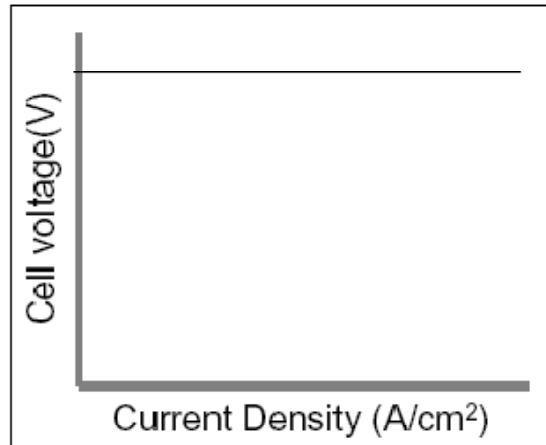
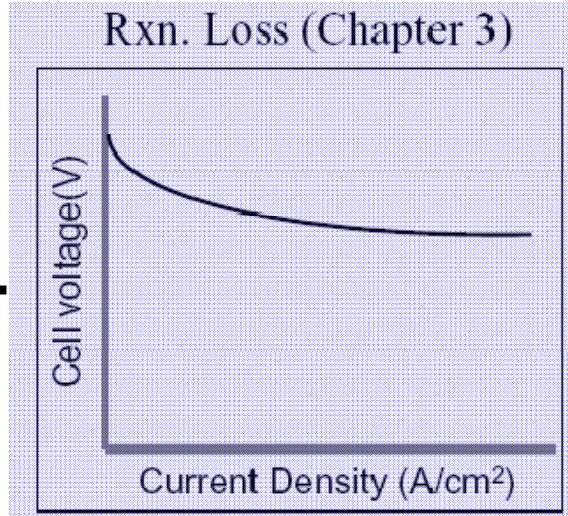


Losses in Fuel Cells

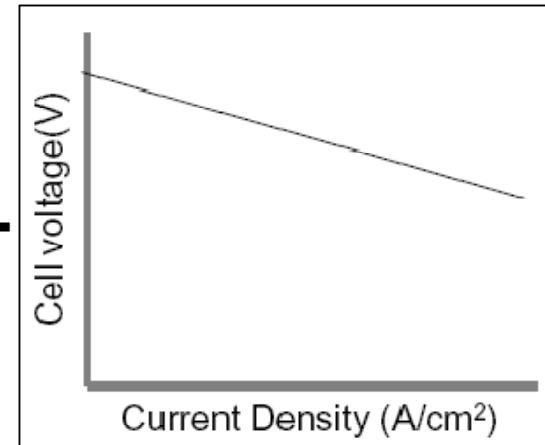
Reversible Voltage (Chapter 2)



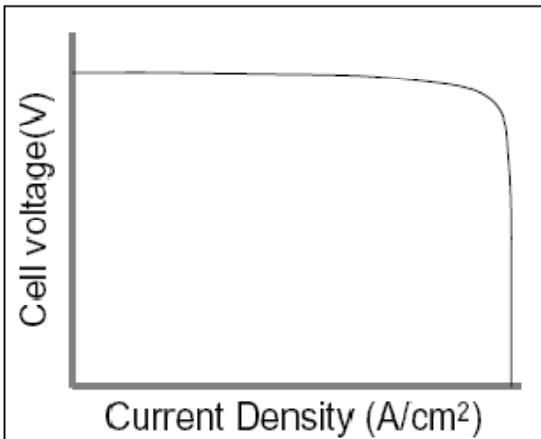
Rxn. Loss (Chapter 3)



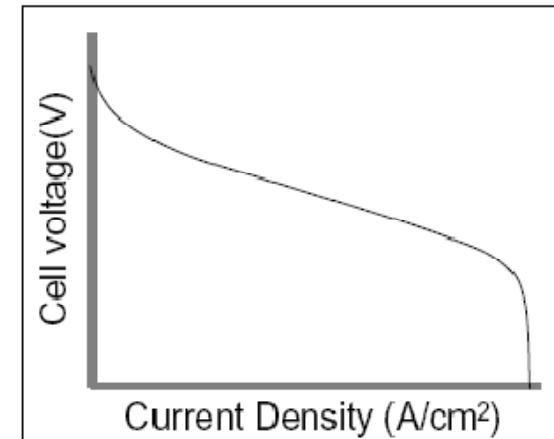
Ohmic Loss (Chapter 4)



Concentration Loss (Chapter 5)



Net Fuel Cell Performance



$$V = E_{\text{thermo}} - \eta_{\text{act}} - \eta_{\text{ohmic}} - \eta_{\text{conc}}$$

