

Lecture Note #4

Adsorption & desorption at solid surfaces

Reading: Shaw, ch. 5

I. Adsorption: basic concepts

1. Physisorption vs. Chemisorption

Physisorption

- Van der Waals interaction
- Small adsorption energy: ≤ 20 kJ/mole
- Similar to condensation
- Multilayer adsorption possible
- No charge transfer
- Substrate non-specific

Chemisorption

- Chemical bonding
- Large adsorption energy: ≥ 200 kJ/mole
- Charge transfer : work function change
- Limited to a monolayer
- Substrate specific
- Gas specific

Synoptic table 25.1* Maximum observed enthalpies of physisorption

Adsorbate	$\Delta_{\text{ad}}H^\ominus/(\text{kJ mol}^{-1})$
CH ₄	-21
H ₂	--10
H ₂ O	-59
N ₂	-21

Synoptic table 25.2* Enthalpies of chemisorption, $\Delta_{\text{ad}}H^\ominus/(\text{kJ mol}^{-1})$

Adsorbate	Adsorbent (substrate)		
	Cr	Fe	Ni
CH ₄	-427	-285	-243
CO		-192	
H ₂	-188	-134	
NH ₃		-188	-155

Terminology

- Adsorption site density

$$N_s = \# \text{ of sites } / \text{cm}^2 \sim 10^{15} / \text{cm}^2$$

- Coverage

$$\text{fractional coverage } \theta = N_s / N$$

$$\text{saturation coverage : } \theta_s = 1$$

- Wall collision rate Z_w

$$Z_w = \# \text{ molecules striking a surface } / \text{cm}^2 \cdot \text{s}$$

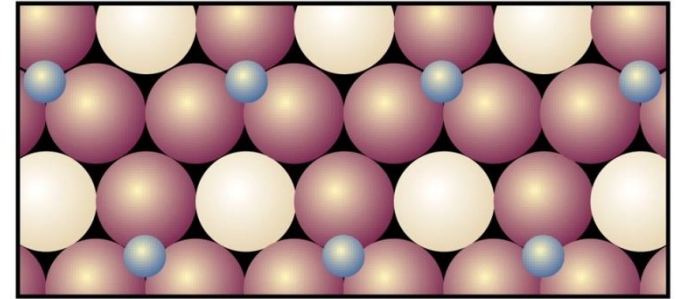
$$Z_w = P / (2\pi mkT)^{1/2} \sim 10^{15} \text{ molecules } / \text{cm}^2 \cdot \text{s}$$

@ 10^{-6} Torr and 298 K

$$1 \text{ L (Langmuir)} = 10^{-6} \text{ Torr} \cdot \text{s of gas exposure.}$$

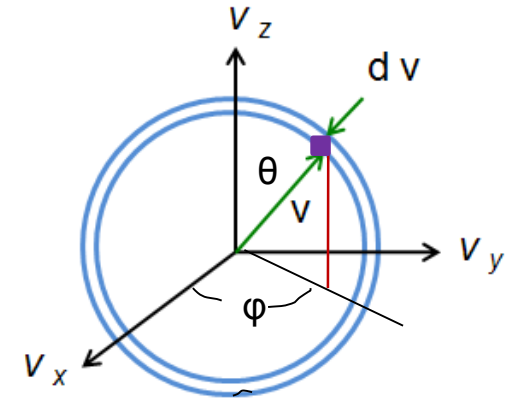
$$Z_w = \int \int \mathcal{N} f(v) v \cos \theta dS dv d\Omega / dS$$

- Monolayer completion time $\sim 1 \text{ sec @ } 10^{-6} \text{ Torr}$

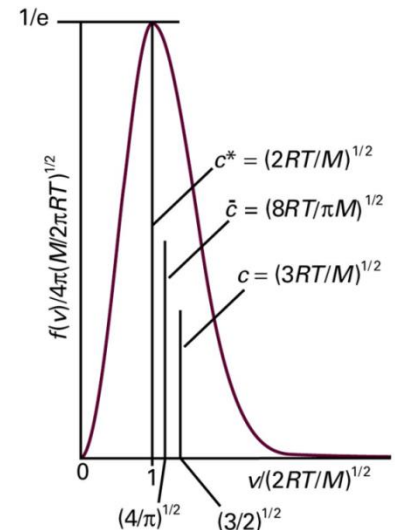


Another way to obtain $f(v)dv$

- Consider 1D velocity distribution $f_x(v_x)dv_x$
- $\epsilon = \frac{1}{2} m v_x^2$ is non-degenerate, so $g = 1$ for all v_x
- According to the Boltzmann distribution law,
 $f_x(v_x)dv_x = (m/2\pi kT)^{1/2} \exp(-\frac{1}{2} m v_x^2 / kT) dv_x$
 cf: $\int_{-\infty}^{\infty} \exp(-\frac{1}{2} m v_x^2 / kT) dv_x = (2\pi kT/m)^{1/2}$
- $\langle v_x \rangle = (2kT/\pi m)^{1/2}$
- $f_x(v_x)$, $f_y(v_y)$, and $f_z(v_z)$ are independent with one another and have the same function.
- $f_x(v_x) f_y(v_y) f_z(v_z) dv_x dv_y dv_z$
 $= (m/2\pi kT)^{3/2} \exp \{-\frac{1}{2} m(v_x^2 + v_y^2 + v_z^2)/kT\} dv_x dv_y dv_z$
- Expressing it in polar coordinate (v, θ, ϕ) ,
 $f(v, \theta, \phi) dv d\theta d\phi = (m/2\pi kT)^{3/2} \exp(-\frac{1}{2} m v^2 / kT) v^2 dv \sin\theta d\theta d\phi$
- Integrating over $d\theta$ and $d\phi$,
 $f(v) dv = 4\pi (m/2\pi kT)^{3/2} \exp(-\frac{1}{2} m v^2 / kT) v^2 dv$
 $= 4\pi (M/2\pi RT)^{3/2} \exp(-\frac{1}{2} m v^2 / kT) v^2 dv$; text eq. (20.4)
- Mean speed** $\bar{c} = \langle v \rangle = \int_0^\infty v f(v) dv = (8RT/\pi M)^{1/2}$
- Most probable speed** $c^* = (2RT/M)^{1/2}$; $df/dv|_{v=c^*} = 0$
- Root mean square speed** $c_{rms} = (\langle v^2 \rangle)^{1/2} = (3RT/M)^{1/2}$



velocity space



2. Kinetics of Adsorption

Langmuir model assumes that

- Uniform adsorption site
- Adsorption energy independent of θ
- No surface diffusion

$M(g) + * \rightarrow M(ad)$: non-dissociative

$$d\theta/dt = k_a(1 - \theta) : k_a = Z_w s_0 / N_s = k_a p$$

s_0 = initial sticking probability

$$s(\theta) = s_0 (1 - \theta)$$

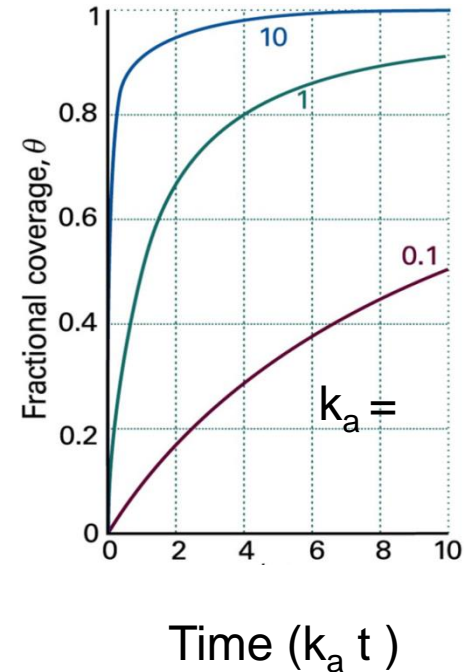
$$\theta(t) = 1 - \exp(-k_a t)$$

$A_2 + 2* \rightarrow 2 A(ad)$: dissociative adsorption

$$d\theta/dt = k_a(1 - \theta)^2 : k_a = 2 Z_w s_0 / N_s$$

$$s(\theta) = s_0 (1 - \theta)^2$$

$$\theta(t) = k_a t / (1 + k_a t)$$



3. Reversible adsorption

Adsorption-desorption equilibrium



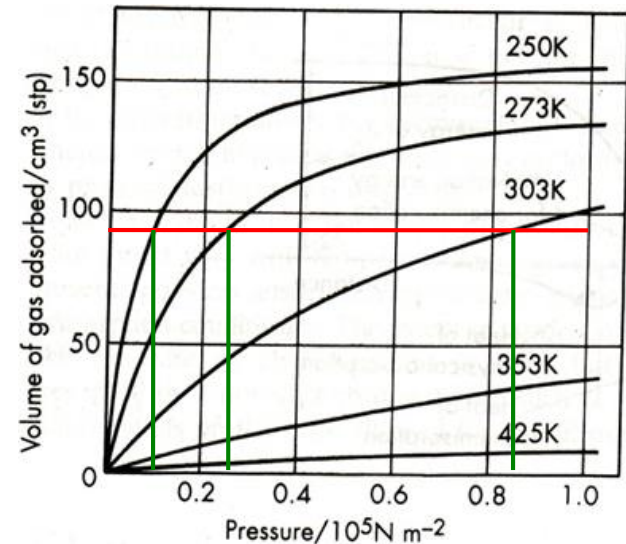
- $d\theta/dt = k_a P(1 - \theta) - k_d \theta$
at equilibrium, $d\theta/dt = 0$.
- The desorption rate constant
 $k_d = k_d^0 \exp(-E_d/RT)$:
- At equilibrium, $d\theta/dt = 0$.

$$\theta = \frac{K(T) p}{1 + K(T) p},$$

where $K = k_a / k_d$: equilibrium constant.

