

Electro-Optics:

Electro-Optics (2)

Yoonchan Jeong

School of Electrical Engineering, Seoul National University

Tel: +82 (0)2 880 1623, Fax: +82 (0)2 873 9953

Email: yunchan@snu.ac.kr

Quadratic Electro-Optic Effect

$$\rightarrow s_{ij} = \begin{pmatrix} s_{11} & s_{12} & s_{13} & s_{14} & s_{15} & s_{16} \\ s_{21} & s_{22} & s_{23} & s_{24} & s_{25} & s_{26} \\ s_{31} & s_{32} & s_{33} & s_{34} & s_{35} & s_{36} \\ s_{41} & s_{42} & s_{43} & s_{44} & s_{45} & s_{46} \\ s_{51} & s_{52} & s_{53} & s_{54} & s_{55} & s_{56} \\ s_{61} & s_{62} & s_{63} & s_{64} & s_{65} & s_{66} \end{pmatrix}$$

Permutation symmetries:

$$\rightarrow s_{ijkl} = s_{jikl}$$

$$\rightarrow s_{ijkl} = s_{ijlk} \quad \rightarrow 1 = (11), 2 = (22), 3 = (33),$$

$$4 = (23) = (32), 5 = (13) = (31), 6 = (12) = (21)$$

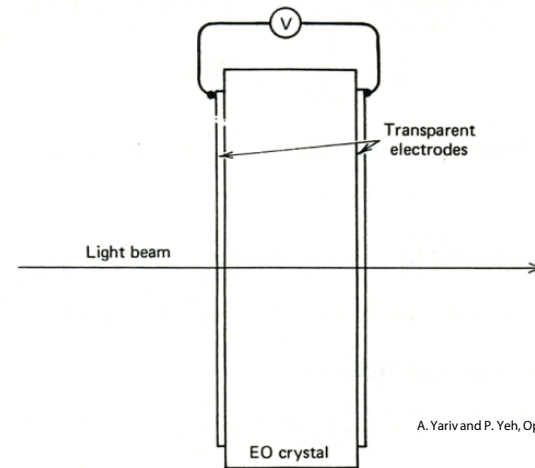
Index ellipsoid: $\rightarrow \eta_{ij}(\mathbf{E}) = \eta_{ij}(0) + r_{ijk} E_k + s_{ijkl} E_k E_l$

$$\begin{aligned} \rightarrow & x^2 \left(\frac{1}{n_x^2} + s_{11} E_x^2 + s_{12} E_y^2 + s_{13} E_z^2 + 2s_{14} E_y E_z + 2s_{15} E_z E_x + 2s_{16} E_x E_y \right) \\ & + y^2 \left(\frac{1}{n_y^2} + s_{21} E_x^2 + s_{22} E_y^2 + s_{23} E_z^2 + 2s_{24} E_y E_z + 2s_{25} E_z E_x + 2s_{26} E_x E_y \right) \\ & + z^2 \left(\frac{1}{n_z^2} + s_{31} E_x^2 + s_{32} E_y^2 + s_{33} E_z^2 + 2s_{34} E_y E_z + 2s_{35} E_z E_x + 2s_{36} E_x E_y \right) \\ & + 2yz (s_{41} E_x^2 + s_{42} E_y^2 + s_{43} E_z^2 + 2s_{44} E_y E_z + 2s_{45} E_z E_x + 2s_{46} E_x E_y) \\ & + 2zx (s_{51} E_x^2 + s_{52} E_y^2 + s_{53} E_z^2 + 2s_{54} E_y E_z + 2s_{55} E_z E_x + 2s_{56} E_x E_y) \\ & + 2xy (s_{61} E_x^2 + s_{62} E_y^2 + s_{63} E_z^2 + 2s_{64} E_y E_z + 2s_{65} E_z E_x + 2s_{66} E_x E_y) = 1 \end{aligned}$$

Electro-Optic Light Modulators

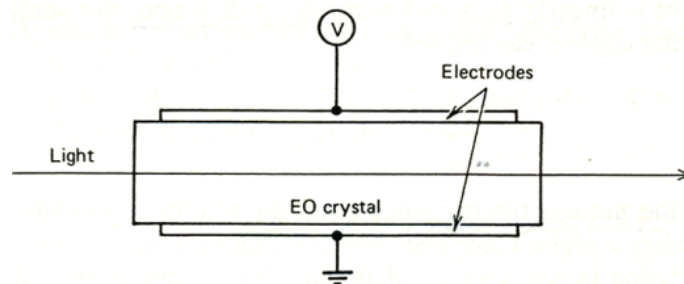
Longitudinal electro-optic modulation:

→ Large acceptance area with a thin EO crystal plate



A. Yariv and P. Yeh, Optical Waves in Crystals, John Wiley & Sons, 1984.

Transverse electro-optic modulation:

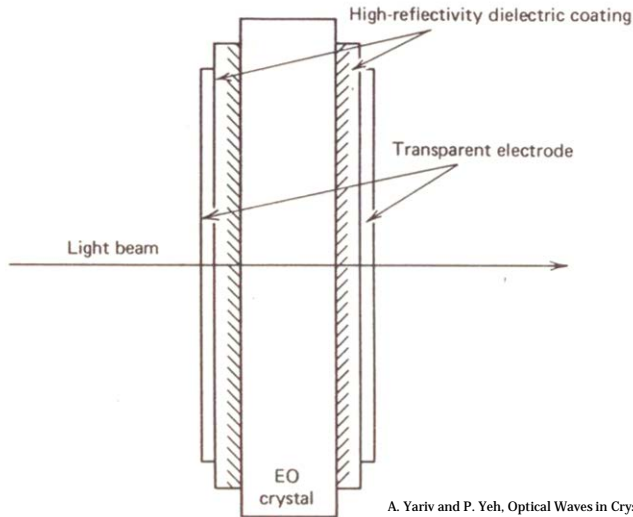


A. Yariv and P. Yeh, Optical Waves in Crystals, John Wiley & Sons, 1984.

→ Long interaction length at a given field strength

Electro-Optic Fabry-Perot Modulators

Electro-optic amplitude modulator:

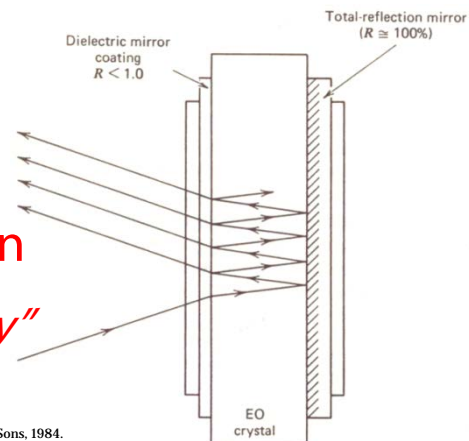


Charles Fabry
(1867-1945)

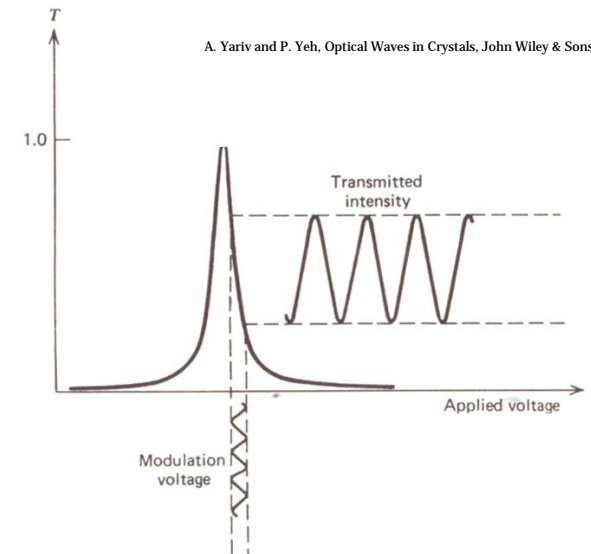


Alfred Perot
(1863-1925)

Transmission as a function of applied voltage:

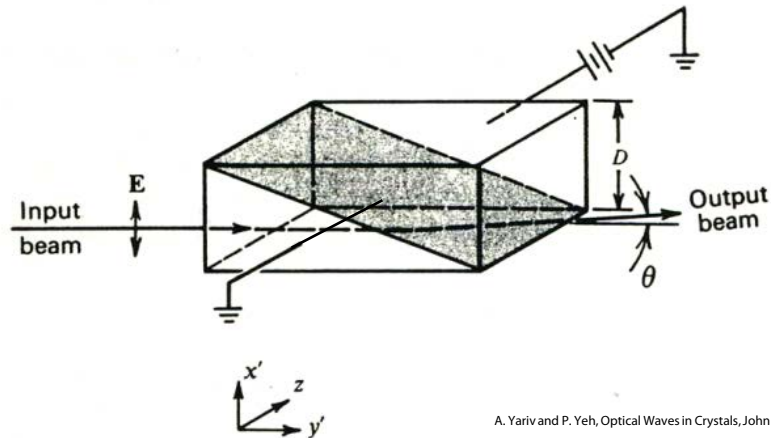
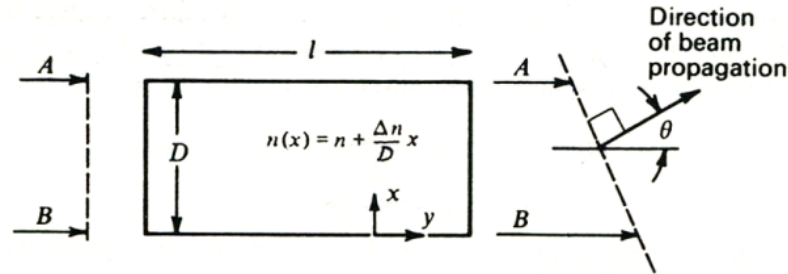


→ Gires-Tournois etalon
"Phase modulation only"



Electro-Optic Beam Deflectors

Double-prism KDP beam deflectors:



A. Yariv and P. Yeh, Optical Waves in Crystals, John Wiley & Sons, 1984.

Electro-Optic Property of Liquid Crystal

Liquid crystals:

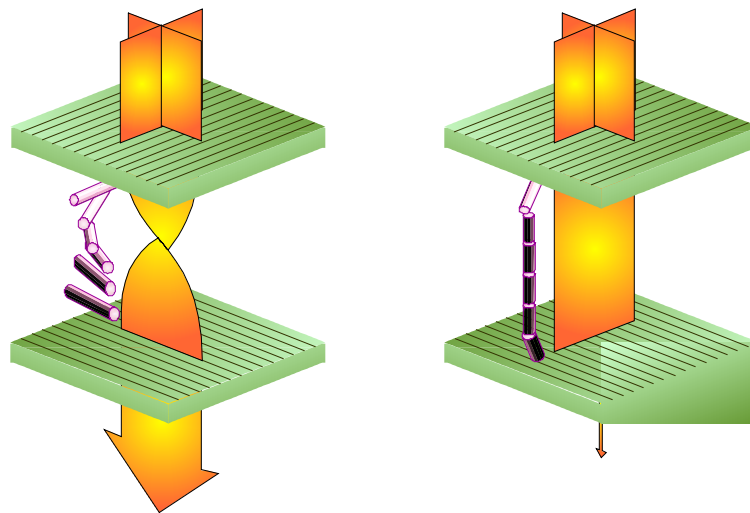
Liquid crystal phases: smectic, nematic, and cholesteric

Nematic LC: uniaxial dipole moment

→ Dynamic director alignment along the applied electric field

→ Switching time: ~msec

Twisted nematic LC in liquid crystal displays (LCDs):



$V_{LC} = 0V$ (off)

$V_{LC} = 5V$ (on)

Applicable to
fiber-optic devices?

LC-Filled Hollow Optical Fiber (1)

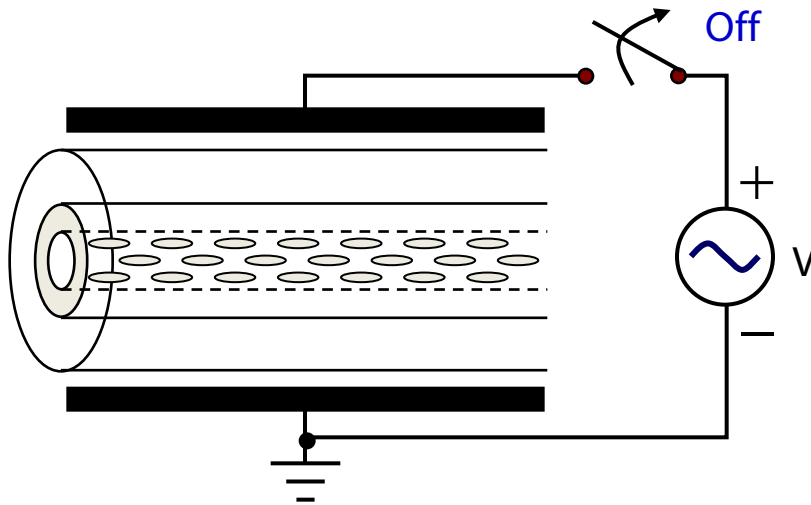
Director alignment of nematic LC:

Highly dependent on the liquid crystals-capillary interface interaction

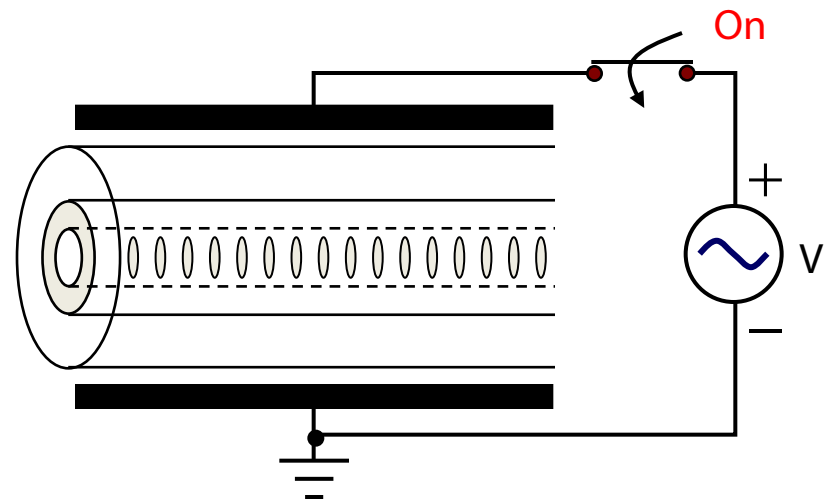
Silica: longitudinal direction

borosilicate capillaries: radial direction

Voltage off:

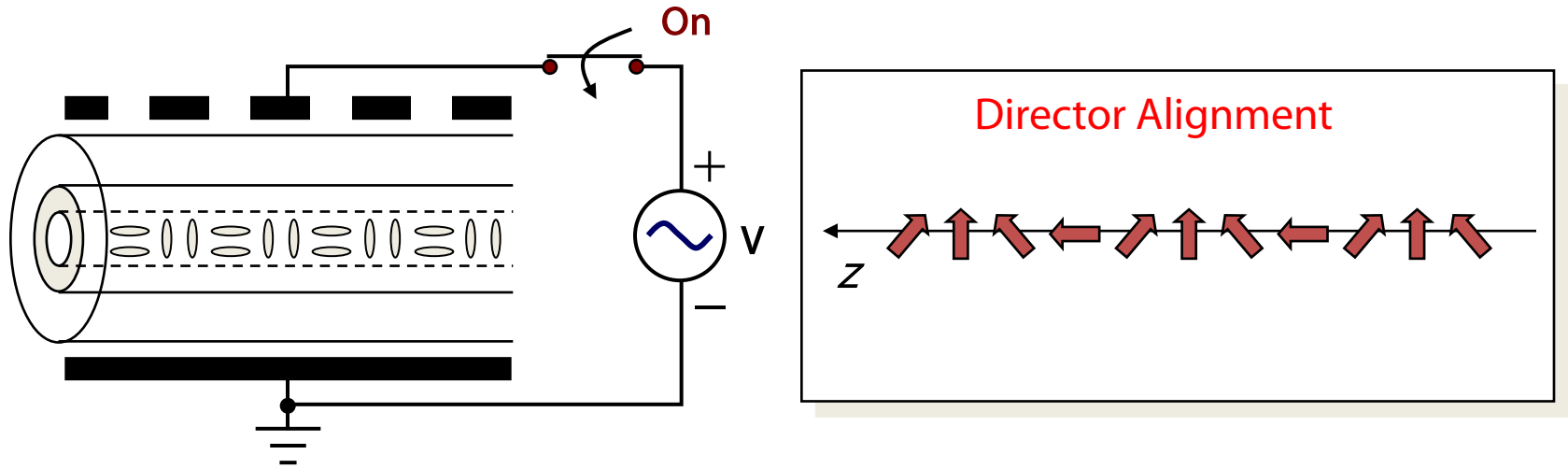


Voltage on:



LC-Filled Hollow Optical Fiber (2)

Comb electrode:



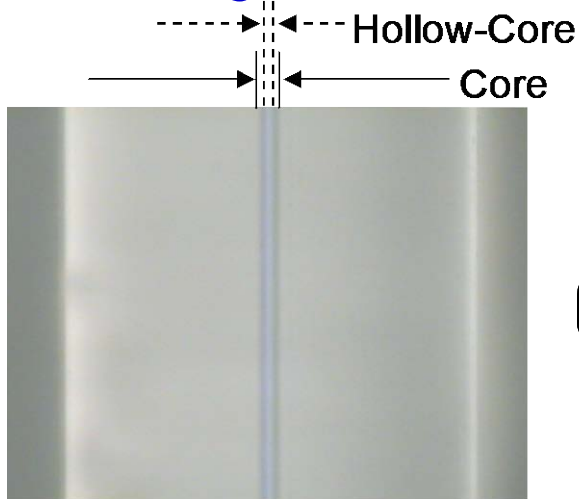
Electrically controllable director alignment:

Periodical modulation of director alignment

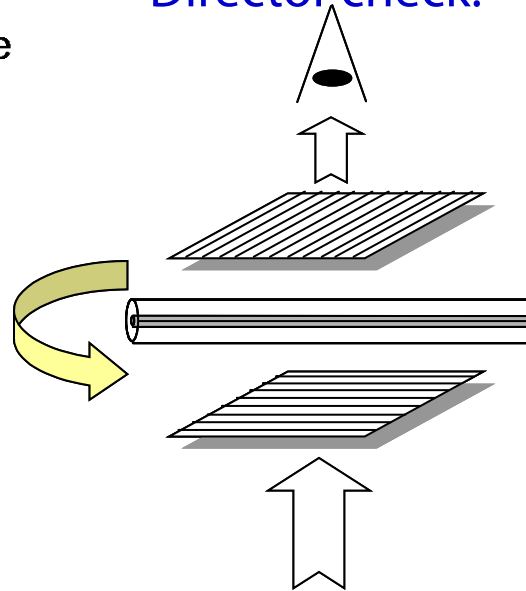
→ Controllable long-period gratings

LC-Filled Hollow Optical Fiber (3)

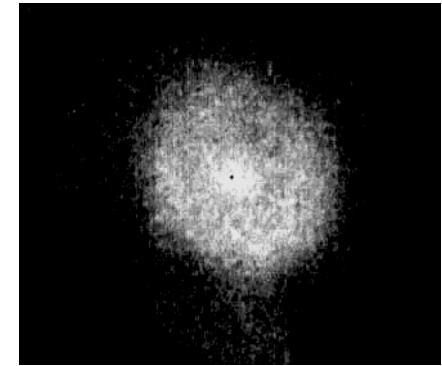
Fiber image:



Director check:



Far-field image:



Properties of MLC-6295:

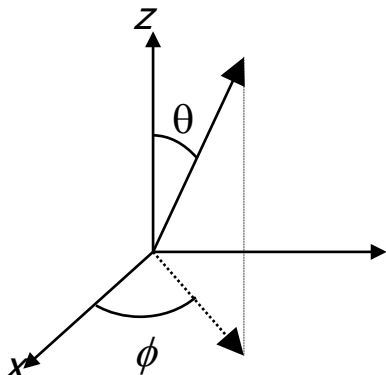
Smectic/Nematic turning point: $-30\text{ }^{\circ}\text{C}$, clearing point $+101\text{ }^{\circ}\text{C}$
 n_o : 1.4772, n_e : 1.5472 @ $20\text{ }^{\circ}\text{C}$, 589 nm