Fuel Cell Reaction Kinetics

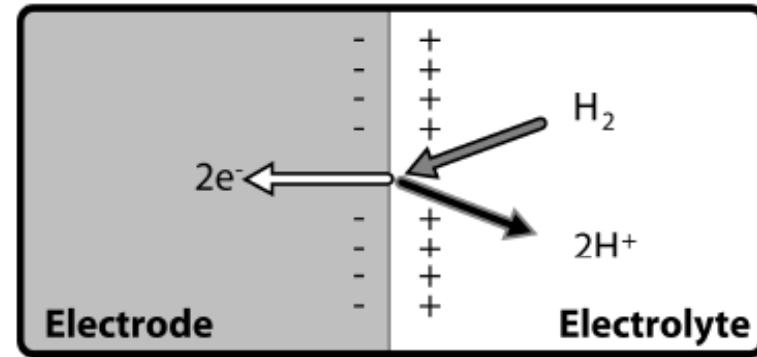
Electrode Kinetic

Current = Charge/Time

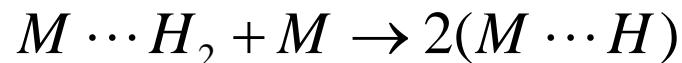
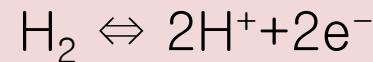
$$i = \frac{dQ}{dt} = \frac{nFdN}{dt}$$

$$\Leftrightarrow \int_0^t idt = Q = nFN$$

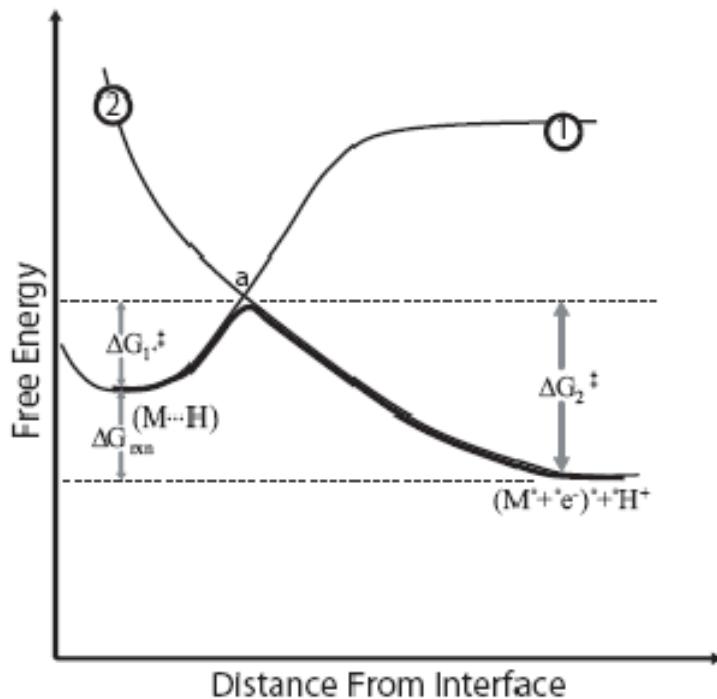
$$j = \frac{i}{A} [A/cm^2]$$



Heterogeneous process



Electrode Kinetic



Probability of activation

$$P_{act} = Ke^{\left(\frac{-\Delta G_1}{RT}\right)}$$

Forward reaction rate

$$\nu_1 = Kc_R^* f_1 P_{act} = Kc_R^* f_1 e^{\left(\frac{-\Delta G_1}{RT}\right)}$$

Backward reaction rate

$$\nu_2 = Kc_P^* f_2 P_{act} = Kc_P^* f_2 e^{\left(\frac{-\Delta G_2}{RT}\right)}$$

Rate of reaction

$$\begin{aligned} \nu &= \nu_1 - \nu_2 = Kc_R^* f_1 e^{\left(\frac{-\Delta G_1}{RT}\right)} - Kc_P^* f_2 e^{\left(\frac{-\Delta G_2}{RT}\right)} \\ &= Kc_R^* f_1 e^{\left(\frac{-\Delta G_1}{RT}\right)} - Kc_P^* f_2 e^{\left(\frac{-\Delta G_1 - \Delta G_{rxn}}{RT}\right)} \end{aligned}$$

Equilibrium Potential: Galvani Potential

Conversion to current density

$$j = nFv = nFc_R^* f_1 e^{\left(\frac{-\Delta G_1}{RT}\right)} - nFc_P^* f_2 e^{\left(\frac{-\Delta G_1 - \Delta G_{rxn}}{RT}\right)}$$