- As $p \rightarrow \infty$, $\theta \rightarrow 1$
- θ - P plot at constant T is called **Langmuir isotherm**.
- As seen in the Fig., the coverage θ depends **more sensitively** on **T** than on **p** .

NH_3 / charcoal



4. Measurement of adsorption isotherm

Volumetric measurement

$$\theta = K(T)p / \{1 + K(T)p\}$$

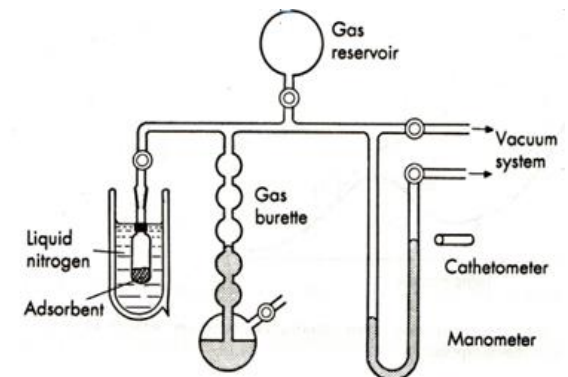
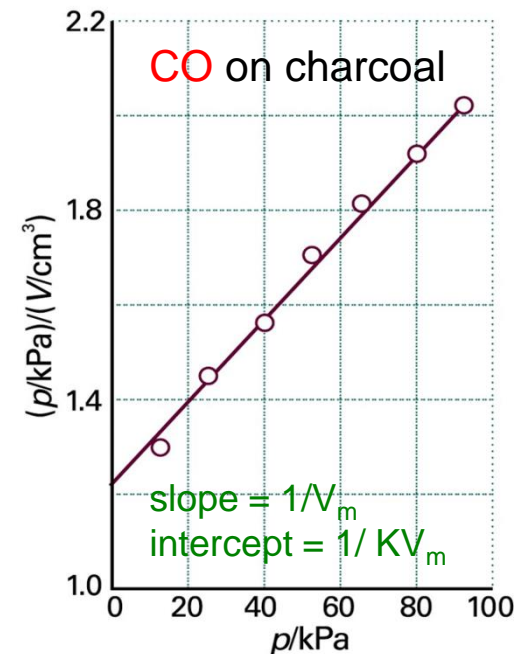
$\theta = p/V_m$ measured as a volume change,
where V is the volume of gas adsorbed
and V_m is the saturation volume.

$$V/V_m = Kp / (1 + Kp),$$

$$P/V = (1 + Kp)/K V_m = p/V_m + 1/KV_m$$

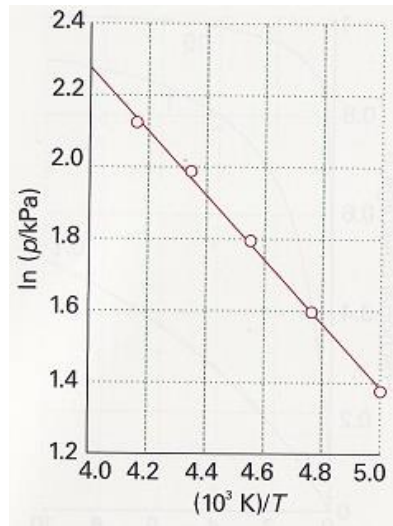
p/V vs. p plot gives a straight line.

Slope = $1/V_m$ and intercept = $1/KV_m$

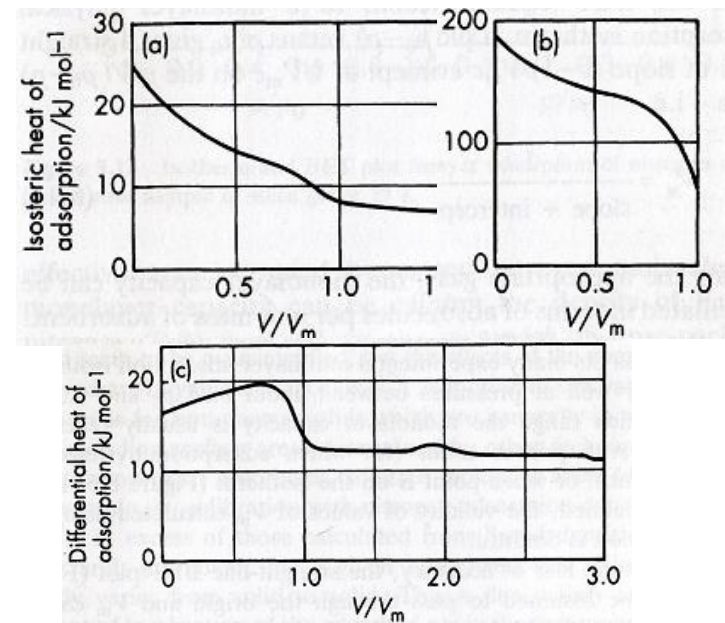


Isosteric enthalpy(heat) of adsorption

- $dG = Vdp - SdT$, and $d(\Delta G) = \Delta Vdp - \Delta S dT$ for any change
- At equilibrium, $\Delta Vdp - \Delta SdT = 0$.
- $\Delta V = V_{ad} - V_g \sim -nRT/p$
- $(\partial p / \partial T)_\theta = \Delta S / \Delta V = -(\Delta H/T)/(nRT/p) = -p \Delta H/nRT^2$ **at constant θ .**
- $d \ln p = (\Delta H_m/R) d(1/T) \rightarrow$ The slope of $(\ln p) - (1/T)$ plot gives $\Delta H_m/R$
- In genera, Δh_{ad} is coverage-dependent because of
 - 1) **Heterogeneity** of the adsorption sites
 - 2) **Lateral interaction** between adjacent adsorbates



CO on charcoal
 $\Delta H_m = -7.52 \text{ kJ/mol}$



- Physisorbed N_2 on rutile TiO_2 at 85 K
- Chemisorbed H on W
- Physisorbed Kr on graphitized carbon black

Sticking probability

- Sticking probability

$s = \# \text{ molecules adsorbed} / \# \text{ molecules impinging on a surface}$

- Molecular beam method, in which the partial pressure change is monitored with a QMS.

TABLE 5.1 Some Typical Values of the Initial Sticking Probability at 300 K (Chemisorption)

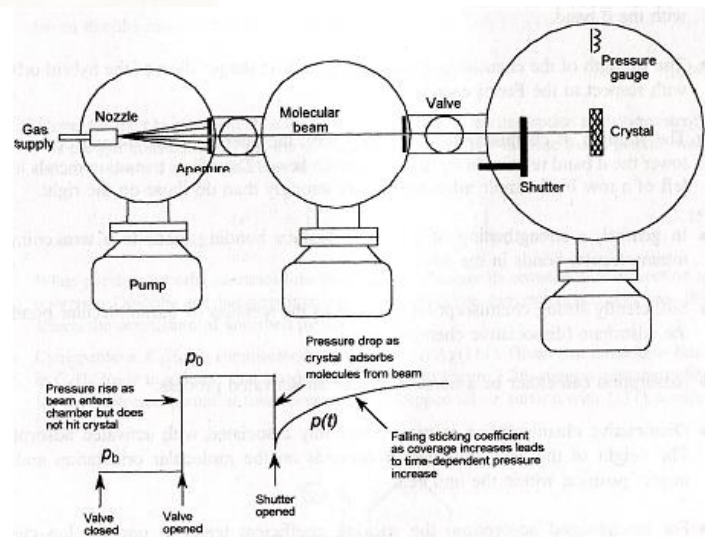
Gas	Surface	$S(0)$	Gas	Surface	$S(0)$
H ₂	Ni(100)	0.06	N ₂	W(320)	0.7
H ₂	Ni(111)	0.02	N ₂	W(110)	$< 3 \times 10^{-3}$
H ₂	Pt(110)	0.2	Ga	GaAs(100)-B	1.0
H ₂	Si(100)	$< 10^{-4}$	As ₄	GaAs(100)-B	$< 10^{-3}$
CO	Pt(111)	0.67	As ₄	GaAs(100)-A	0.5

Data taken from Morris et al. [1984] and Joyce and Foxton [1984].

