

1.2 Shear Strength of Granular Soils

- (1) Drained shear strength ($\phi', c' (=0)$)
($u_e=0$)

- Parameters affecting drained strength

1) density

2) mineral composition

3) grain size distribution

ϕ' (well graded) > ϕ' (poorly graded)

4) grain shape

ϕ' (angular particle) > ϕ' (rounded particle)

- **Components of drained strength**

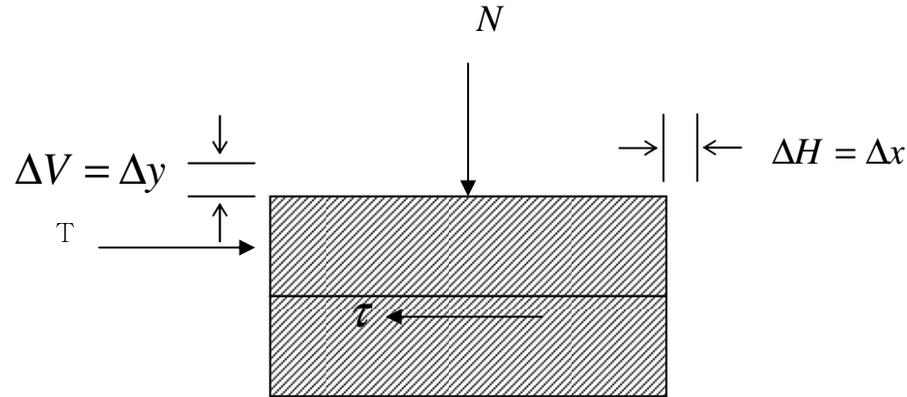
- Energy is expended in 2 ways.

- 1) overcome frictional resistance of soil

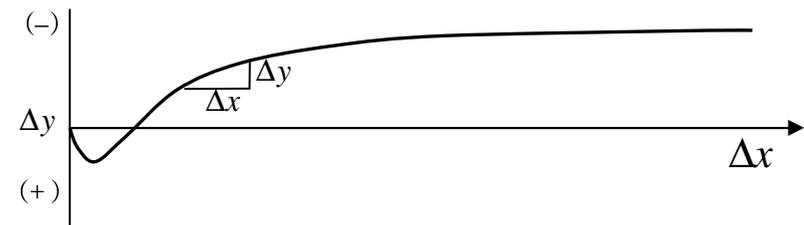
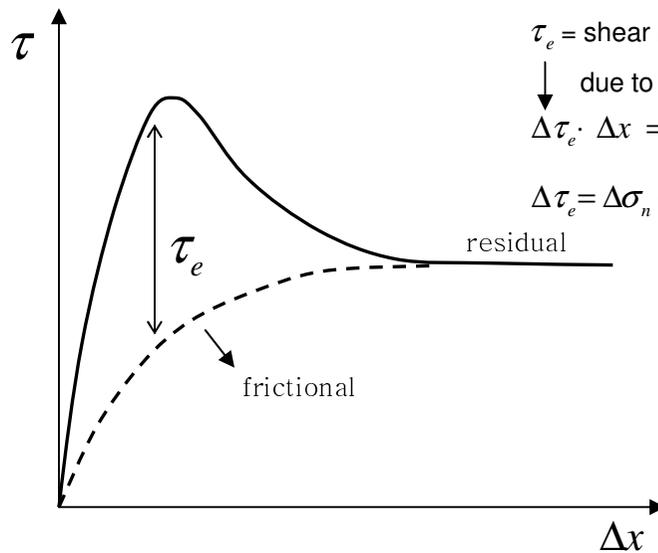
- 2) expand soil against confining pressure.