$$= j_1 - j_2$$

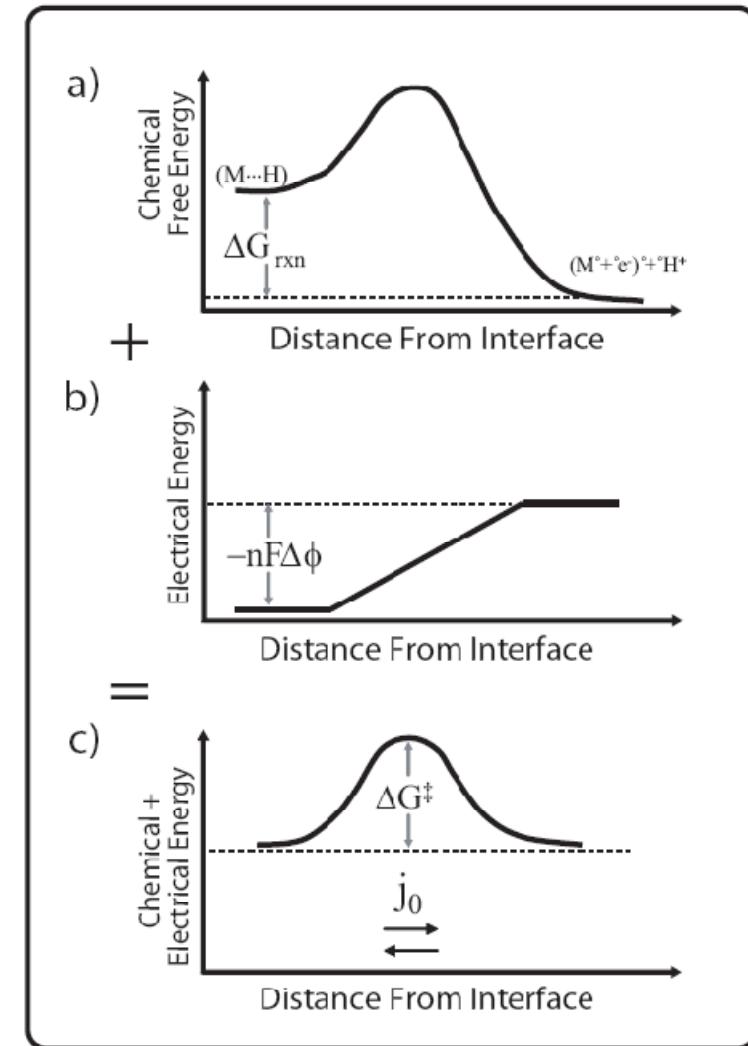
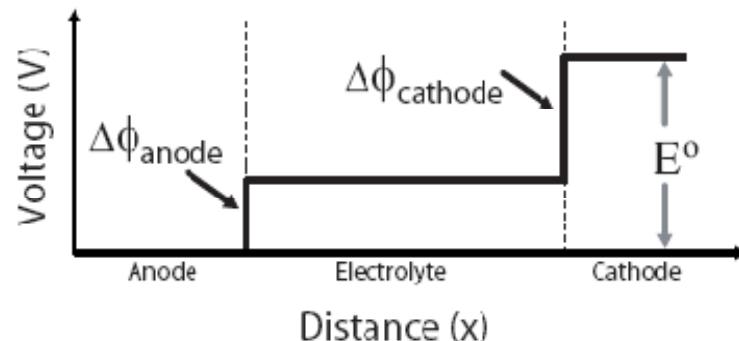
At equilibrium

$$j = j_1 - j_2 = 0$$

$j_1 = j_2 = j_0$: Exchange Current Density

$$j_1 = nFc_R^* f_1 e^{\left(\frac{-\Delta G_1 + nF\Delta\phi}{RT}\right)} = nFc_R^* fe^{\left(\frac{-\Delta G^{++}}{RT}\right)}$$

$$j_2 = nFc_P^* f_2 e^{\left(\frac{-\Delta G_1 - \Delta G_{rxn} + nF\Delta\phi}{RT}\right)} = nFc_P^* fe^{\left(\frac{-\Delta G^{++}}{RT}\right)}$$



Bultler–Volmer Equation: Non-Equilibrium

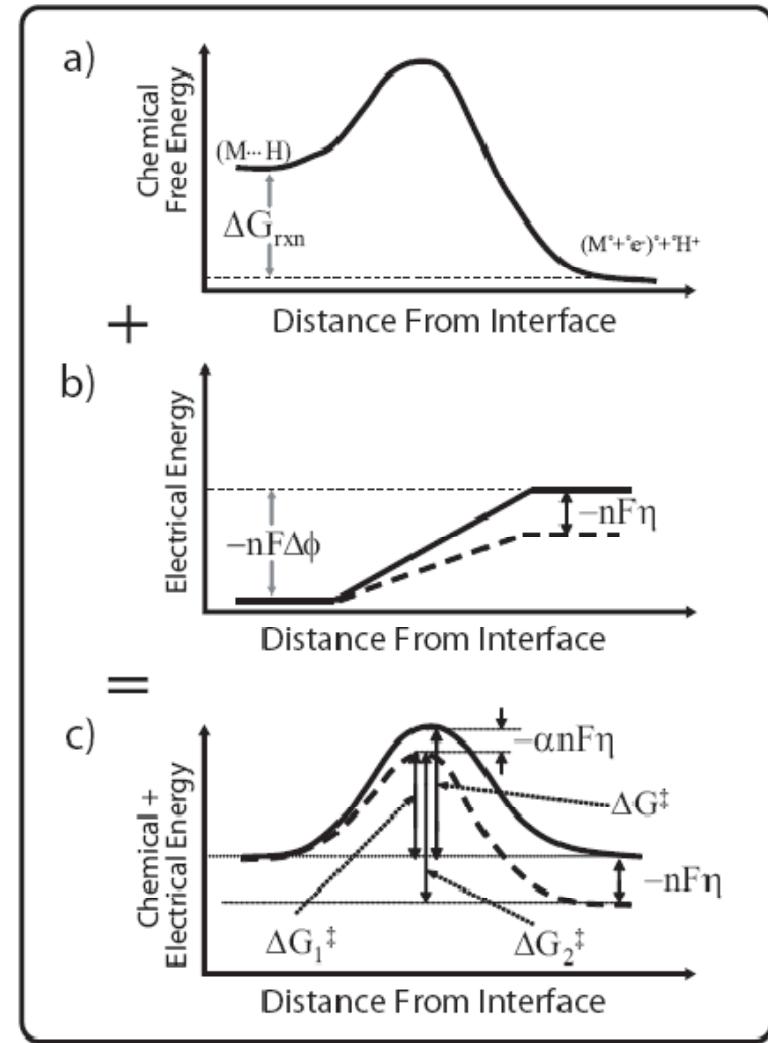
$$j_1 = j_0 e^{\left(\frac{\alpha nF\eta}{RT}\right)}$$

$$j_2 = j_0 e^{-\left(\frac{(1-\alpha)nF\eta}{RT}\right)}$$

$$j = j_0 \left(e^{\left(\frac{\alpha nF\eta}{RT}\right)} - e^{-\left(\frac{(1-\alpha)nF\eta}{RT}\right)} \right)$$