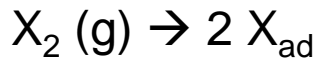
$$s(t) = \frac{p_0 - p(t)}{p_0 - p_b}$$

Factors influencing s_0 in chemisorption

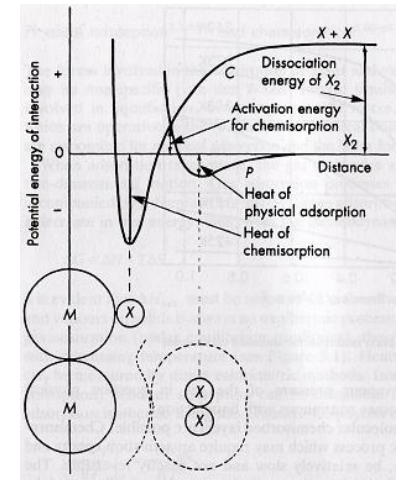
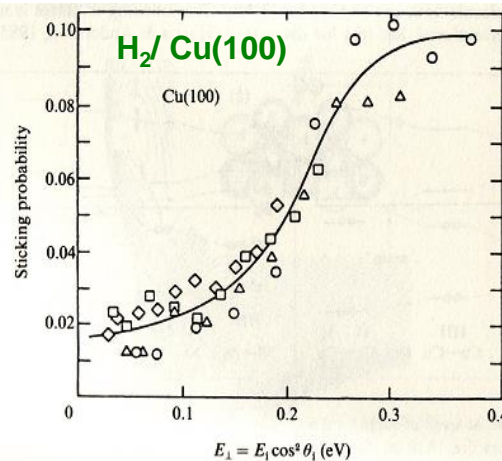
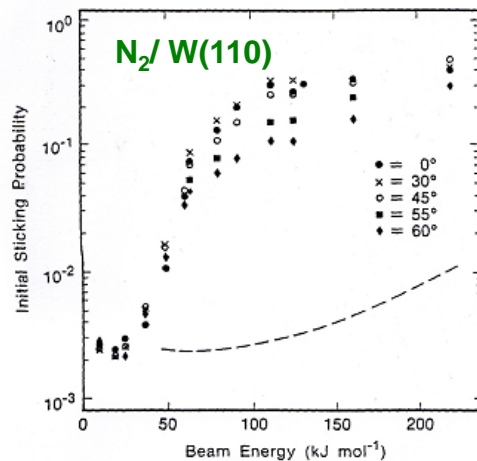
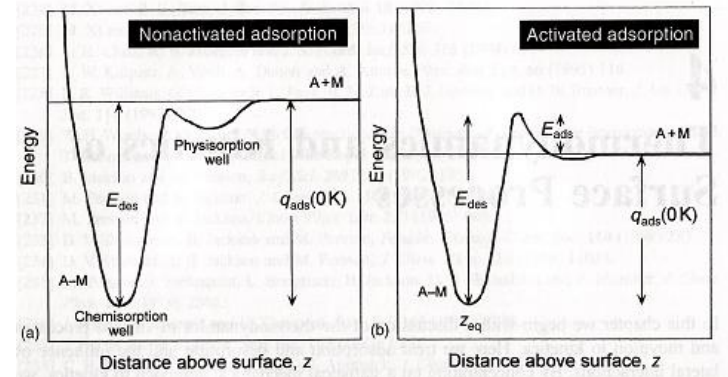
- Gas- surface combination
- Efficiency of energy transfer in gas-surface collisions
- Surface orientation of the surface for a given single crystal material
- Presence of an energy barrier for dissociative adsorption: **activated adsorption**



5. Activated adsorption

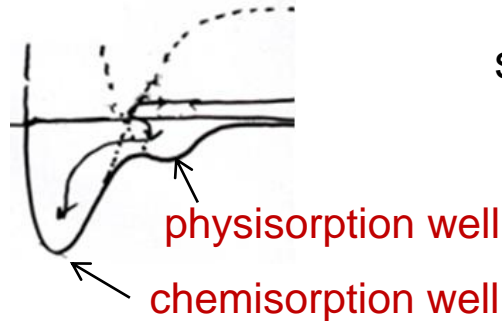
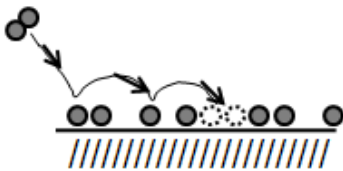


- Important process in heterogeneous catalysis
- **Very small s_0** due to the presence of an adsorption barrier
- A fast N_2 can overcome the barrier to directly populate the atomic state.
- **A large kinetic energy dependence of s_0**

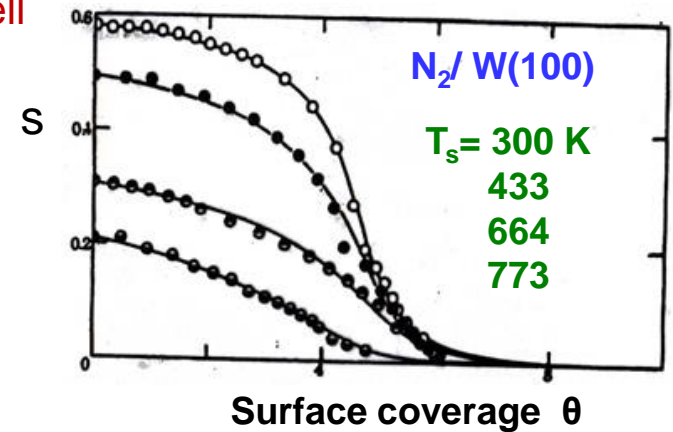
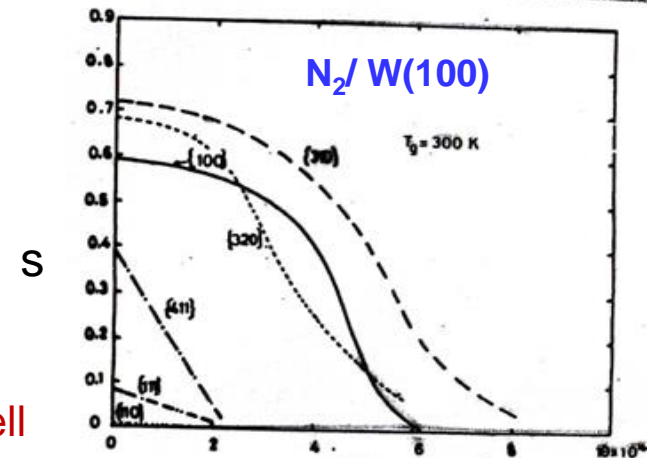


6. Precursor-controlled adsorption

- Marked deviation from Langmuir adsorption
Langmuir adsorption; $s = s_0 (1 - \theta)^2$
- Coverage-insensitive s .
- Decrease in s with increasing T_s : re-evaporation of the precursor state.

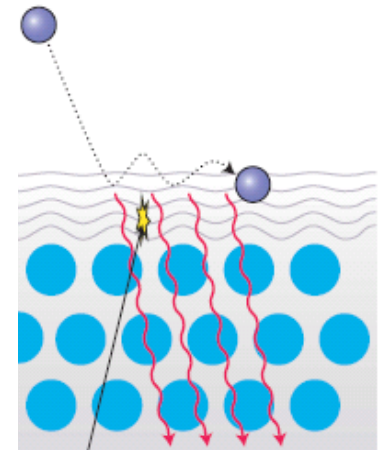
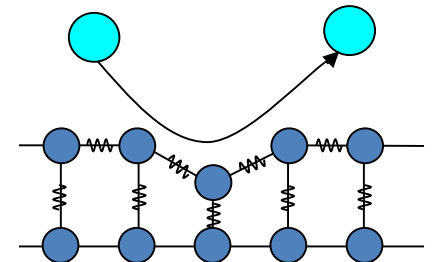
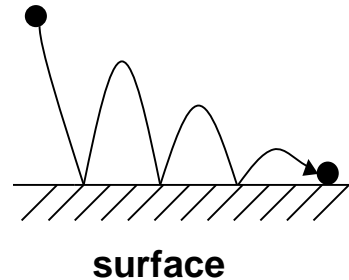
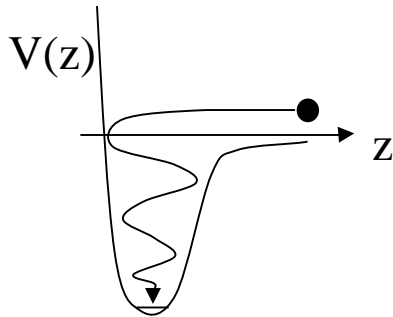


- Trapping in the physisorption well
- Precursor hopping on the surface to find an empty site
→ increase in s
- Re-evaporation of the precursor due to a finite surface lifetime τ ; $\tau = \tau_0 \exp(-E_d/RT)$



II. Adsorption dynamics

- The outcome of the gas-surface collisions;
 - 1) **Trapping**: becoming a bound state after the 1st collision
 - 2) Direct reflection to the gas phase
- The **trapping probability** is determined by the amount of the **energy transfer** to the surface.
- Energy transfer occurs via **multiphonon** excitations.