- (+ particle breakage, particle rearrangement)

● Taylor and Bishop (Direct shear)

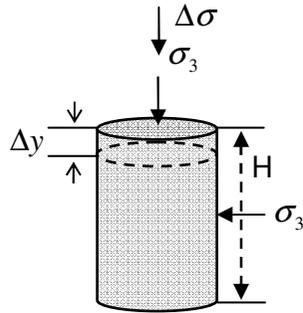


- For dense sand,

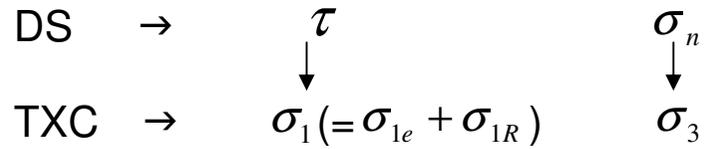


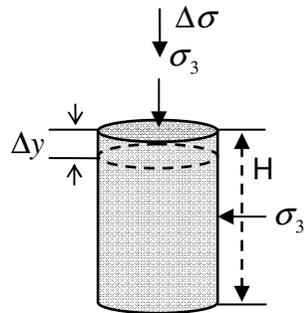
- Similar development can be made for TXC (based on drained test.)

$$(\sigma_c = \sigma'_c = \sigma_3 = \sigma'_3)$$



$$\epsilon_1 = \epsilon_a = \frac{\Delta y}{H}$$





$$\underbrace{\sigma_{1e}}_{\uparrow} d\epsilon_1 = \sigma_3 \left(\underbrace{\frac{dV}{V_0}}_{\uparrow} \right)$$

----- Eq. (1)

component of σ_1 due to vol. expansion ϵ_{vol}

$$\sigma_{1e} = \sigma_3 \frac{dV}{d\epsilon_1 V_0}$$

$$\Rightarrow \underbrace{\sigma_{1R}}_{\uparrow} = \sigma_1 - \sigma_{1e} = \sigma_1 - \sigma_3 \frac{dV}{d\epsilon_1 V_0}$$

----- Eq. (2)

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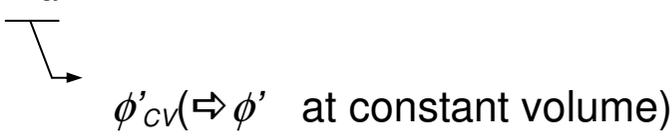
 component of σ_1 due to mineral friction
 and particle rearrangement

}

 $\rightarrow \phi'$ at constant volume

Recall, $\left(\frac{\sigma_1}{\sigma_3}\right)_f = \tan^2(45^\circ + \phi'/2)$

$$\therefore \left(\frac{\sigma_{1R}}{\sigma_3}\right)_f = \tan^2(45^\circ + \phi'_R/2) \quad \text{----- Eq. (3)}$$



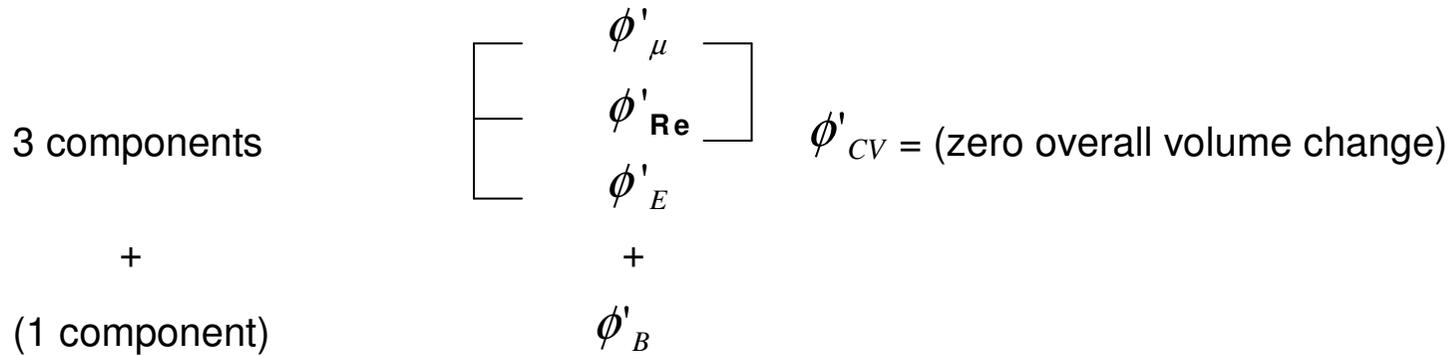
And from Eq.(2)

$$\left(\frac{\sigma_{1R}}{\sigma_3}\right) = \frac{\sigma_1}{\sigma_3} - \frac{dV}{d\varepsilon_1 V_0},$$

Therefore,

$$\underline{\tan^2(45^\circ + \phi'_R/2) = \left(\frac{\sigma_1}{\sigma_3}\right)_f - \frac{1}{(d\varepsilon_1)_f} \left(\frac{dV}{V_0}\right)_f}$$