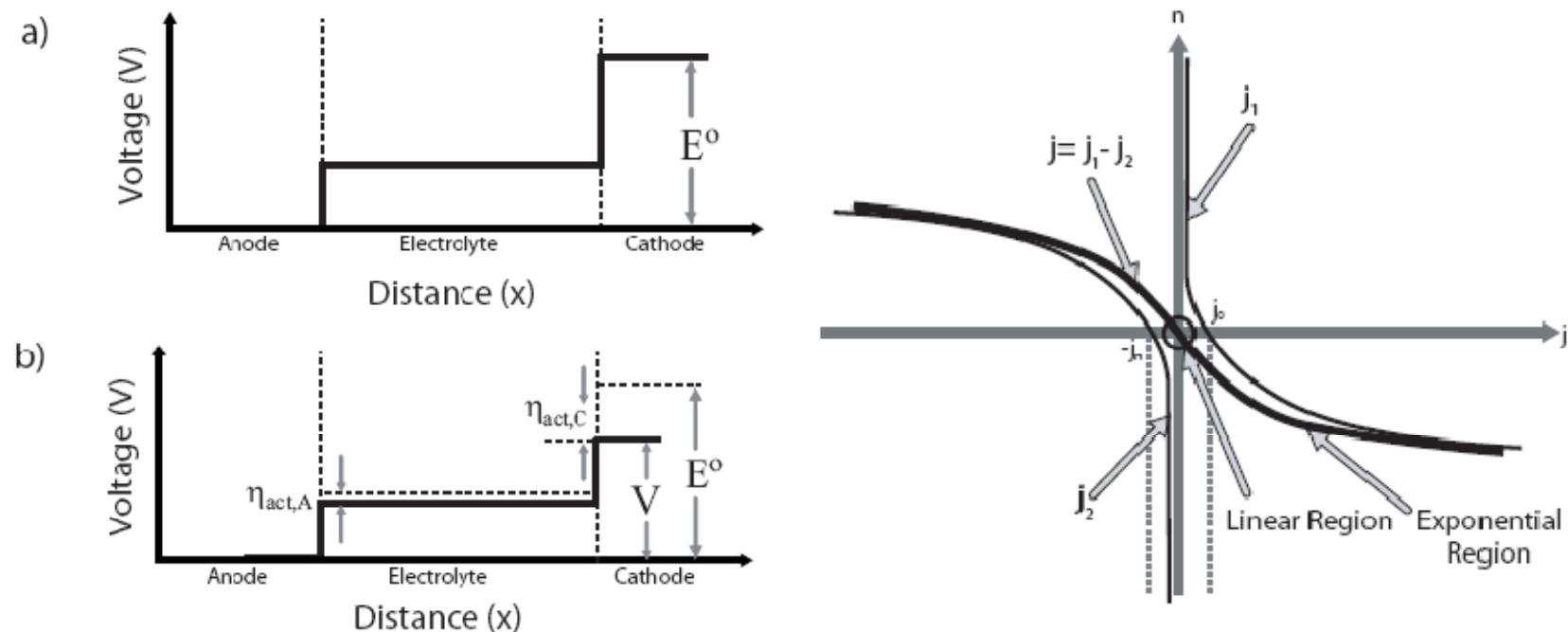
$$j = j_0 \left(\frac{C_R}{C_R^0} e^{\left(\frac{\alpha nF\eta}{RT}\right)} - \frac{C_P}{C_P^0} e^{-\left(\frac{(1-\alpha)nF\eta}{RT}\right)} \right)$$

