Phase equilibrium basics



What was the "equilibrium?"

- Mechanical equilibrium
 - $-F_1 = F_2$
 - Difference in force \rightarrow difference in potential energy \rightarrow movement
- Mechanical equilibrium
 - $P_1 = P_2$
 - Difference in pressure \rightarrow difference in potential energy \rightarrow flow
- Thermal equilibrium
 - $-T_1=T_2$
 - Difference in temperature \rightarrow difference in thermal energy \rightarrow heat flow

Phase equilibrium

Looks like no change from one phase to another phase (ex: liquid → vapor)



Phase Equilibrium for pure substance





Phase Equilibrium for pure substance

Let's imagine an unstable state



 $P_{H_2O} < P_{H_2O}^{sat} = 2.34 \, kPa$



- For pure substance, saturation pressure is
 - P at which a pure substance boils at a given T.
 - P exerted by the vapor that escapes from the liquid at a given T.
 - P at which vaporization rate is same as condensation rate.
 - P at phase equilibrium

Phase Equilibrium for pure substance

Let's imagine an unstable state



 $P_{H_20}(=1 \ kPa) < P_{H20}^{sat}(=2.34 \ kPa)$



 $P_{H_2O} < P_{H2O}^{sat} = 2.34 \ kPa$



 $P_{H_20} = 2.34 \ kPa = P_{H_20}^{sat}$







$$\begin{array}{l} dU = \delta Q + \delta W = \delta Q - P dV \\ dH = d(U + PV) = dU + P dV + V dP = \delta Q + V dP \\ \text{With constant P,} \\ dH = \delta Q \\ 0 \ge dH - T dS \\ \text{From 2^{nd} law,} \\ dS \ge \frac{\delta Q_{rev}}{T} \\ \end{array} \quad \begin{array}{l} 0 \ge d(H - TS) = dG \end{array}$$

 \rightarrow Gibbs Energy must go to decreasing way, to the minimum point.

- \rightarrow Spontaneous change
- \rightarrow For equilibrium, dG=0



 n^{α}

 n^{β}



$$dG = d(g^{\alpha}n^{\alpha} + g^{\beta}n^{\beta}) \le 0$$
$$= g^{\alpha}dn^{\alpha} + g^{\beta}dn^{\beta} \le 0$$
$$dn^{\beta} = -dn^{\alpha}$$
$$dG = (g^{\alpha} - g^{\beta})dn^{\alpha} \le 0$$

If
$$g^{\alpha} > g^{\beta}$$
, $dn^{\alpha} \le 0$
 $dn^{\alpha} < 0 \rightarrow \text{only } \beta \text{ exists}$

If
$$g^{\alpha} < g^{\beta}$$
, $dn^{\alpha} \ge 0$
 $dn^{\alpha} > 0 \rightarrow \text{only } \alpha \text{ exists}$

→Phase equilibrium is possible at $g^{\alpha} = g^{\beta}$ only Chemical potential $\mu = g$



• Ex)
$$g^{\alpha} > g^{\beta}$$

- If $g^{\alpha} = 2 \text{ J/mol}, g^{\beta} = 1 \text{ J/mol}, n^{\alpha} = 1 \text{ mol}, n^{\beta} = 1 \text{ mol}$
 $G = g^{\alpha}n^{\alpha} + g^{\beta}n^{\beta} = 2 \cdot 1 + 1 \cdot 1 = 3 \text{ J}$
- If $(dn^{\alpha} = 0) \rightarrow \text{G}=3$
- If $(dn^{\alpha} = 0.1)$
 $G = g^{\alpha}n^{\alpha} + g^{\beta}n^{\beta} = 2 \cdot 1.1 + 1 \cdot 0.9 = 3.1 \text{ J}$
- If $(dn^{\alpha} = -0.1)$
 $G = g^{\alpha}n^{\alpha} + g^{\beta}n^{\beta} = 2 \cdot 0.9 + 1 \cdot 1.1 = 2.9 \text{ J}$
 $\Rightarrow \text{Condensation to when } G = 2 \cdot 0 + 1 \cdot 2 = 21 \text{ (minimum)}$



dg = vdP - sdT

With constant T,

$$\left(\frac{\partial g}{\partial P}\right)_T = v$$