● Component of friction angle



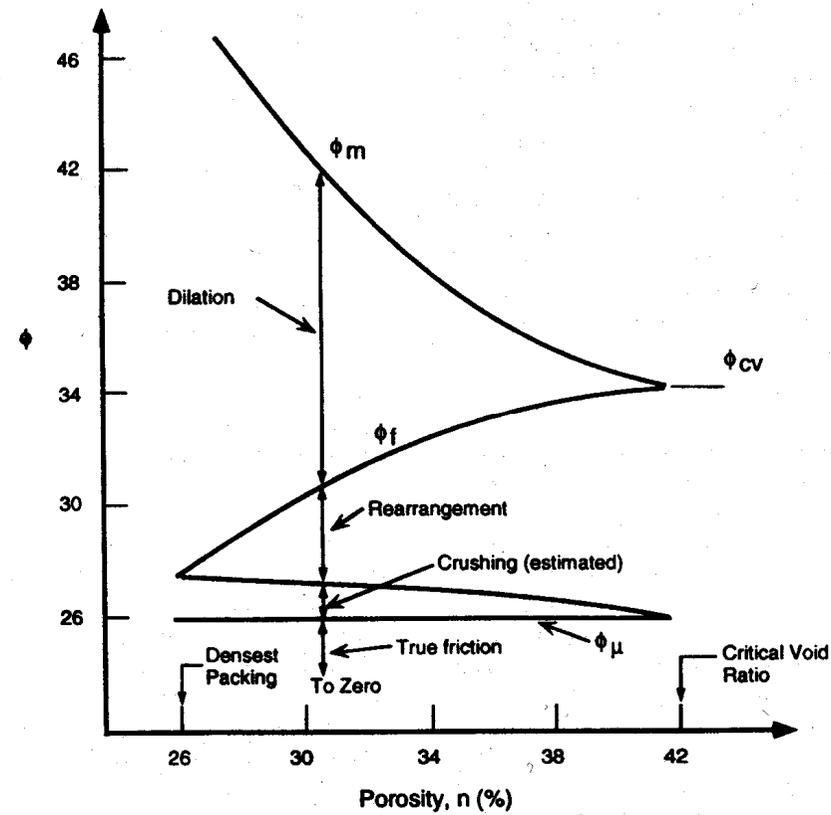
- ϕ'_{μ} values (Terzaghi, peck, and Mesri, table 19.1)

Mineral	ϕ'_{μ} , Range, deg (Typical Value)
Quartz	22-35 (26)
Feldspar	36-38 (37)
Hornblende	31
Calcite	31-34 (33)
Anthracite	31
Chalk	30

- Breakage component (ϕ'_B) of ϕ'
 - For quartz sands, $\sigma_3 > 500\text{psi}$, ϕ'_B becomes important.
 - For chlorite sands, $\sigma_3 > 50\text{psi}$, ϕ'_B becomes important.

- Accordingly,
 - For low σ_3 , ϕ'_{CV} and ϕ_E are important.
 - For high σ_3 , ϕ'_{CV} and ϕ_B are important.