Phonons
Electron-hole pair excitation?

TABLE 5.1 Some Typical Values of the Initial Sticking Probability at 300 K

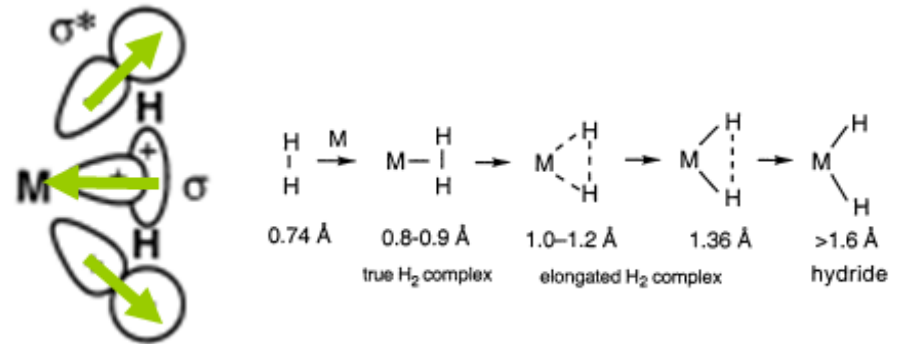
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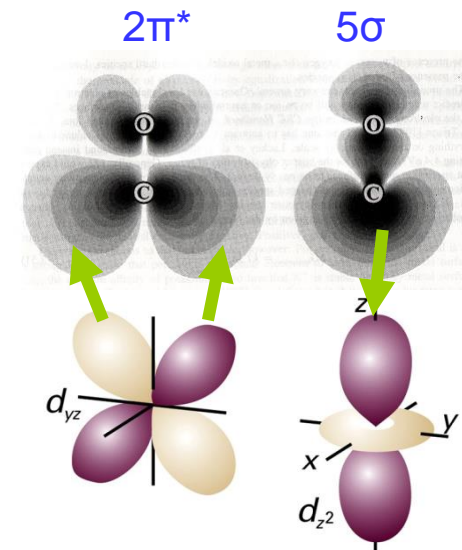
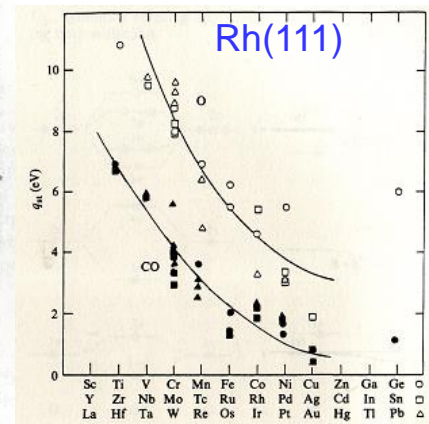
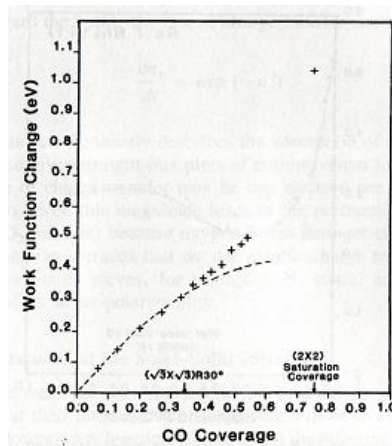
Chemisorption bonding of H_2 and $CO(NO)$

- Charge transfer : work function change
- e^- donation + backdonation
- Orbital symmetry
- Transition metal : d-band metal
- Noble metal: sp-band metal
- Heat of adsorption: bond strength
- Dissociation
- Activated adsorption

Kubas interaction



Heat of adsorption of CO



III. Desorption

- Reverse process of adsorption
- Thermal desorption by phonon annihilation
- Temperature programmed desorption (TPD)

information available: surface coverage,
desorption kinetics, adsorption energy,

Desorption rate

$$d\theta/dt = k_d \theta^n$$

$n = 0$: 0th-order desorption

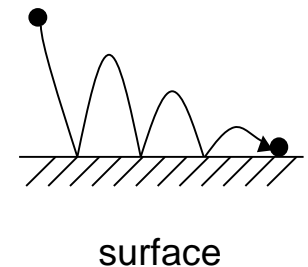
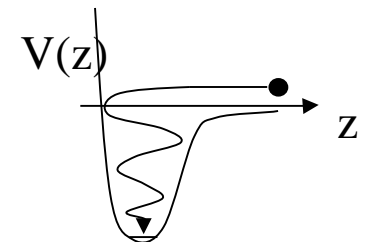
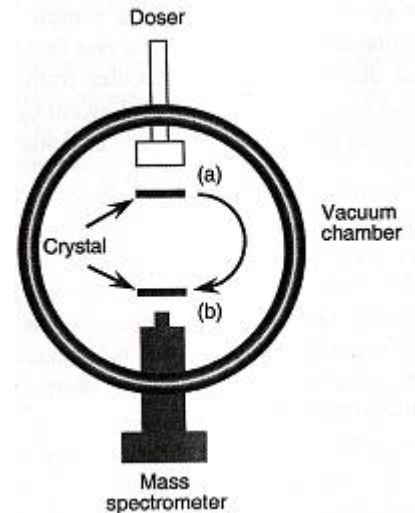
$n = 1$: 1th-order desorption : $M(ad) \rightarrow M(g)$

$n = 2$: 2th-order desorption : $2 A(ad) \rightarrow A_2 (g)$

$$k_d = k_d^0 \exp(- E_{des} / RT)$$

$T = T_0 (1 + \beta t)$, where the

heating rate $\beta = 0.1 \sim 10$ K/s



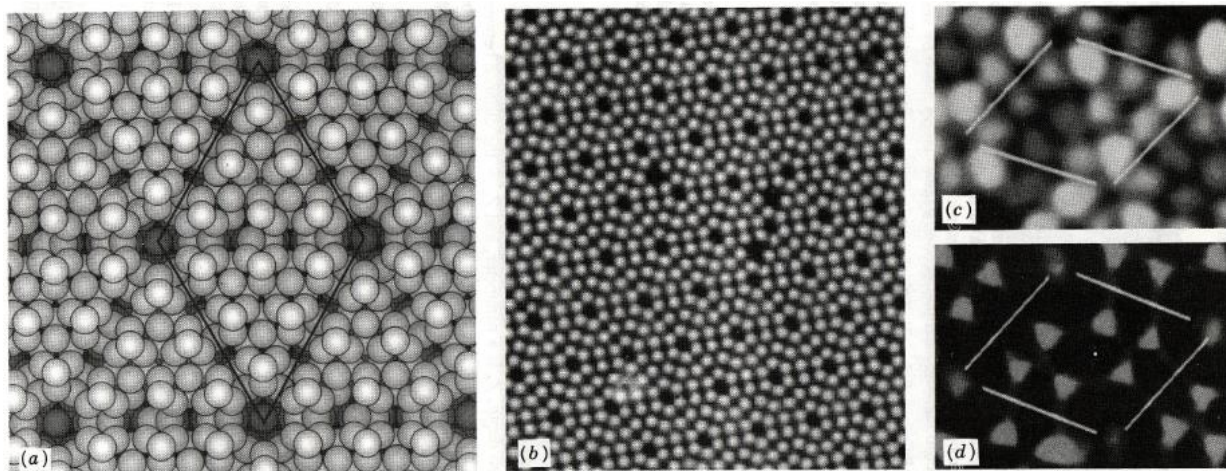


Figure 2.47 (a) A schematic of the (7x7) reconstruction of Si(111). (b) An STM image of the (7x7) surface. (c), (d) Images of the dangling bonds in the (1x1) surface. (From Trump et al. [1988].)

