

Power Aware Scheduling

Motivations

- PDAs and Pocket PCs
 - Display, processor, hard disk, and wireless LAN card are main sources of power consumption
 - Processor may consume up to 25% of the system power for laptop computers
 - Technology advance in processor architecture is much faster than battery technology
 - Powerful processors
 - Limited battery power
- Idea: Trade spare time against power saving with **DVS** (**Dynamic Voltage Scaling**)

Dynamic Voltage Scaling Processors

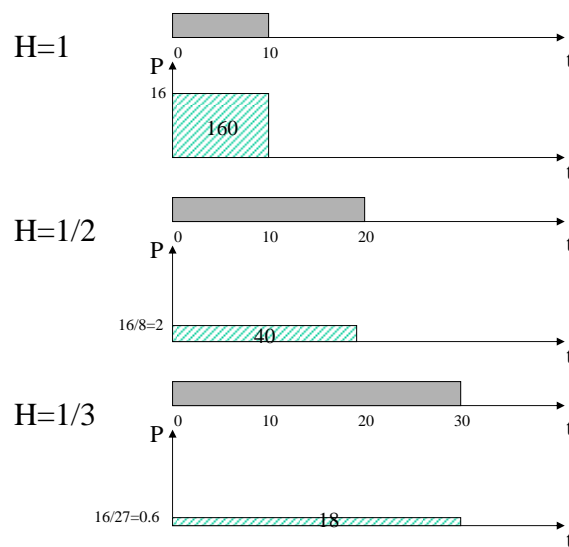
- Crusoe processor of Transmeta, Intel StrongARM processor
- Possible clock frequency (processor speed H) is proportional to supply voltage

$$f \propto V$$

- DVS can dynamically adjust supply voltage and thus processor speed
- Power consumption rate (P) vs. supply voltage (V) and clock frequency (f)

$$P = C \cdot f \cdot V^2 \propto V^3$$

Optimal Voltage? ($0 < V \approx H \leq 1$)



How to determine optimal speed in real-time systems?

- Minimize the energy consumption while guaranteeing the schedulability
- Theorem: n periodic tasks $\{(p_i, e_i, NPS_i) \mid 1 \leq i \leq n\}$ can be feasibly scheduled by EDF at processor speed H ($0 < H \leq 1$) if

$$\forall i, 1 \leq i \leq n, \sum_{j=1}^n \frac{e_j}{p_j} + \frac{\max\{NPS_j \mid p_j > p_i\}}{p_i} \leq H$$

- Proof:

$$\forall i, 1 \leq i \leq n, \sum_{j=1}^n \frac{e_j / H}{p_j} + \frac{\max\{NPS_j \mid p_j > p_i\} / H}{p_i} \leq 1$$

Optimization Problem

Minimize H

Subject to

$$\sum_{j=1}^n \frac{e_j}{p_j} + \frac{\max\{NPS_j \mid p_j > p_i\}}{p_i} \leq H \text{ for all } 1 \leq i \leq n$$

We change H only when a existing task leaves or a new task is admitted

Further Energy Saving

- First, while the blocking is not ongoing, the total utilization is lower than 1. So, we can further reduce the speed for spare times
- Second, the speed H was determined assuming WCET. If jobs execute much less than WCET, we can reclaim the unused time and the unused time can be used for further reduction of speed

Dual-Speed Switching Algorithm

- If the tasks are fully preemptible, they can be feasibly scheduled with a minimum speed L

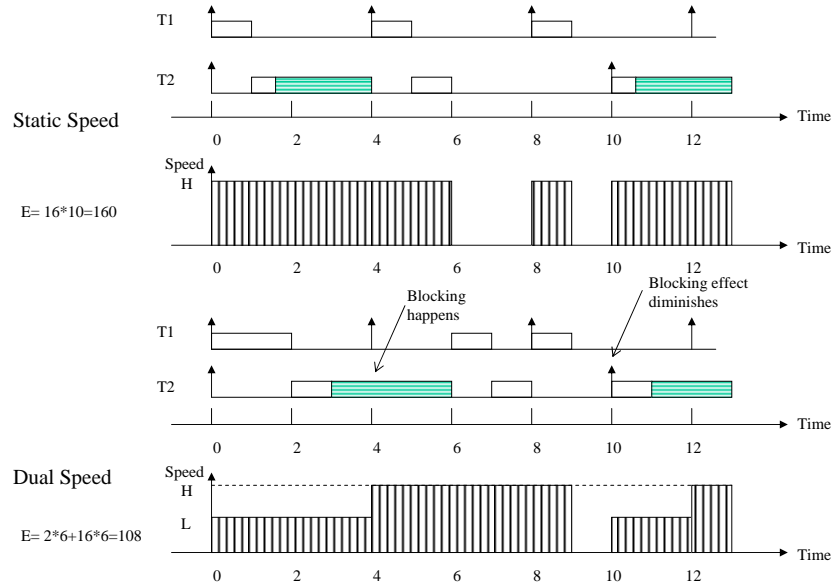
$$\sum_{j=1}^n \frac{e_j}{p_j} \leq L$$

- If a high priority job is blocked by a low priority job, the processor runs in High speed (H) mode until the blocking effect completely diminishes.