Bulter–Volmer Equation



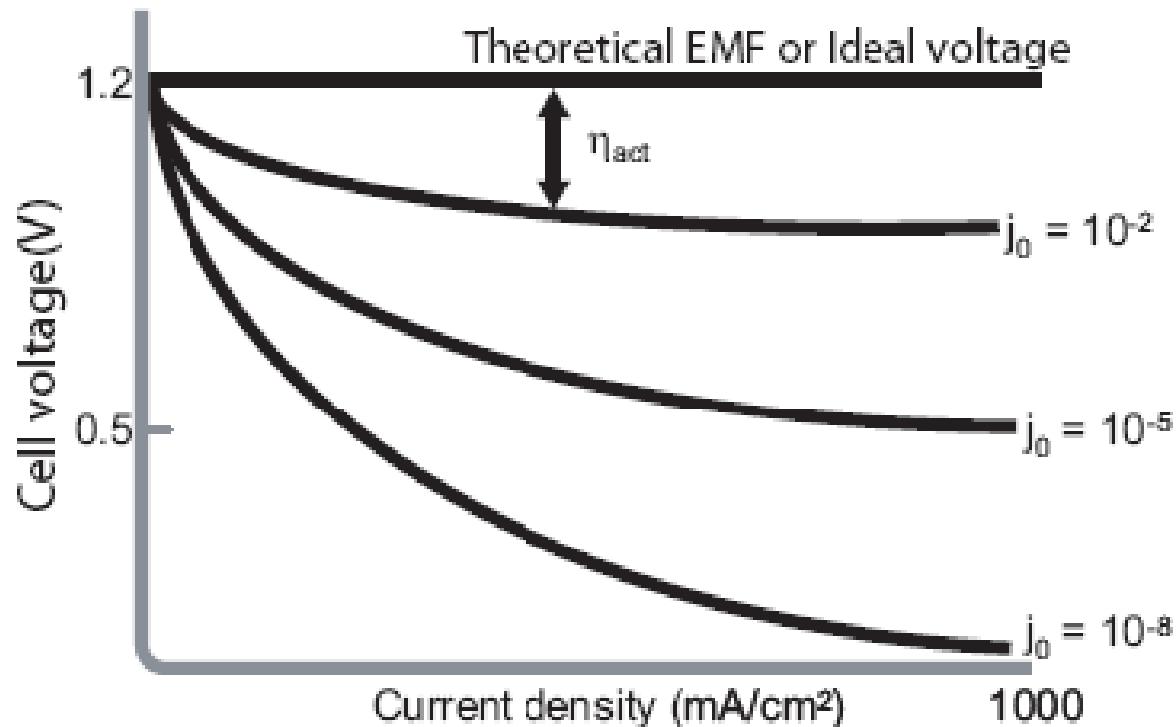
Boltz–Volmer Equation: Non-Equilibrium

$$j = j_0 \left(\frac{C_R}{C_R^0} e^{\left(\frac{\alpha n F \eta}{RT} \right)} - \frac{C_P}{C_P^0} e^{-\left(\frac{(1-\alpha)n F \eta}{RT} \right)} \right)$$



Exchange Current Density Effect

$$j = j_0 \left(\frac{C_R}{C_R^0} e^{\left(\frac{\alpha nF\eta}{RT} \right)} - \frac{C_P}{C_P^0} e^{-\left(\frac{(1-\alpha)nF\eta}{RT} \right)} \right)$$



Improving Kinetic

$$j = j_0 \left(\frac{C_R}{C_R^0} e^{\left(\frac{\alpha n F \eta}{RT} \right)} - \frac{C_P}{C_P^0} e^{-\left(\frac{(1-\alpha) n F \eta}{RT} \right)} \right)$$

1. C_R : Increase reactant concentration
2. Increase j_0

$$j_0 = n F C^* f e^{\left(\frac{-\Delta G^{++}}{RT} \right)}$$

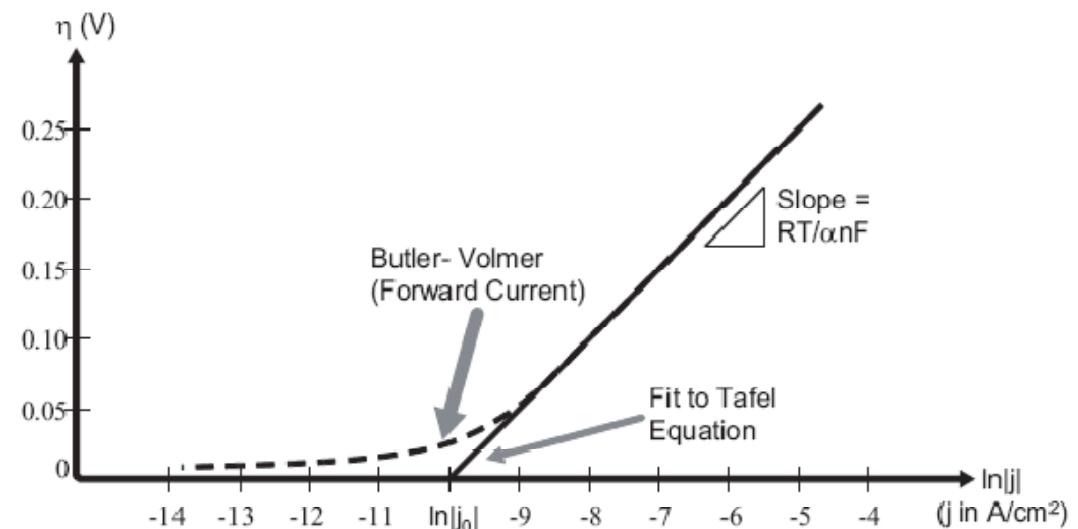
- Decrease the activation energy (G^{++})
- Increase T
- Increase reaction site (equivalent to C^*)