Director alignment check:

Visibility detection under a microscope between crossed polarizers
Uniform director alignment to the direction of the fiber axis

Anisotropic Mode Couplings in the LC Core

Permittivity tensor dependent on the director alignment:



$$\varepsilon_{xyz}(\theta) = \varepsilon_o \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \theta & -\sin \theta \\ 0 & \sin \theta & \cos \theta \end{pmatrix} \cdot \begin{pmatrix} n_o^2 & 0 & 0 \\ 0 & n_o^2 & 0 \\ 0 & 0 & n_e^2 \end{pmatrix} \cdot \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \theta & \sin \theta \\ 0 & -\sin \theta & \cos \theta \end{pmatrix}$$

$$\varepsilon_{r\phi z}(\theta, \phi) = \varepsilon_o \begin{pmatrix} \cos \phi & \sin \phi & 0 \\ -\sin \phi & \cos \phi & 0 \\ 0 & 0 & 1 \end{pmatrix} \cdot \varepsilon_{xyz}(\theta) \cdot \begin{pmatrix} \cos \phi & -\sin \phi & 0 \\ \sin \phi & \cos \phi & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

Permittivity perturbation:

$$\Delta \varepsilon_{r\phi z}(\theta, \phi) = \varepsilon_{r\phi z}(\theta, \phi) - \varepsilon_{r\phi z}(0, 0)$$

Mode couplings:

Long-period regime: a fundamental core mode (HE_{11}) \leftrightarrow cladding modes

Cladding modes to be coupled:

$$TM_{0m}^{cl}, TE_{0m}^{cl}, HE_{1m}^{cl}, HE_{2m}^{cl}, HE_{3m}^{cl} \leftarrow \Delta \varepsilon_{r\phi z}(\theta, \phi)$$

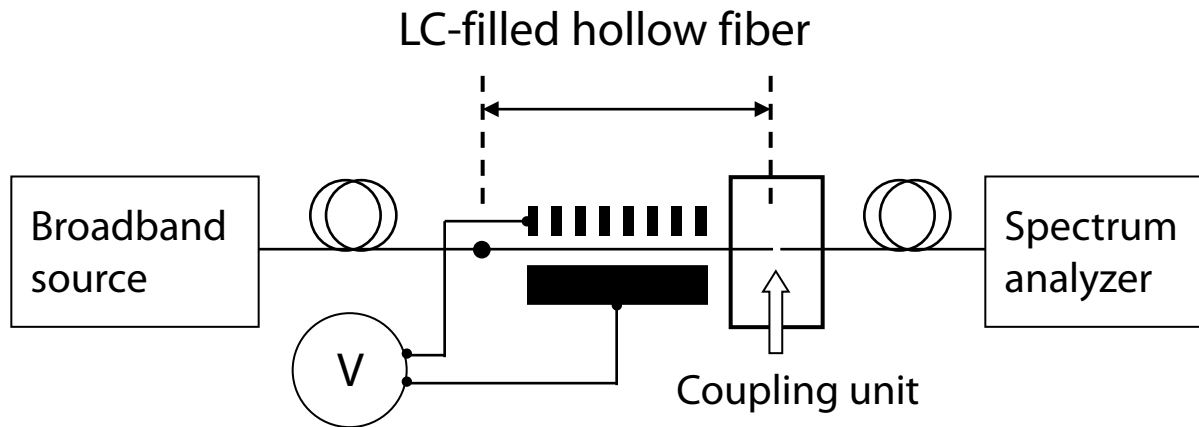
Experimental Arrangement

Experimental setup:

Broadband source: EDFA ASE

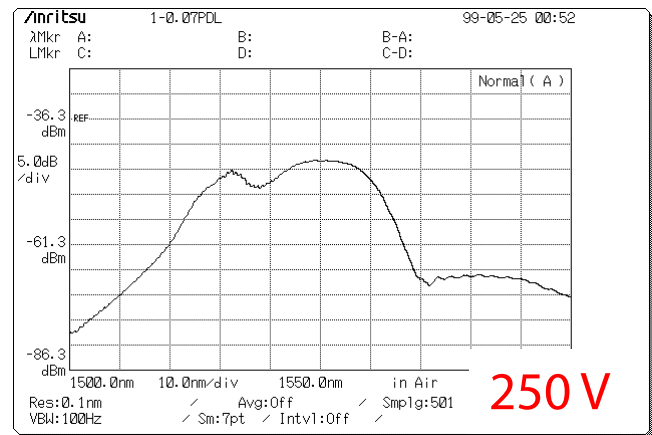
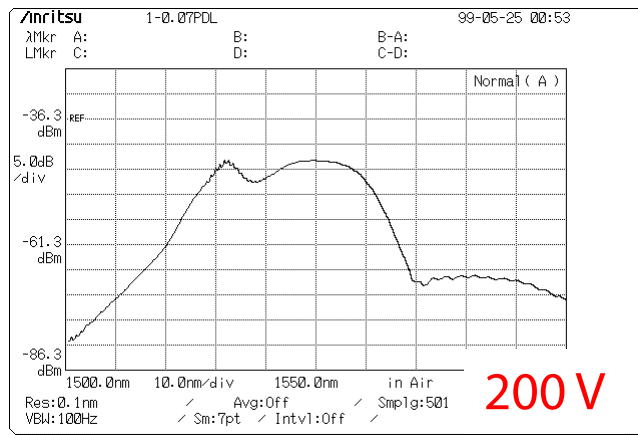
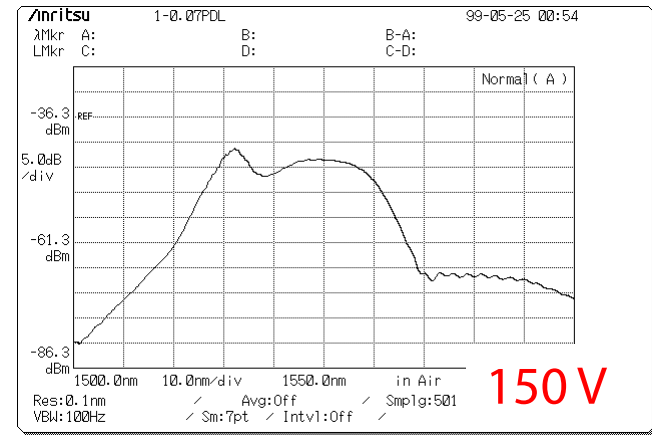
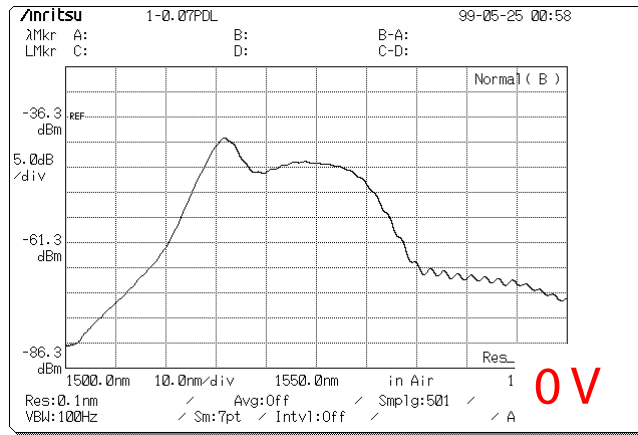
Comb electrode: Period of $483 \mu\text{m}$, length of 15.5 mm

Applied voltage: $0 \sim 250 \text{ V}$



Long-Period LC Fiber Grating (1)

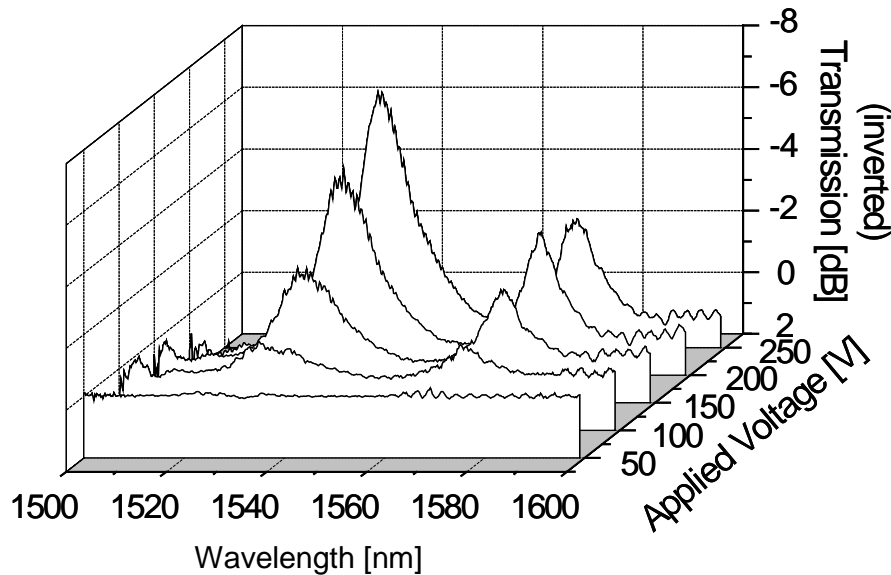
Spectral responses with respect to applied voltages:



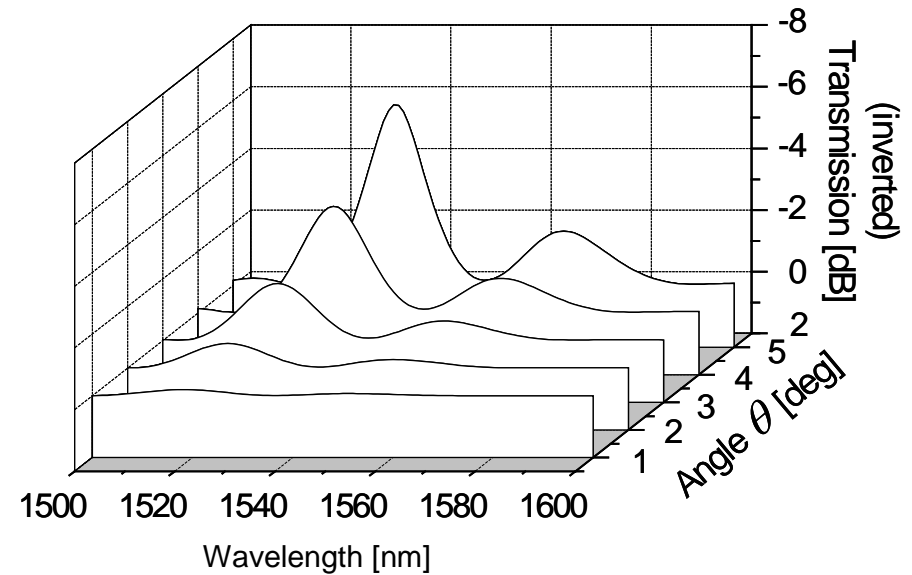
Long-Period LC Fiber Grating (2)

Normalized spectral responses:

Experiments:



Simulations:



Simulations:

Based on the coupled-mode theory in anisotropic media

Resonant couplings to the 3rd and 4th TM cladding modes

Nonlinear Response of Fiber Gratings (1)

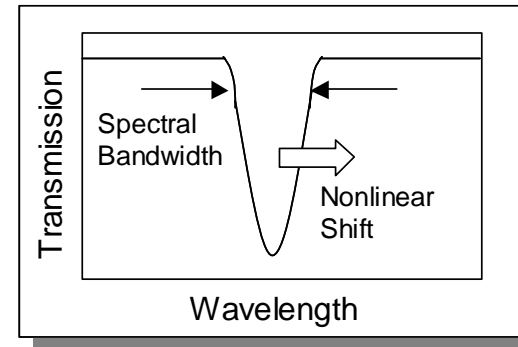
Coupled-mode theory with nonlinear perturbation:

$$\nabla \cdot (E' \times H_p^* + E_p^* \times H') = -i\omega E_p^* \cdot (\Delta\epsilon_L + \Delta\epsilon_{NL})E', \quad (p = 1, 2, \dots)$$

$$\Delta\epsilon_{NL(q)} = \epsilon_0 \frac{3}{4} \chi^{(3)}(r, \phi, z) \cdot \sum_s \alpha_{(q,s)} |E_s(t, z)|^2 |\hat{e}_s|^2, \quad \alpha_{(q,s)} = \begin{cases} 1 & (q = s), \\ 2 & (q \neq s). \end{cases}$$

Nonlinear spectral shift:

$$\rightarrow \frac{\Delta\lambda_s}{\lambda} \approx \frac{n_{2,eff} I_{eff}}{\Delta n_g}$$

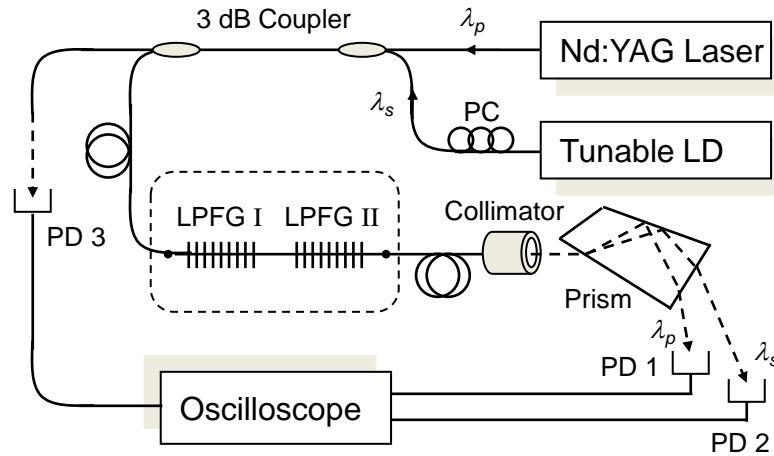


Nonlinear Response of Fiber Gratings (2)

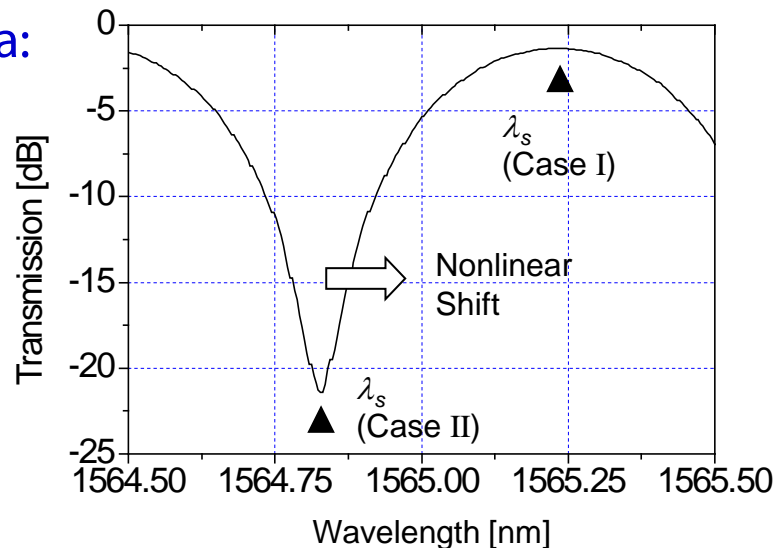
Experimental setup:

Signal wave: Tunable LD @1565.2 nm (Case I), @1564.8 nm (Case II)

Pump wave: Q-switched Nd:YAG laser (1 kHz)

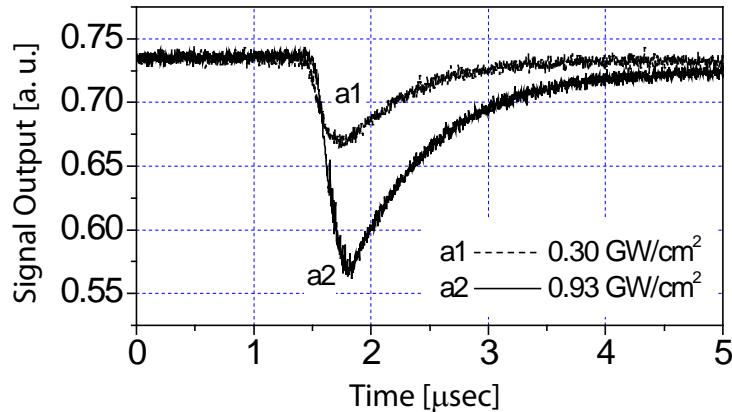


Initial transmission spectra:

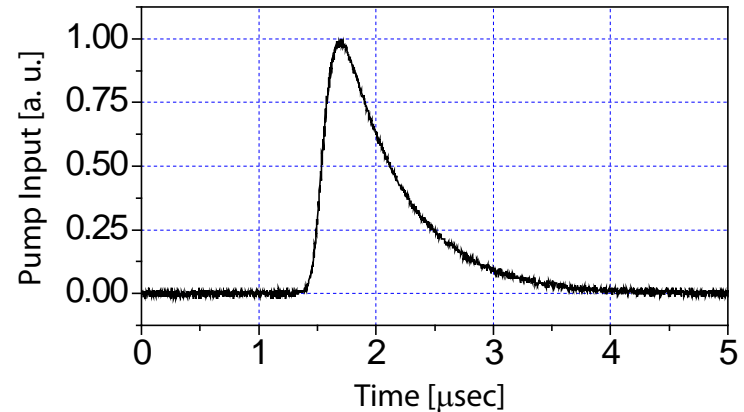


Nonlinear Response of Fiber Gratings (3)

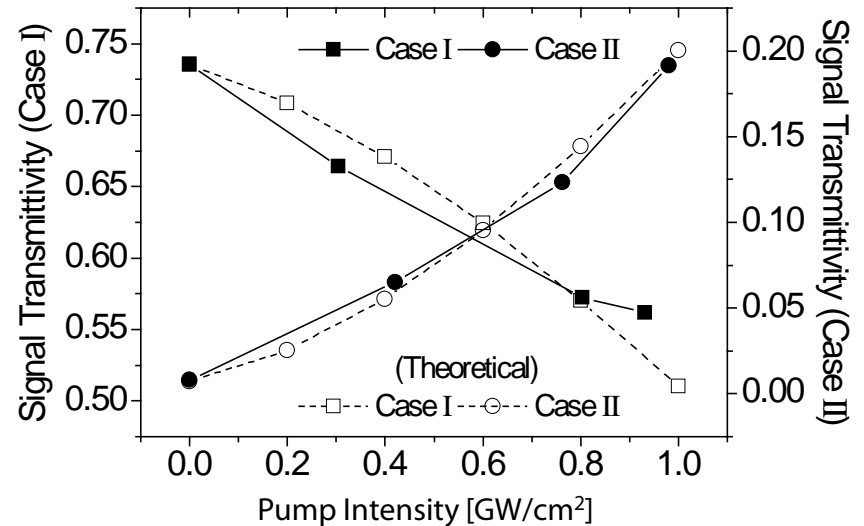
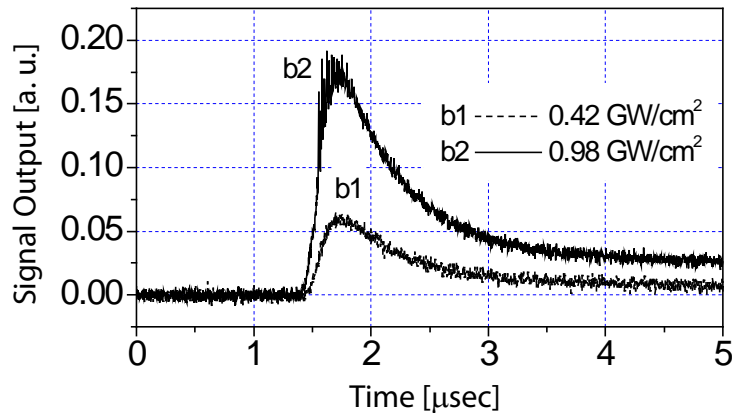
Signal (Case I):



Pump:



Signal (Case II):



$\rightarrow \Delta\lambda_s \sim 0.12 \text{ nm}/(\text{GW}/\text{cm}^2)$