

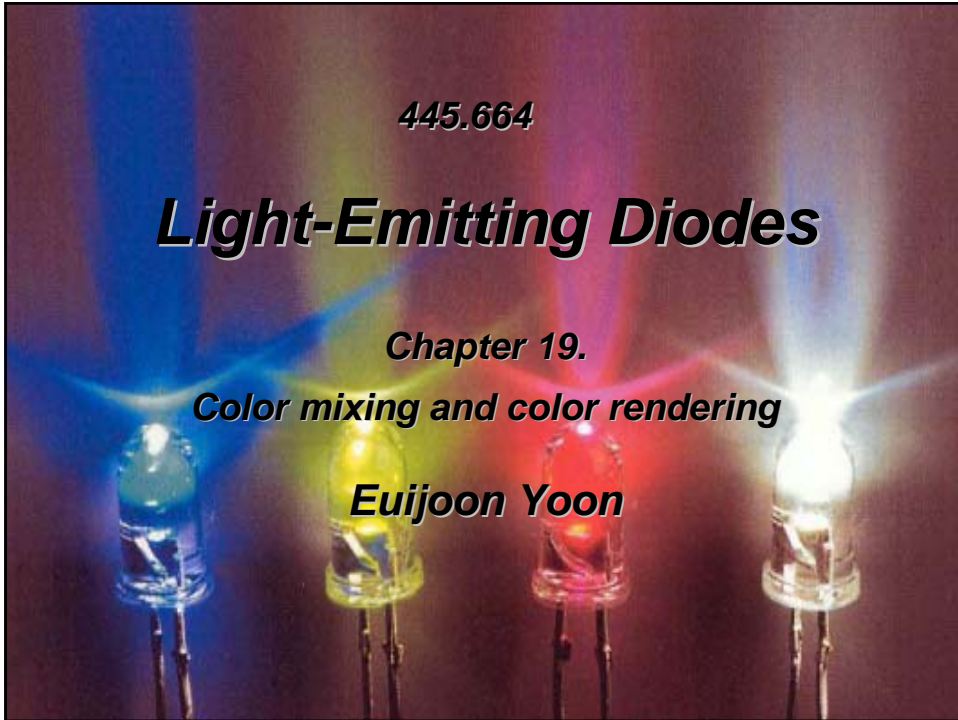
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# Light-Emitting Diodes

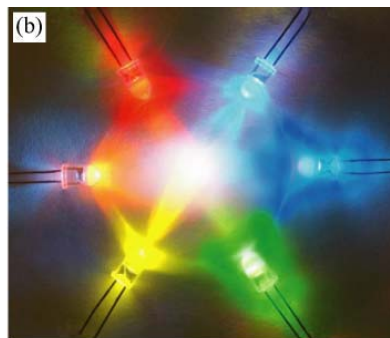
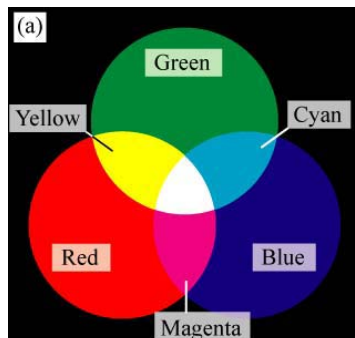
Chapter 19.

Color mixing and color rendering

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## Color mixing - examples



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Light-Emitting Diodes (Cambridge Univ. Press)  
[www.LightEmittingDiodes.org](http://www.LightEmittingDiodes.org)

- RGB color mixing
- Color gamut
- Gamut size increases with the number of light source.

## Additive color mixing

- In LED displays, three different types of LEDs, usually emitting in the red, green, and blue, are used. The three colors are mixed so that the observer sees a mixture of the three colors.