Simplified B-V Equation

1. When n_{act} is very small

$$j = j_0 \frac{nF\eta_{act}}{RT}$$

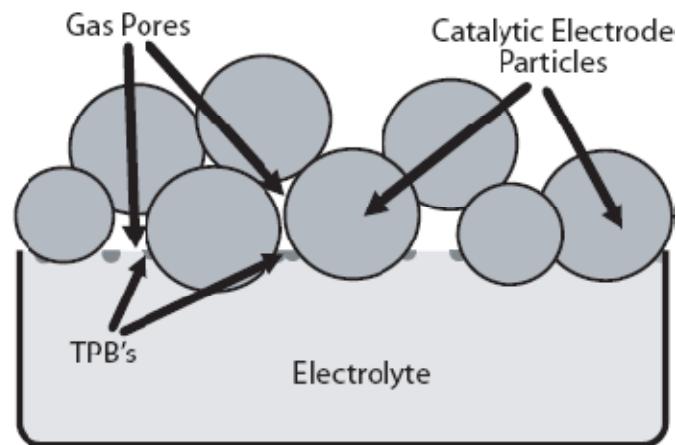
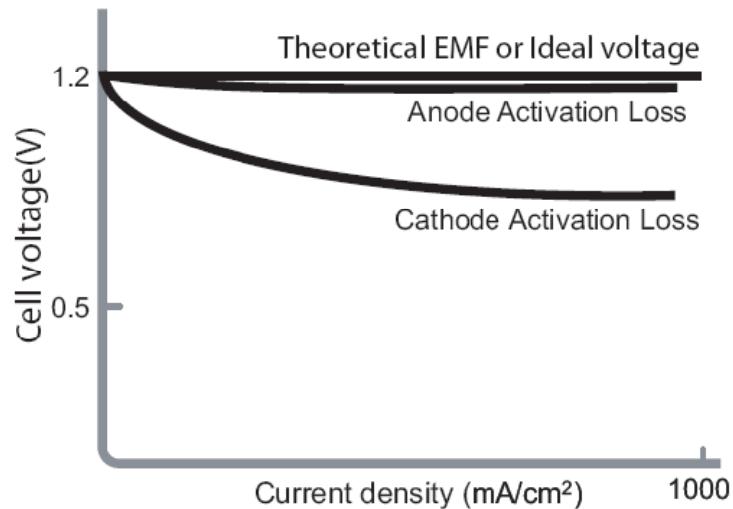
1. When n_{act} is large



$$j = j_0 e^{\frac{\alpha n F \eta_{act}}{RT}} \text{ or } \eta_{act} = -\frac{RT}{\alpha n F} \ln j_0 + \frac{RT}{\alpha n F} \ln j \\ = a + b \log j$$

Tafel Equation

B-V Equation: Practical Consideration



Triple Phase Boundary

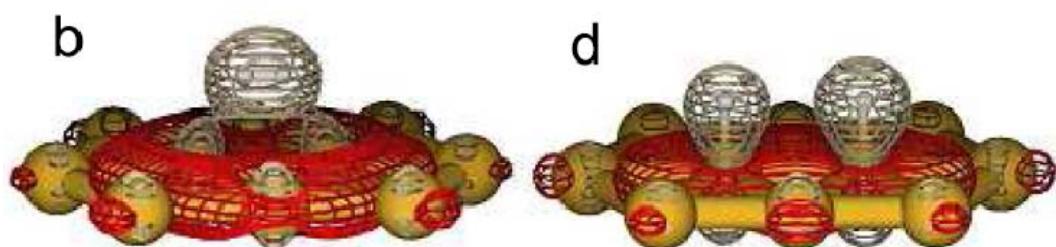
Hydrogen

Surface	Electrolyte	j'_0 (A/cm^2)
Pt	Acid	10^{-3}
Pt	Alkaline	10^{-4}
Pd	Acid	10^{-4}
Rh	Alkaline	10^{-4}
Ir	Acid	10^{-4}
Ni	Alkaline	10^{-4}
Ni	Acid	10^{-5}

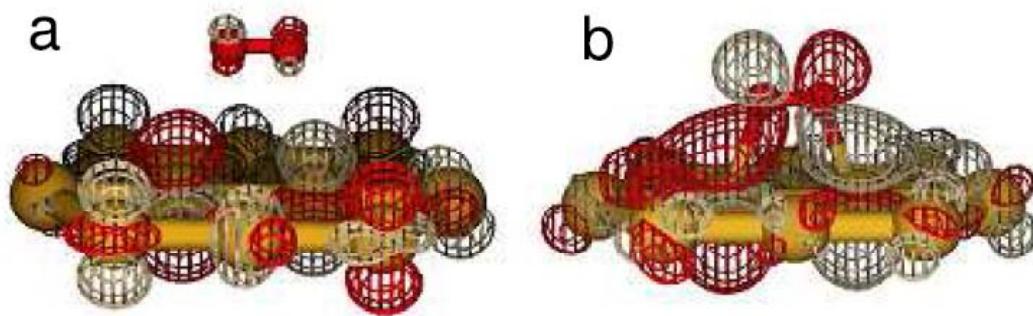
Oxygen

Surface	Electrolyte	j'_0 (A/cm^2)
Metal Surfaces in Acid Electrolyte		
Pt	Acid	10^{-9}
Pd	Acid	10^{-10}
Ir	Acid	10^{-11}
Rh	Acid	10^{-11}
Au	Acid	10^{-11}
Pt-Alloys in PEM Fuel Cell		
Pt/C	Nafion	3×10^{-9}
PtMn/C	Nafion	6×10^{-9}
PtCr/C	Nafion	9×10^{-9}
PtFe/C	Nafion	7×10^{-9}
PtCo/C	Nafion	6×10^{-9}
PtNi/C	Nafion	5×10^{-9}