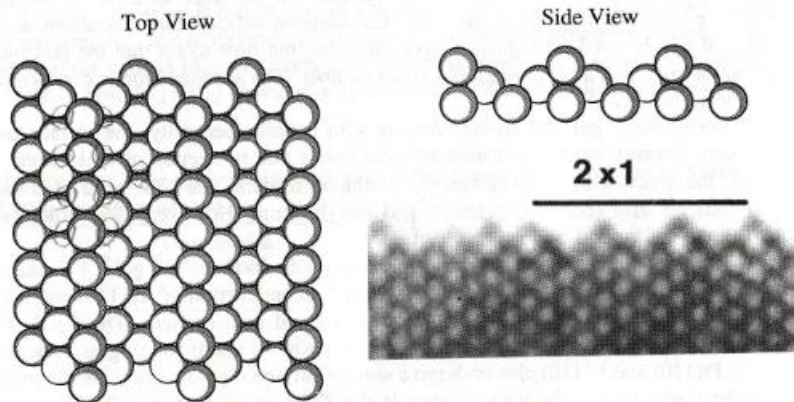
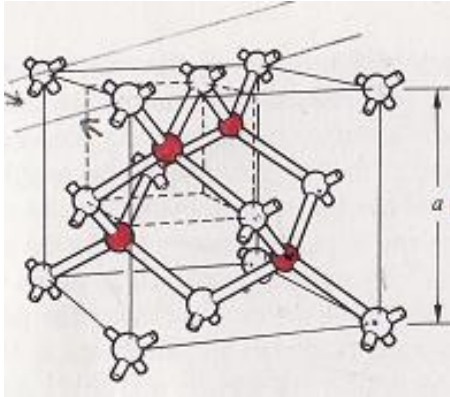
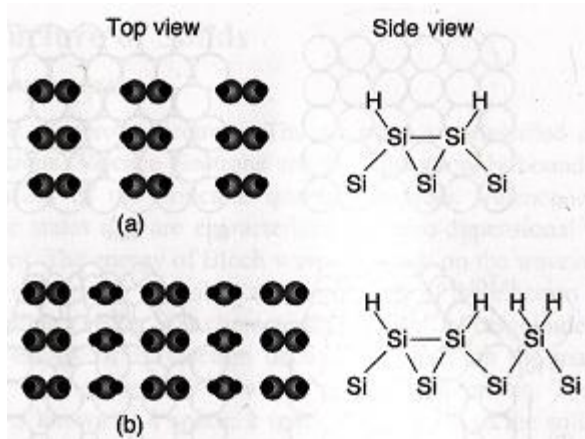


Figure 2.52 A schematic of the (2x1) reconstruction of Au(110) and a TEM image that looks down the surface. (The TEM image is from Marks and Smith [1983]. Reprinted with permission from *Nature* 303, 316 (1983). © 1983 McMillan Magazines Limited.)

1. Example of TPD spectra: H/Si(100)



Unreconstructed Si(100)



saturation β_1 coverage = 6.683×10^{14} H atoms/cm²

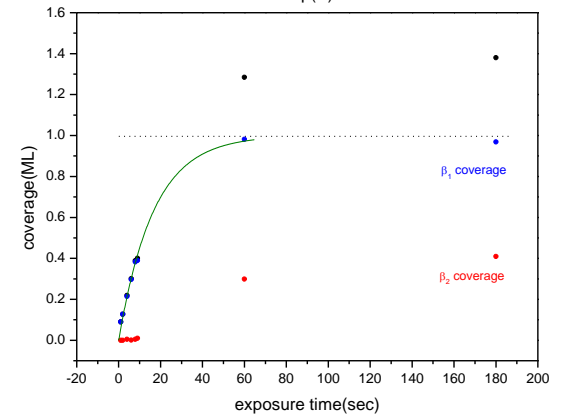
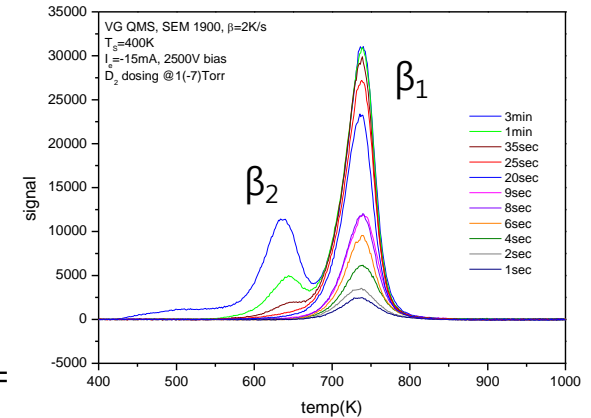
β_1 state

monohydride (1 ML)
(2x1)

β_2 state

dihydride ($1\frac{1}{3}$ ML)
(3x1)

D atom beam dosing



2. Desorption kinetics

A. 0th –order desorption

- $d\theta/dt = k_d = k_d^0 \exp(-E_{\text{des}}/RT)$
- For a multilayer $\theta = 1$.
- Exponential rate increase with $T \rightarrow$ obtain E_{des}

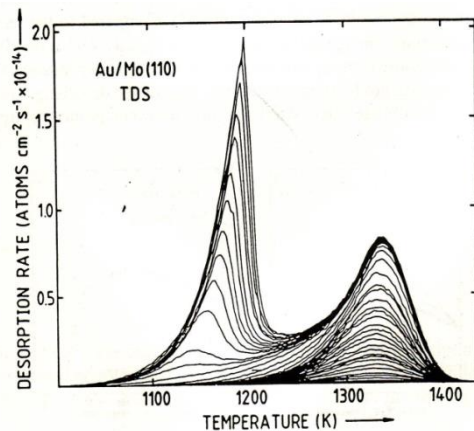
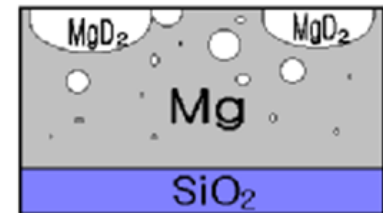
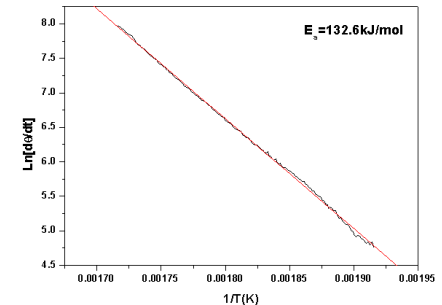
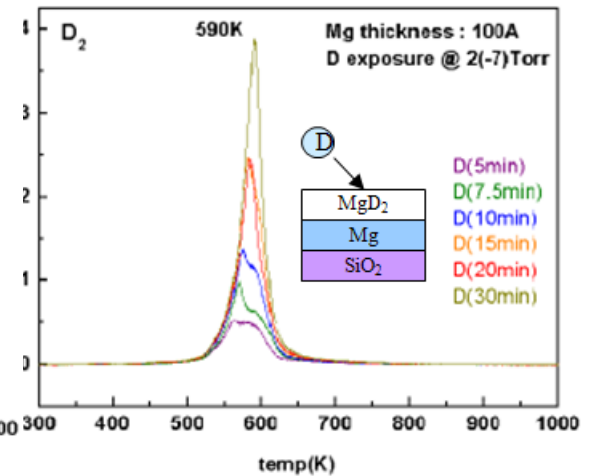
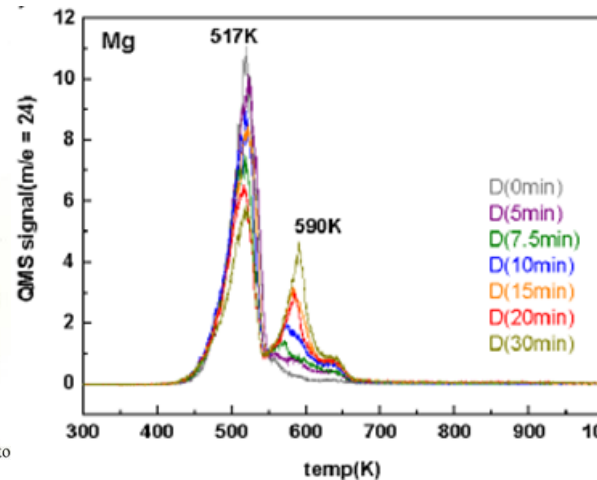


Figure 2 Thermal desorption spectra of Au on Mo(110) in the coverage range from 0 to 2 ML. Heating rate 5.2 K s^{-1}
(Reproduced with permission from *Surf. Sci.*, 1988, **195**, 207)



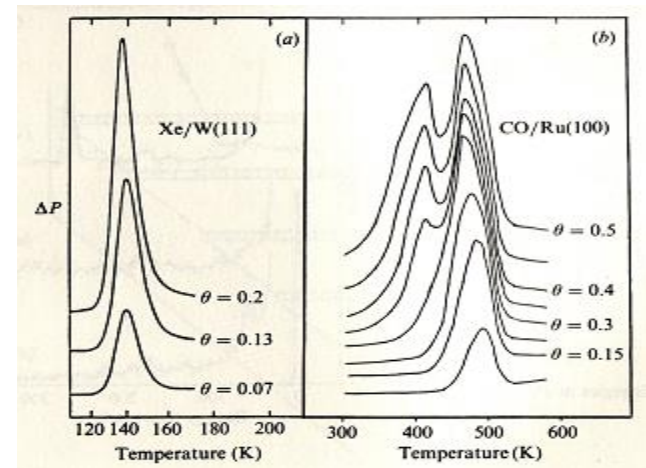
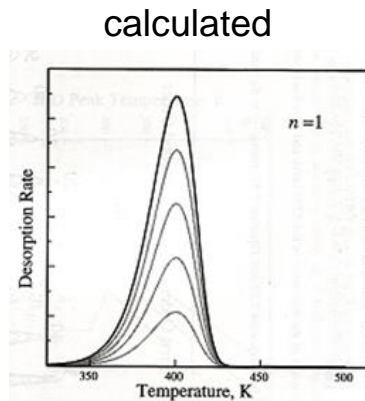
B. 1th –order desorption