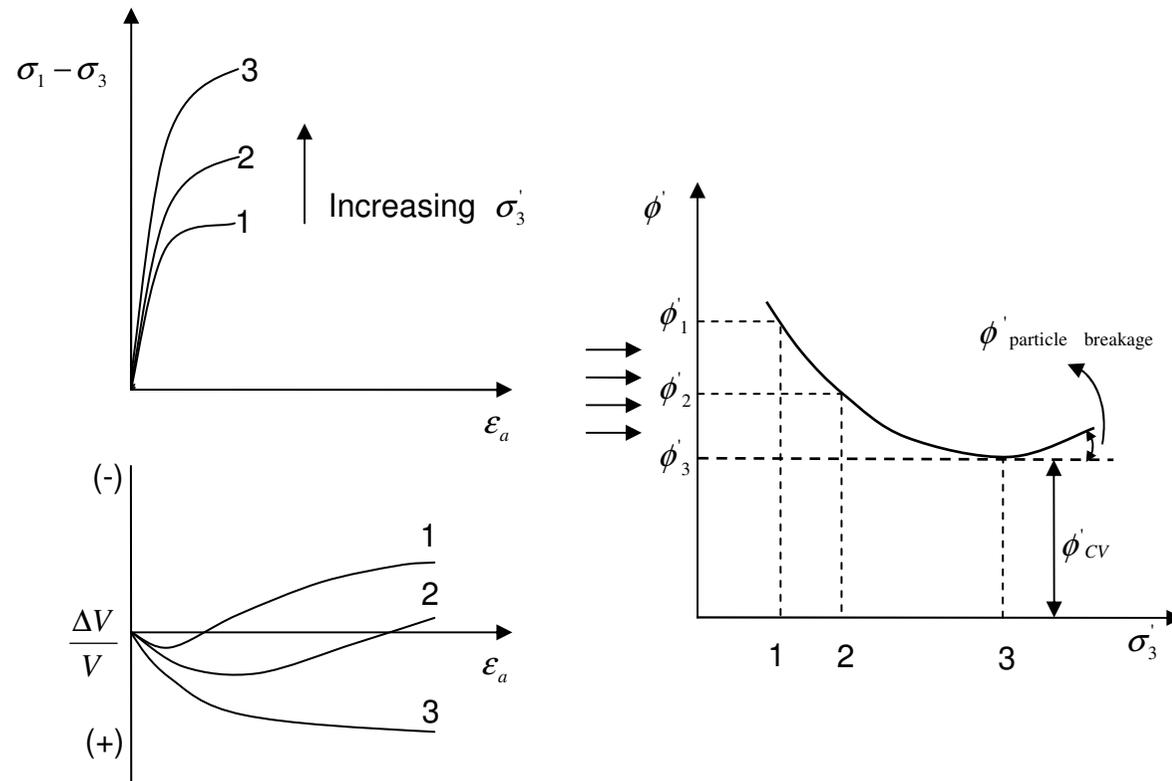
- For a given σ_{3c}'



(Redrawn after Rowe(1962))

● To test our hypothesis

Run tests on dense samples with varying σ_3' .



- The effect of relative density or void ratio, grain shape, grain size distribution, and particle size on ϕ'

By Cassagrande (Holtz and Kovacs, Table 11-2)

(Holtz and Kovacs, Table 11-3)

No.	General Description	Grain Shape	D_{10} (mm)	C_u	Loose		Dense	
					e	ϕ (deg)	e	ϕ (deg)
1	Ottawa standard sand	Well rounded	0.56	1.2	0.70	28	0.53	35
2	Sand from St. Peter sandstone	Rounded	0.16	1.7	0.69	31	0.47	37†
3	Beach sand from Plymouth, MA	Rounded	0.18	1.5	0.89	29	—	—
4	Silty sand from Franklin Falls Dam site, NH	Subrounded	0.03	2.1	0.85	33	0.65	37
5	Silty sand from vicinity of John Martin Dam, CO	Subangular to subrounded	0.04	4.1	0.65	36	0.45	40
6	Slightly silty sand from the shoulders of Ft. Peck Dam, MT	Subangular to subrounded	0.13	1.8	0.84	34	0.54	42
7	Screened glacial sand, Manchester, NH	Subangular	0.22	1.4	0.85	33	0.60	43
8‡	Sand from beach of hydraulic fill dam, Quabbin Project, MA	Subangular	0.07	2.7	0.81	35	0.54	46
9	Artificial, well-graded mixture of gravel with sands No. 7 and No. 3	Subrounded to subangular	0.16	68	0.41	42	0.12	57
10	Sand for Great Salt Lake fill (dust gritty)	Angular	0.07	4.5	0.82	38	0.53	47
11	Well-graded, compacted crushed rock	Angular	—	—	—	—	0.18	60

Factor	Effect
Void ratio e	$e \uparrow, \phi \downarrow$
Angularity A	$A \uparrow, \phi \uparrow$
Grain size distribution	$C_u \uparrow, \phi \uparrow$
Surface roughness R	$R \uparrow, \phi \uparrow$
Water W	$W \uparrow, \phi \downarrow$ slightly
Particle size S	No effect (with constant e)
Intermediate principal stress	$\phi_{ps} \geq \phi_{ix}$ (see Eqs. 11-5a, b)
Overconsolidation or prestress	Little effect