Understanding Catalyst via DFT

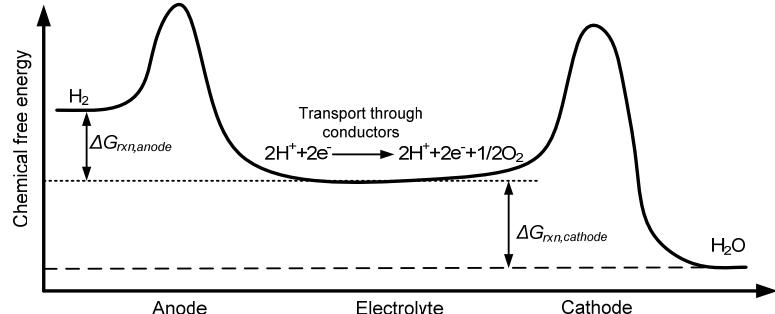


Hydrogen dissociation

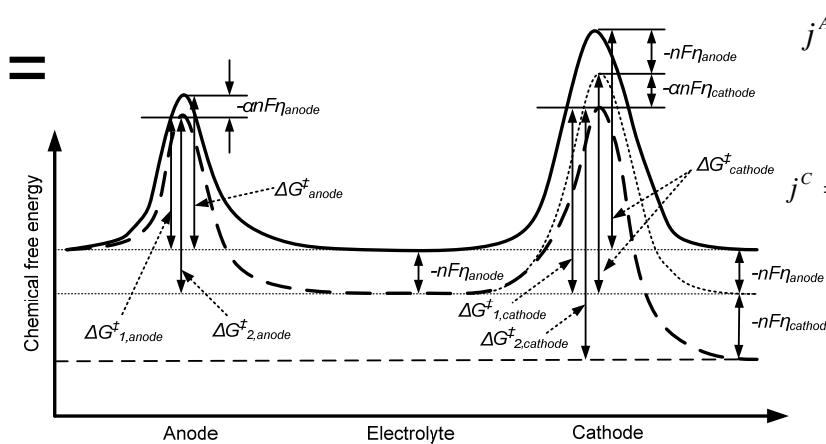
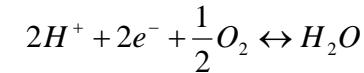
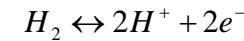
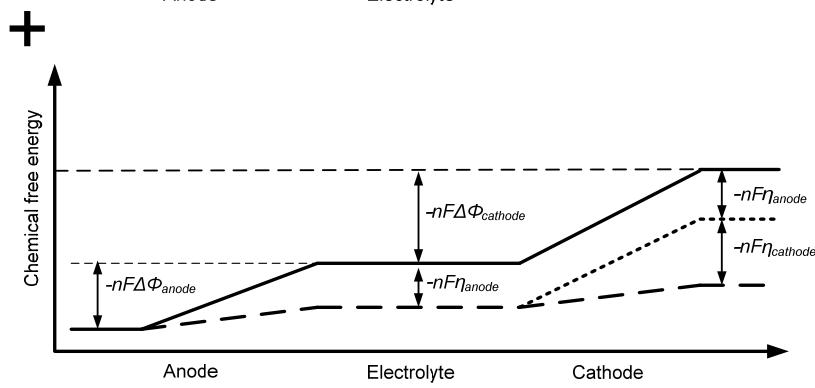


Oxygen dissociation

Anode and Cathode



$$j = j_0 \left(\prod \left(\frac{C_{R,i}^*}{C_{R,i}^{0*}} \right)^{v_i} \exp(\alpha nF\eta / (RT)) - \prod \left(\frac{C_{P,i}^*}{C_{P,i}^{0*}} \right)^{v_i} \exp(-(1-\alpha)nF\eta / (RT)) \right)$$



$$j^A = j_0^A \left(\frac{C_{H_2}^{*,A}}{C_{H_2}^{0*,A}} \exp(2\alpha^A F\eta^A / (RT)) - \left(\frac{C_{H^+}^{*,A}}{C_{H^+}^{0*,A}} \right)^2 \left(\frac{C_{e^-}^{*,A}}{C_{e^-}^{0*,A}} \right)^2 \exp(-2(1-\alpha^A)F\eta^A / (RT)) \right)$$

$$j^C = j_0^C \left(\left(\frac{C_{H^+}^{*,C}}{C_{H^+}^{0*,C}} \right)^2 \left(\frac{C_{e^-}^{*,C}}{C_{e^-}^{0*,C}} \right)^2 \left(\frac{C_{O_2}^{*,C}}{C_{O_2}^{0*,C}} \right)^{\frac{1}{2}} \exp(2\alpha^C F\eta^C / (RT)) - \frac{C_{H_2O}^{*,C}}{C_{H_2O}^{0*,C}} \exp(-2(1-\alpha^C)F\eta^C / (RT)) \right)$$

$$j^A = j^C = j$$

Anode and Cathode at Equilibrium

$$0 = j_0^A \left(\frac{C_{H_2}^{*,A}}{C_{H_2}^{0*,A}} \exp\left(2\alpha F \eta^A / (RT)\right) - \left(\frac{C_{H^+}^{*,A}}{C_{H^+}^{0*,A}} \right)^2 \left(\frac{C_{e^-}^{*,A}}{C_{e^-}^{0*,A}} \right)^2 \exp\left(-2(1-\alpha^A) F \eta^A / (RT)\right) \right)$$