- $d\theta/dt = k_d^0 \exp(-E_{\text{des}}/RT) \theta$
- The peak temperature is coverage-independent
- Asymmetric peak shape

$$E_{\text{des}} = RT_p \left[\ln \left(\frac{AT_p}{\beta} \right) - 3.46 \right]$$

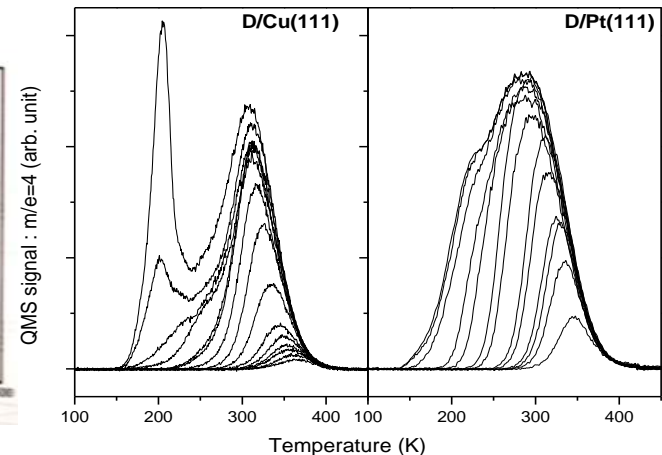
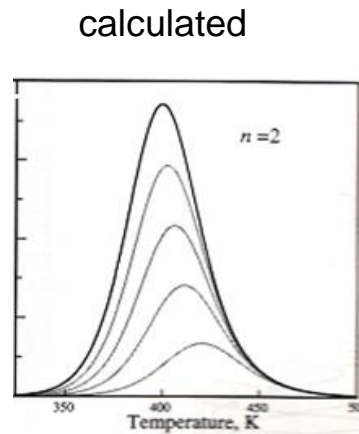
$\sim 31 \text{ kT}_p$

Ex: $T_p = 300 \rightarrow E_{\text{des}} = 0.81 \text{ eV}$.



C. 2th –order desorption

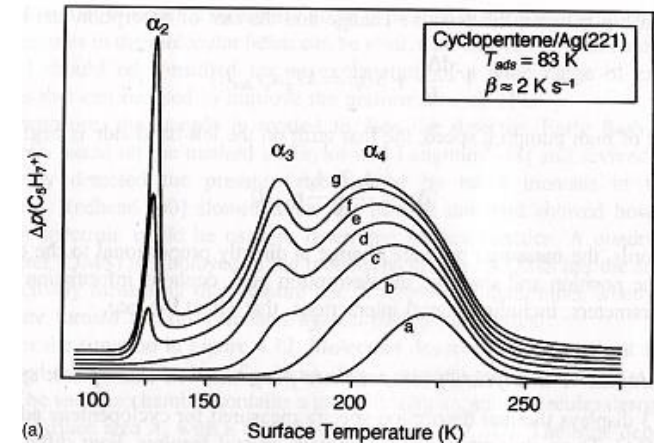
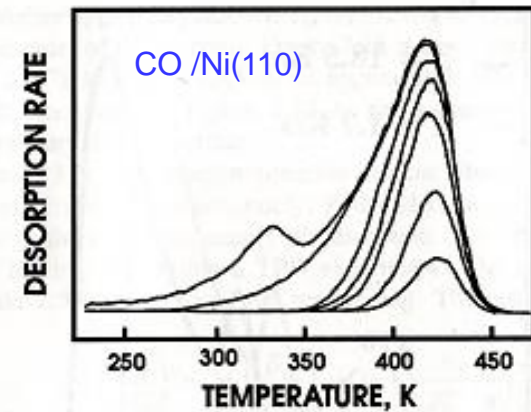
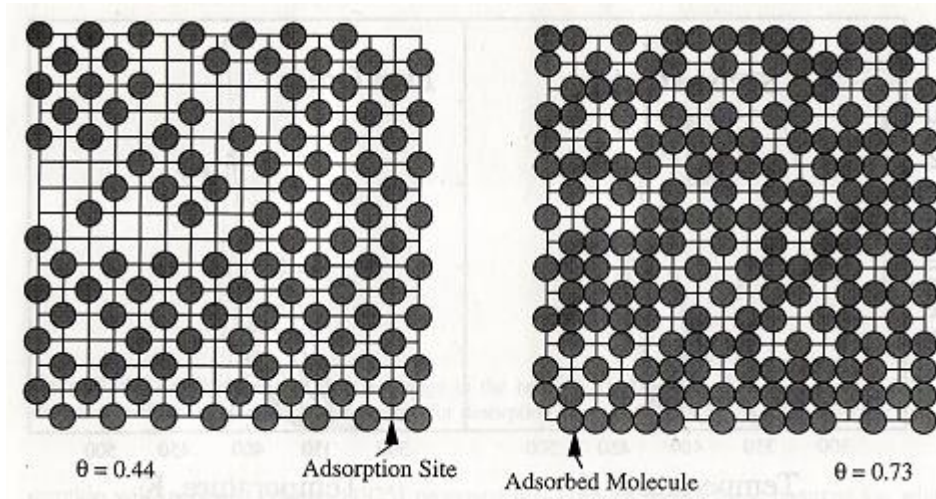
- $d\theta/dt = k_d^0 \exp(-E_{\text{des}}/RT) \theta^2$
- Peak shift to a lower T with increasing coverage
- Almost-symmetric peak



3. Deviation from simple kinetic theory

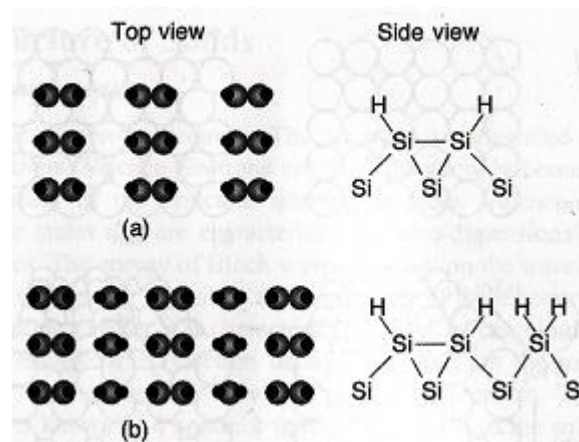
1) Adsorbate-adsorbate interaction

- Repulsive or attractive interaction.
- E_{des} is coverage-dependent.
- Repulsive interaction \rightarrow
- T_p shifts to a lower T with increasing θ .

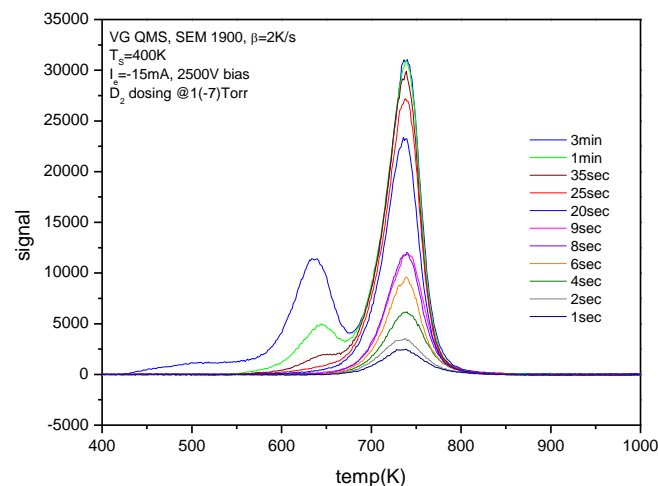


2) Pre-pairing of atoms

- $2 A(\text{ad}) \rightarrow A(\text{ad})-A(\text{ad}) \rightarrow A_2 (\text{g})$
- No direct bonding between $A(\text{ad})$'s.
- Occupy the adjacent sites.
- $2 \text{H}(\text{ad})/\text{Si}(100) \rightarrow \text{H}(\text{ad})-\text{H}(\text{ad}) (\text{pair}) \rightarrow \text{H}_2 (\text{g})$.
- No T_p shift with coverage.
- 2 $\text{H}(\text{ad})$ occupy the Si dimer sites.