- If the spectral linewidth of the three sources is much narrower than the color matching functions, then

$$\begin{aligned} X &= \bar{x}(\lambda_1)P_1 + \bar{x}(\lambda_2)P_2 + \bar{x}(\lambda_3)P_3 & L_1 &= \bar{x}(\lambda_1)P_1 + \bar{y}(\lambda_1)P_1 + \bar{z}(\lambda_1)P_1 \\ Y &= \bar{y}(\lambda_1)P_1 + \bar{y}(\lambda_2)P_2 + \bar{y}(\lambda_3)P_3 & L_2 &= \bar{x}(\lambda_2)P_2 + \bar{y}(\lambda_2)P_2 + \bar{z}(\lambda_2)P_2 \\ Z &= \bar{z}(\lambda_1)P_1 + \bar{z}(\lambda_2)P_2 + \bar{z}(\lambda_3)P_3 & L_3 &= \bar{x}(\lambda_3)P_3 + \bar{y}(\lambda_3)P_3 + \bar{z}(\lambda_3)P_3 \end{aligned}$$

( $P_1$ ,  $P_2$ , and  $P_3$  are the optical powers emitted by the three sources.)

- The chromaticity coordinates of the combined light is given by

$$x = \frac{x_1 L_1 + x_2 L_2 + x_3 L_3}{L_1 + L_2 + L_3}, \quad y = \frac{y_1 L_1 + y_2 L_2 + y_3 L_3}{L_1 + L_2 + L_3}$$

- The chromaticity coordinate of the multi-component light is a linear combination of the individual chromaticity coordinates weighted by the  $L_i$  factors.

## Color mixing and color rendition

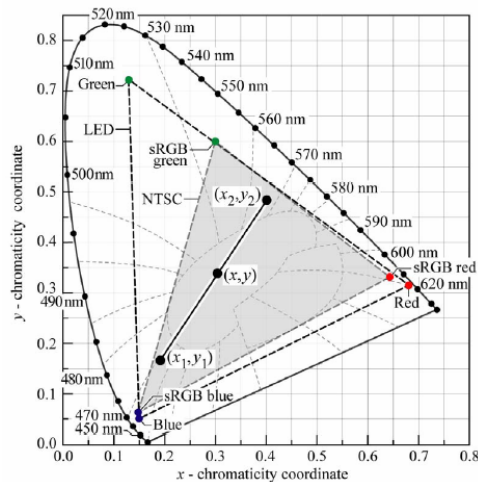


Fig. 11C.1. Principle of color mixing illustrated with two light sources with chromaticity coordinates  $(x_1, y_1)$  and  $(x_2, y_2)$ . The resulting color has the coordinates  $(x, y)$ . Also shown is the triangular area of the chromaticity diagram (color gamut) accessible by additive mixing of a red, green, and blue LED. The locations of the red, green, and blue phosphors of the sRGB display standard ( $x_r = 0.64, y_r = 0.33, x_g = 0.30, y_g = 0.60, x_b = 0.15, y_b = 0.06$ ) are also shown. The sRGB standard is similar to the NTSC standard.

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- **Color gamut**; represents all colors that can be created by mixing primary colors, e.g. red, green, and blue. **Webster: n. the entire scale or range**
- Gamut of Red-Green-Blue light source has triangular shape.
- Area of gamut matters for displays, color printers, etc.

## Color rendition

- A light source has **color rendition capability**
  - : Capability to render the true colors of an object



## Color rendering index

- Color rendering index (CRI)
  - A measure of the ability of the illuminant to faithfully render the colors of physical objects illuminated by source



High CRI

Low CRI

## Calculation of the CRI

- For the calculation of the CRI, the reference source is chosen as follows,
  - If the chromaticity point of the test source is located *on* the planckian locus, the reference source is a planckian black-body radiator with the same CT as the test source
  - One of the standardized CIE illuminants can be used as a reference source (CIE, 1995).
  - Planckian black-body reference source is assumed to have perfect color rendering properties. CRI=100
  - The selection of the reference source
    - Critical importance when calculating the CRI of the test sources.