$$\frac{C_{H_2}^{*,A}}{C_{H_2}^{0*,A}} \exp\left(2\alpha F \eta^A / (RT)\right) = \left(\frac{C_{H^+}^{*,A}}{C_{H^+}^{0*,A}} \right)^2 \left(\frac{C_{e^-}^{*,A}}{C_{e^-}^{0*,A}} \right)^2 \exp\left(-2(1-\alpha^A) F \eta^A / (RT)\right)$$

$$\log\left(\frac{C_{H_2}^{*,A}}{C_{H_2}^{0*,A}}\right) + \frac{2\alpha^A F \eta^A}{RT} = \log\left(\frac{C_{H^+}^{*,A}}{C_{H^+}^{0*,A}}\right)^2 + \log\left(\frac{C_{e^-}^{*,A}}{C_{e^-}^{0*,A}}\right)^2 - \frac{2(1-\alpha^A) F \eta^A}{RT}$$

$$\frac{2F\eta^A}{RT} = -\log\left(\frac{C_{H_2}^{*,A}}{C_{H_2}^{0*,A}}\right) + \log\left(\frac{C_{H^+}^{*,A}}{C_{H^+}^{0*,A}}\right)^2 + \log\left(\frac{C_{e^-}^{*,A}}{C_{e^-}^{0*,A}}\right)^2$$

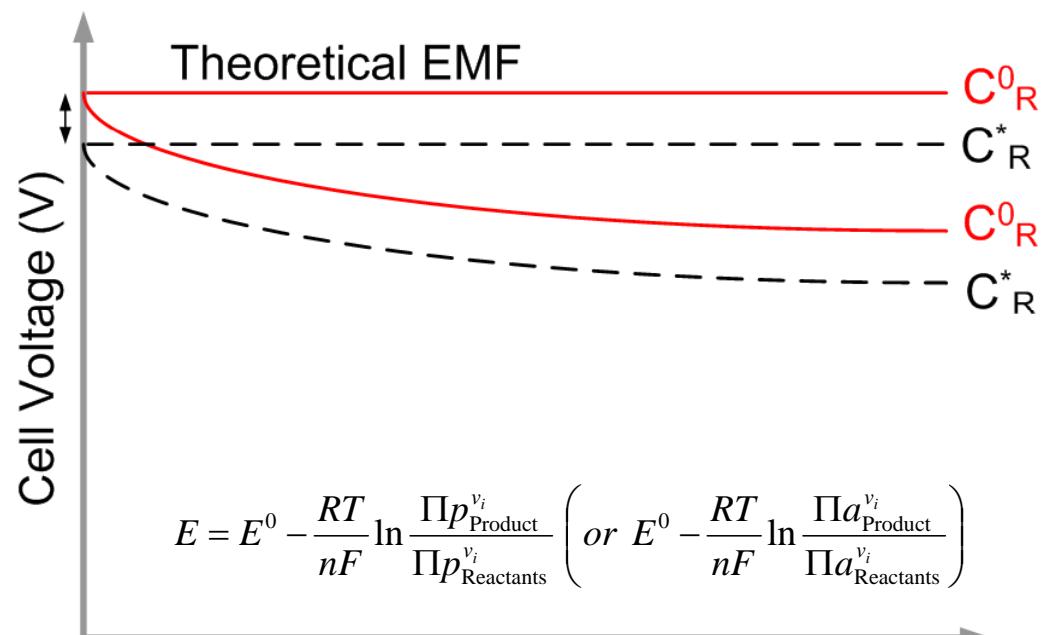
$$\eta^A = \frac{RT}{2F} \left(-\log(a_{H_2}^{*,A}) + \log(a_{H^+}^{*,A})^2 + \log(a_{e^-}^{*,A})^2 \right)$$

$$\eta^C = \frac{RT}{2F} \left(-\log(a_{H^+}^{*,C})^2 - \log(a_{e^-}^{*,C})^2 - \log(a_{O_2}^{*,C})^{\frac{1}{2}} + \log(a_{H_2O}^{*,C}) \right)$$

$$\eta^A + \eta^C = \frac{RT}{2F} \left(\log \frac{a_{H_2O}^{*,C}}{a_{H_2}^{*,A} (a_{O_2}^{*,A})^{\frac{1}{2}}} - \log \left(\frac{a_{H^+}^{*,C}}{a_{H^+}^{*,A}} \right)^2 - \log \left(\frac{a_{e^-}^{*,C}}{a_{e^-}^{*,A}} \right)^2 \right)$$

$$\eta^A + \eta^C = E^0 - E$$

$$\therefore E = E^0 - \frac{RT}{2F} \left(\log \frac{a_{H_2O}^{*,C}}{a_{H_2}^{*,A} (a_{O_2}^{*,A})^{\frac{1}{2}}} - \log \left(\frac{a_{H^+}^{*,C}}{a_{H^+}^{*,A}} \right)^2 - \log \left(\frac{a_{e^-}^{*,C}}{a_{e^-}^{*,A}} \right)^2 \right)$$



Current Density (A/cm^2)

$$j = j_0 \left(\prod \left(\frac{C_{R,i}^*}{C_{R,i}^{0*}} \right)^{v_i} \exp(\alpha n F \eta / (RT)) - \prod \left(\frac{C_{P,i}^*}{C_{P,i}^{0*}} \right)^{v_i} \exp(-(1-\alpha) n F \eta / (RT)) \right)$$