β_1 state (1 ML)
monohydride
(2x1)



IV. Adsorption isotherms

1. Brunner clasification

Type I: Langmuir adsorption

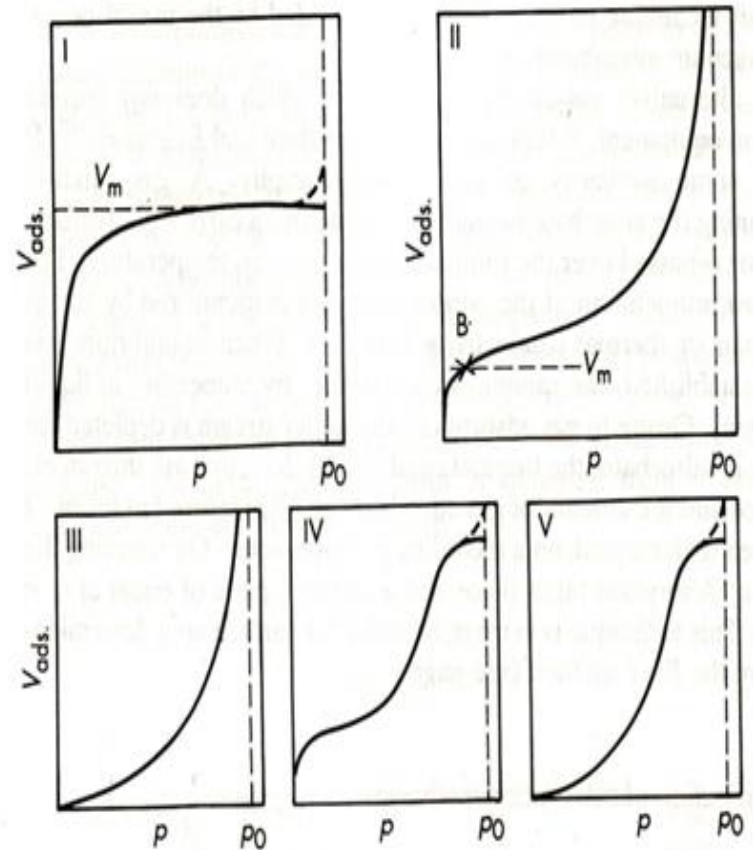
Type II: monolayer + multilayer

Type III: multilayer adsorption

Type IV: Type II

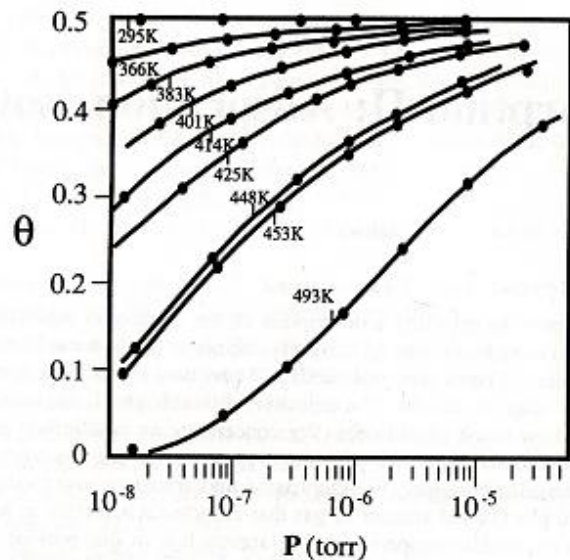
Type V: Type III on a porous adsorbent

- Finite pore volume limits the max. V_{ads} .
- Type II & IV: $\Delta H_{des} \gg \Delta H_{vap}$
- Type III & V: $\Delta H_{des} \sim \Delta H_{vap}$

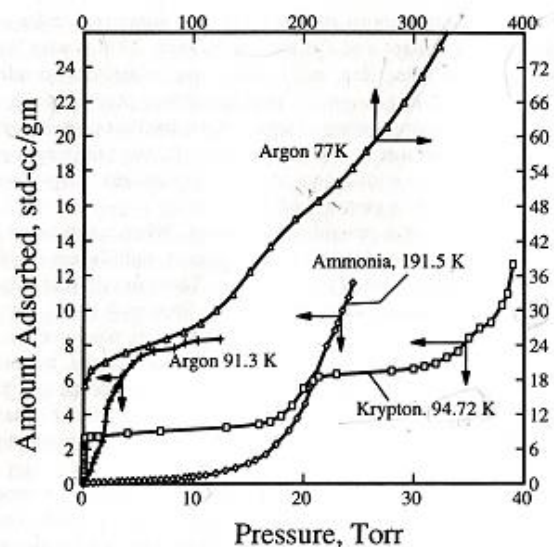


p_0 = saturation vapor pressure

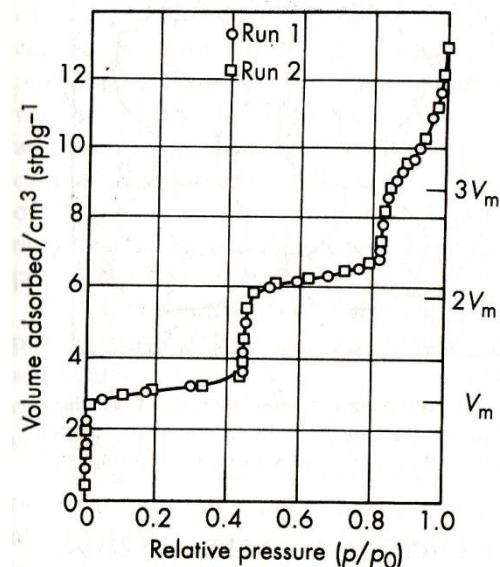
Examples of adsorption isotherms



CO/Pd(111)



Ar, NH₃ /carbon black



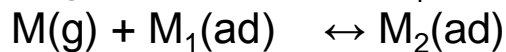
Kr /carbon black

* carbon black graphitized at 3000 K

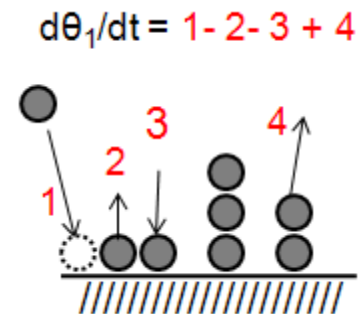
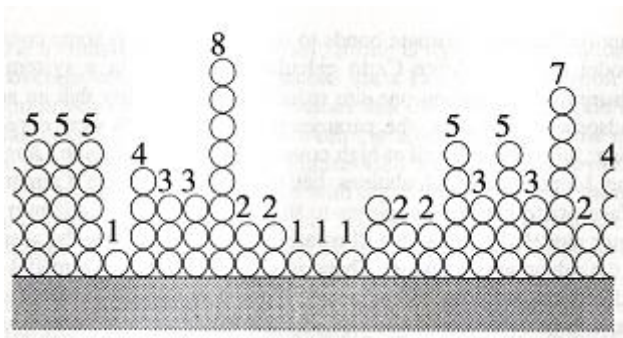
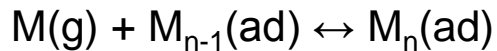
2. Multilayer physisorption

BET isotherm: Brunnauer, Emmett, Teller

- Langmuir adsorption extended to allow multilayer adsorption
- Equilibrium maintained between the adjacent layers
- $\Delta H_{\text{ads}}^{\circ}$ for the first layer and $\Delta H_{\text{vap}}^{\circ}$ for the multilayers
- used for surface area measurements.



....



BET equation

- Extension of Langmuir equation beyond the 1st layer.
- Equilibrium between adjacent layers
- The rate of coverage change for each layer is zero.
- The 1st layer may be chemisorption, but the 2nd layer and beyond are always physisorption → Therefore, different k_a and k_d values may be involved.
- At equilibrium

$$d\theta_0/dt = -k_a p \theta_0 + k_d \theta_1 = 0$$

$$d\theta_1/dt = k_a p \theta_0 - k_d \theta_1 - k'_a p \theta_1 + k'_d \theta_2 = 0$$

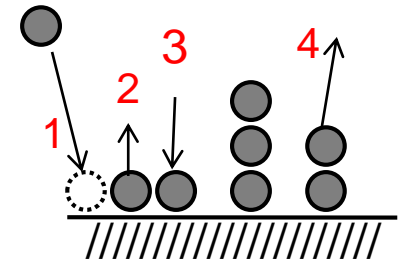
$$d\theta_2/dt = k'_a p \theta_1 - k'_d \theta_2 - k'_a p \theta_2 + k'_d \theta_3 = 0$$

.....

$$d\theta_{n-1}/dt = k'_a p \theta_{n-2} - k'_d \theta_{n-1} - k'_a p \theta_{n-1} + k'_d \theta_n = 0$$

- $k_a = Z_w s_0$, $k_d = v \exp(-\Delta H_{des}/RT)$ for the 1st layer
- $k'_a = Z_w s'_0$, $k'_d = v' \exp(-\Delta H_{eva}/RT)$ for the 2nd layer and beyond.
- For multilayer adsorption $s_0 \sim s'_0$ and $v \sim v'$. Then, $k_a \sim k'_a$.
- But E_{des} can be much larger than E'_{des} , hence k_d much smaller than k'_d .