## Test-color samples

### • CIE general CRI

$$CRI_{general} = \frac{1}{8} \sum_{i=1}^8 CRI_i \quad CRI_i = 100 - 4.6 \Delta E_i^*$$

- $\Delta E_i^*$ : The quantitative color change that occurs when a test-color sample is illuminated with, first, the reference illumination source (“reference source”), and subsequently with the test illumination source (“test source”).
- $\Delta E_i^*$  plays key role in the calculation of the CRI.

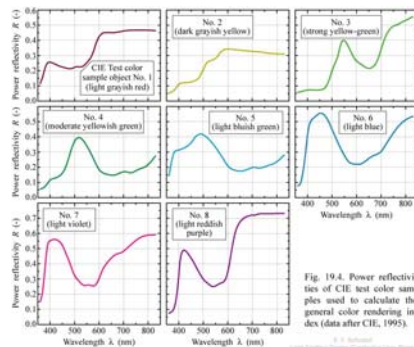


Fig. 19.4. Power reflectivities of CIE test color samples used to calculate the general color rendering index (data after CIE, 1995).

- The test-color samples are defined in terms of their spectral reflectivity.
- The general color-rendering index is calculated from these eight test-color samples.

## Special color-rendering indices

- In addition to the test-color samples (number 1-8) used to calculate the general color rendering index,
  - six supplemental test-color samples (number 9-14) are used.
- Further assess the color rendering capabilities of test sources.
- $CRI_9$  to  $CRI_{14}$ 
  - : Special color-rendering indices 9-14

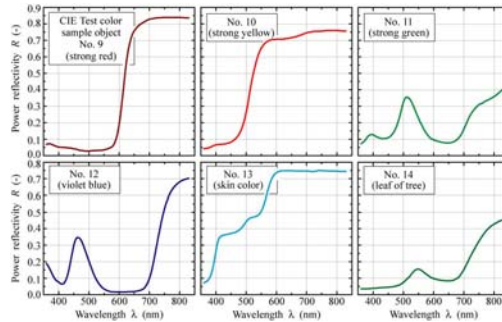


Fig. 19.5. Power reflectivities of CIE test color samples used to calculate the special color rendering indices  $CRI_9 - CRI_{14}$  (data after CIE, 1995).

- The reflectivity spectra and the numerical values of the reflectivity of the supplemental test-color samples.

## Chromaticity difference

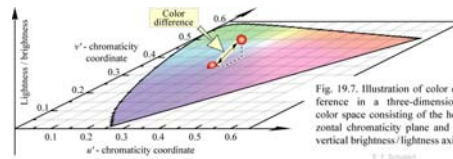
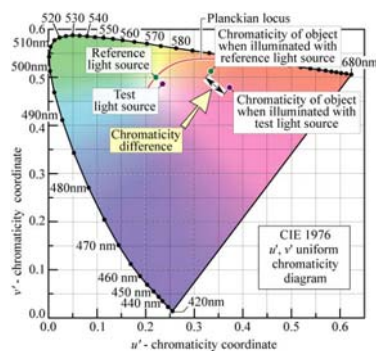


Fig. 19.7. Illustration of color difference in a three-dimensional color space consisting of the horizontal chromaticity plane and the vertical brightness/lightness axis.

- Test source is located slightly off the planckian locus.
- Reference source is a planckian source with the least possible distance from the test-source chromaticity point.
- 3<sup>rd</sup> axis could be added to the chromaticity diagram for a graphical representation of object lightness.

### ***Color rendering indices example***

<b><i>Light source</i></b>	<b><i>Color rendering index</i></b>
Sunlight	100
Quartz halogen W filament light	100
W filament incandescent light	100
Fluorescent light	60 – 85
Phosphor-based white LEDs	60 – 90
Trichromatic white light LEDs	60 – 90
Hg vapor light coated with phosphor	50
Na vapor light	40
Hg vapor light	20
Dichromatic white light LEDs	10 – 60
Green monochromatic light	– 50

Table: Color rendering indices (CRI) of different light sources.