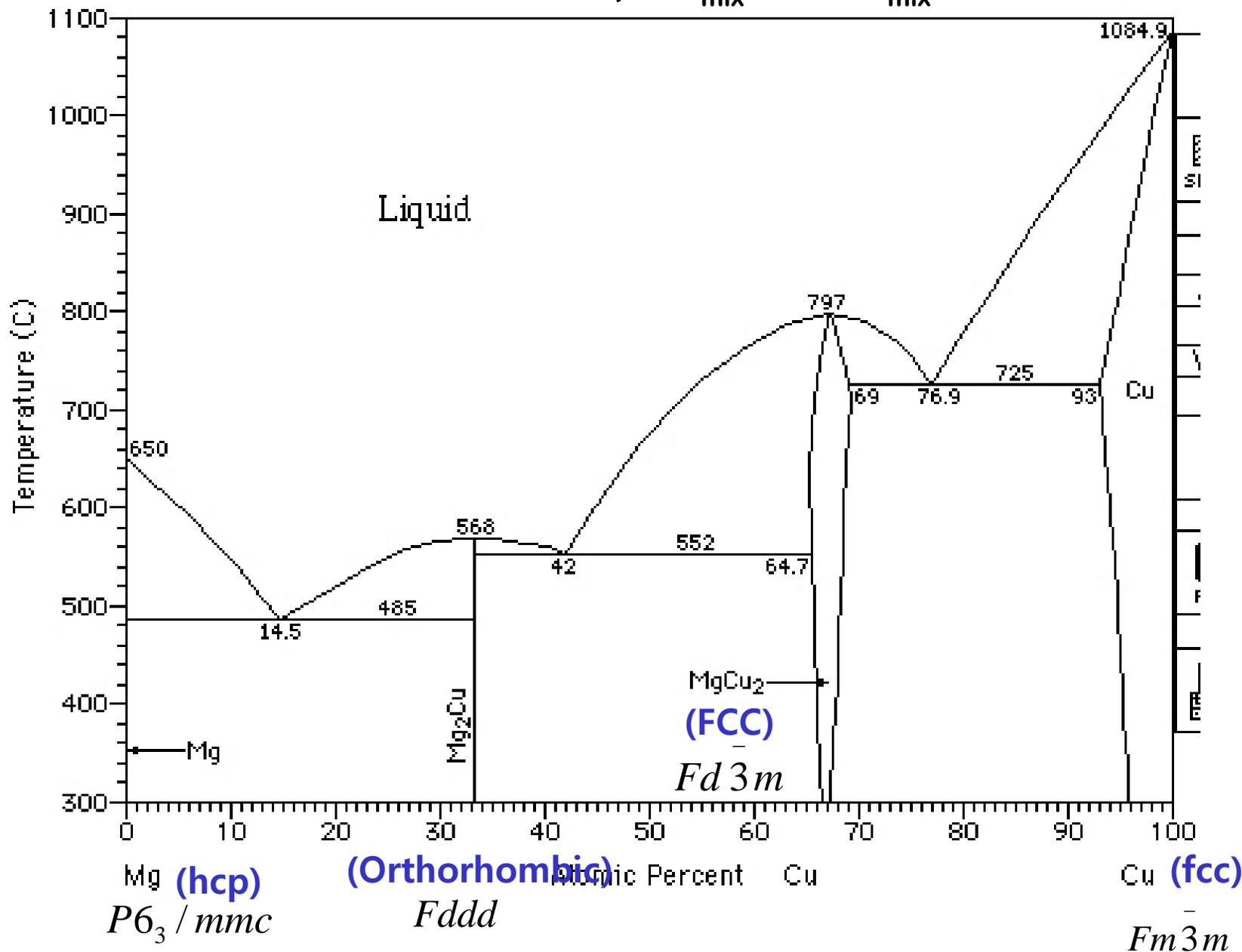
Peritectic: one solid and one liquid phase transform into another solid phase upon cooling

Peritectoid: two other solid phases transform into another solid phase upon cooling



Intermediate Phase

$$\varepsilon < 0, \Delta H_{\text{mix}} < 0 / \Delta H_{\text{mix}} \sim -38 \text{ kJ/mol}$$



Intermediate Phase

$$\varepsilon \ll 0, \Delta H_{\text{mix}} \ll 0 / \Delta H_{\text{mix}} \sim -142 \text{ kJ/mol}$$