$$d\theta_1/dt = 1 - 2 - 3 + 4$$



- Let $k_a/k_d = K$, $k'_a/k'_d = K'$, and
 $c = K / K' = (k_a/k_d) / (k'_a/k'_d) \sim k'_d/k_d = \exp(\Delta h_{\text{des}} - \Delta H_{\text{vap}}) / RT$

$$\theta_1 = (k_a/k_d) p \theta_0 = K p \theta_0 = c K' p \theta_0$$

$$\theta_2 = [(k_d + k'_a p) \theta_1 - k_a p \theta_0] / k'_d = (1/c + K' p) \theta_1 - K' p \theta_0 = c(K' p)^2 \theta_0$$

$$\theta_3 = [(k'_d + k'_a p) \theta_2 - k'_a p \theta_1] / k'_d = (1 + K' p) \theta_2 - K' p \theta_1 = c(K' p)^3 \theta_0$$

.....

$$\theta_n = (1 + K' p) \theta_{n-1} - K' p \theta_{n-2} = c(K' p)^{n-1} \theta_0 + (K' p)_n \theta_0 - c(K' p)^{n-1} \theta_0 = c(K' p)^n \theta_0$$

$$(1) \theta_0 + \theta_1 + \dots + \theta_n (n \rightarrow \infty) = 1$$

$$\rightarrow \theta_0 + c K' p [1 + K p + (K' p)^2 + (K' p)^3 + \dots] \theta_0 = 1 \rightarrow \theta_0 [1 + c K' p / (1 - K' p)] = 1$$

$$\rightarrow \theta_0 = 1 / [1 + c K' p / (1 - K' p)] = (1 - K' p) / [1 + (c-1) K' p]$$

$$(2) V/V_m = \theta_1 + 2 \theta_2 + \dots + n \theta_n = c [K' p + 2(K' p)^2 + 3(K' p)^3 + \dots] \theta_0$$

$$= (1 - K' p) c K' p / [1 + (c-1) K' p] (1 - K' p)^2$$

$$\text{cf: } 1 + x + x^2 + \dots = d(x + x^2 + x^3 + \dots) / dx = d[x / (1 - x)] / dx = 1 / (1 - x)^2$$

- When $p = p_0$ (saturation vapor pressure), adsorption and desorption can take place at all sites. Therefore, $k'_a p_0 (\theta_0 + \theta_1 + \dots + \theta_n) = k'_d (\theta_0 + \theta_1 + \dots + \theta_n) \rightarrow k'_a p_0 = k'_d \rightarrow K' = 1/p_0$ and $K' p = p/p_0$ (3)

$$\bullet V/V_m = (1 - K' p) c K' p / [1 + (c-1) K' p] (1 - K' p)^2 \text{ from (2) and (3)}$$

$$= c (p/p_0) / [1 + (c-1) p/p_0] (1 - p/p_0) = V/V_m = c p p_0 / [p_0 + (c-1) p] (p_0 - p)$$

$$\bullet \text{Rearranging, } [p_0 + (c-1) p] / c p_0 V_m = p / V (p_0 - p) \rightarrow$$

$$p/V(p_0 - p) = 1/c V_m + [(c-1)/c V_m] (p/p_0); \quad y = a + b x \text{ type}$$

$p/V(p_0-p)$ vs. p/p_0 plot gives a **straight line** as shown in the Figure.

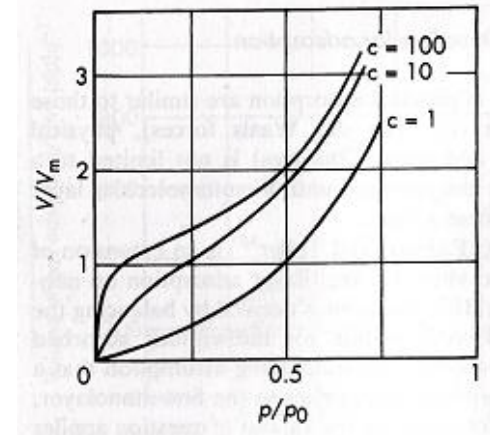
$$\frac{p}{V(p_0-p)} = \frac{1}{V_m c} + \frac{(c-1)}{V_m c} \frac{p}{p_0}$$

Intercept = $1/cV_m$

$$V_m = \frac{1}{\text{slope} + \text{intercept}}$$

V_m = monolayer capacity

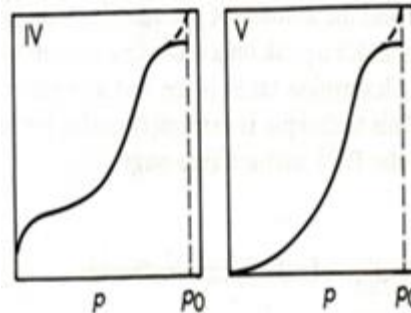
$$c = \exp(\Delta H_{\text{des}} - \Delta H_{\text{vap}}) / RT$$



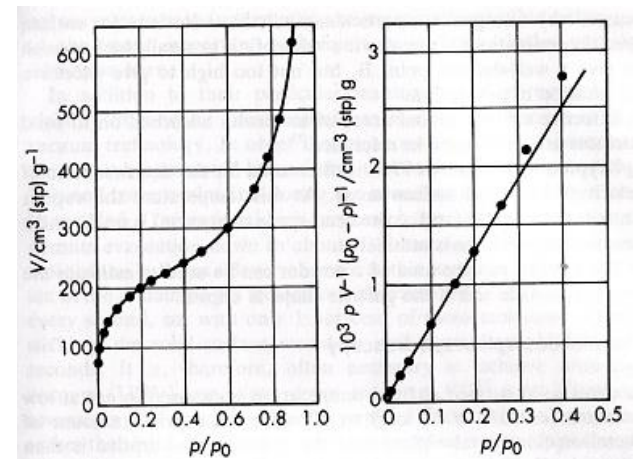
N_2 / silica gel @ 77 K

For a **porous solid**

$$V = \frac{V_m c x}{(1-x)} \cdot \frac{1 - (n+1)x^n + nx^{n+1}}{1 + (c-1)x - cx^{n+1}}$$



, where n is related to the pore size and $x = p/p_0$



Capillary Condensation

Porosity may result from

- 1) Gas evolution during the formation of the solid.
- 2) Fibrous structure.
- 3) Compaction of particulate solid.

Representative example: Zeolites

- Natural or synthetic materials
- SiO_4 and AlO_4 tetrahedra are linked by sharing O atoms
- 3D structure containing regular channels and cavities of sizes similar to those of small and medium-sized molecules.

Classification of pores

- Micropores: width < 2nm
- Mesopores: width = 2nm ~ 50 nm
- Macropores: width > 50 nm

Hysteresis loop in physisorption

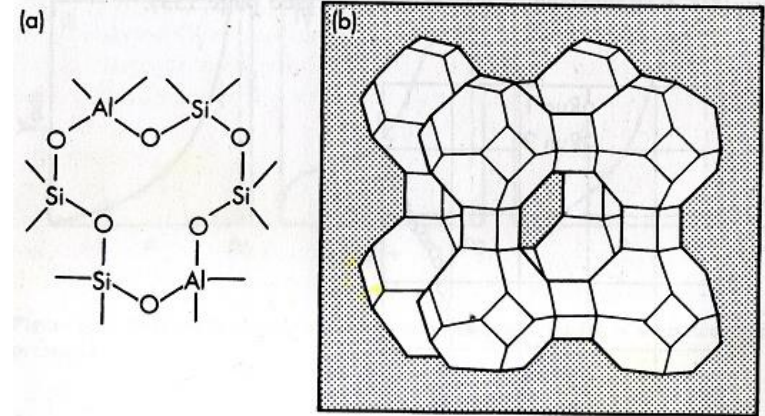
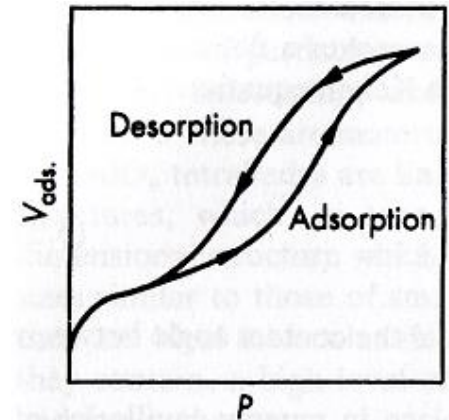


Figure 5.7 Zeolite structure. (a) 6-ring containing two aluminium and four silicon tetrahedral centres. (b) Zeolite A structure. Each of the eight sodalite units depicted contains 24 aluminium or silicon tetrahedral centres arranged to give six 4-rings plus eight 6-rings

Capillary Condensation

- **Kelvin equation:** $RT \ln p_r/p_0 = 2\gamma M/pr = 2\gamma V_m/r$
for a convex liquid-vapor interface
- For a liquid film inside a pore of radius r , which has a concave interface
 $RT \ln p_r/p_0 = - 2\gamma V_m \cos \theta /r$