$$\forall i, 1 \leq i \leq n, \sum_{j=1}^n \frac{e_j}{p_j} + \frac{\max\{NPS_j \mid p_j > p_i\}}{p_i} \leq H$$

- In all other situations, the processor run in Low speed (L) mode

Dual-Speed Switching Algorithm



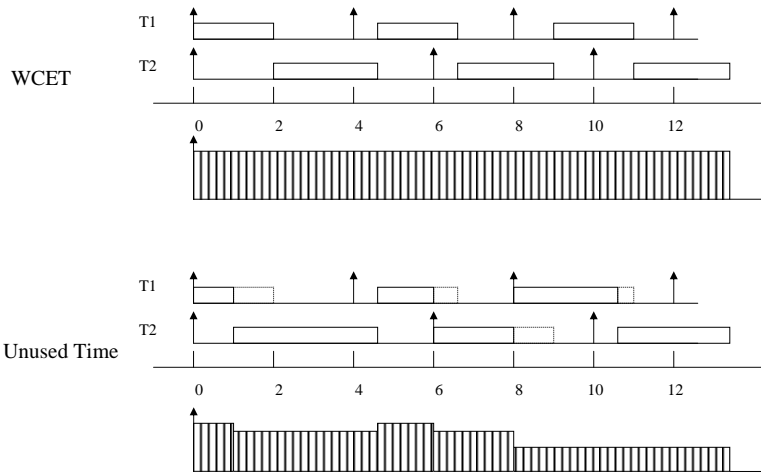
Reclaiming unused time

- When a job (whose deadline is d) finishes, the unused time (WCET – actualExeTime) is spare time for jobs whose deadline is later than d (Why NOT for jobs with deadlines earlier than d ?)
- If we allocate such unused time r to a job J with remaining execution time of e (and deadline later than d),

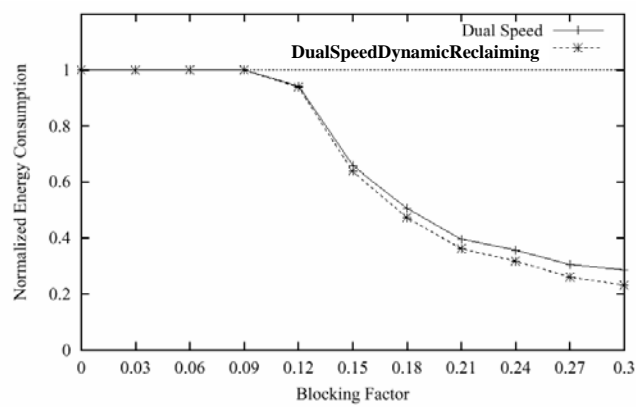
$$\frac{e}{L} = e + r,$$

$$L = \frac{e}{e + r}$$

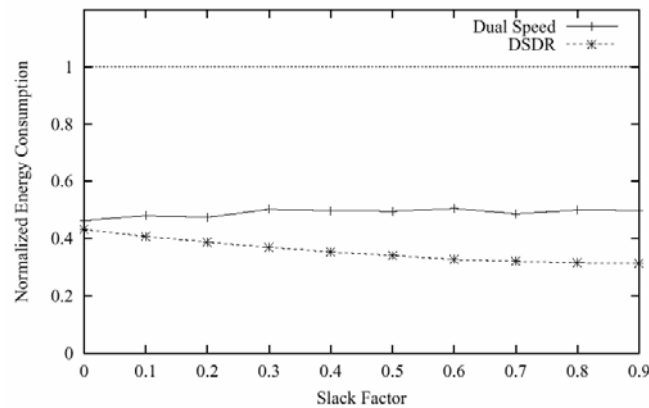
Reclaiming unused time



Normalized Energy Saving Relative to Static Speed (- blocking factor effect -)



Normalized Energy Saving Relative to Static Speed (- slack factor effect -)



Summary

- Power aware scheduling is a hot research topic
 - *Embedded processors with DVS*
 - *Radar scheduling with Energy budget constraints*
 - *Sensor network – power aware processing and routing*
- We saw an example where simple RT-theory can be effectively used for solving a very important and practical problem
- References
 - Hakan Aydin et al., Dynamic and Aggressive Scheduling Techniques for Power-Aware Real-Time Systems, RTSS 2001
 - Fan Zhang et al., Processor Voltage Scheduling for Real-Time Tasks with Non-Preemptible Sections, RTSS 2002