



# Introduction to Data Mining

## Lecture #17: Recommendation – Content based & Collaborative Filtering

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# In This Lecture

- Understand the motivation and the problem of recommendation
- Compare the content-based vs. collaborative filtering approaches for recommender system
- Learn how to evaluate methods for recommendation

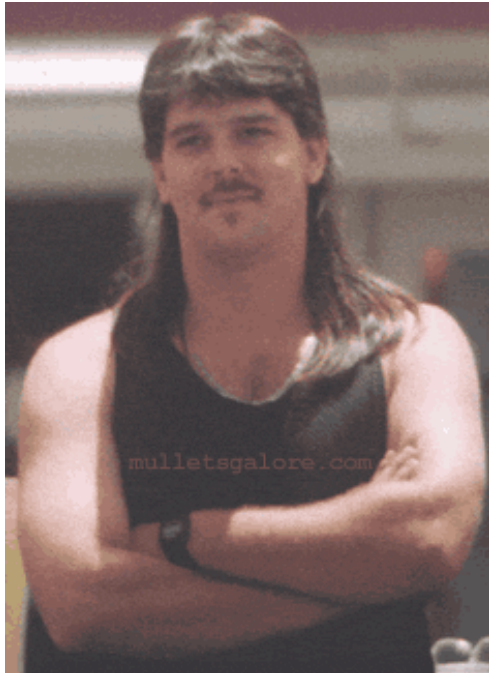


# Outline

- ➔  **Overview**
- Content-based Recommender System
- Collaborative Filtering
- Evaluation & Complexity



# Example: Recommender Systems



## ■ Customer X

- ❑ Buys Metallica CD
- ❑ Buys Megadeth CD

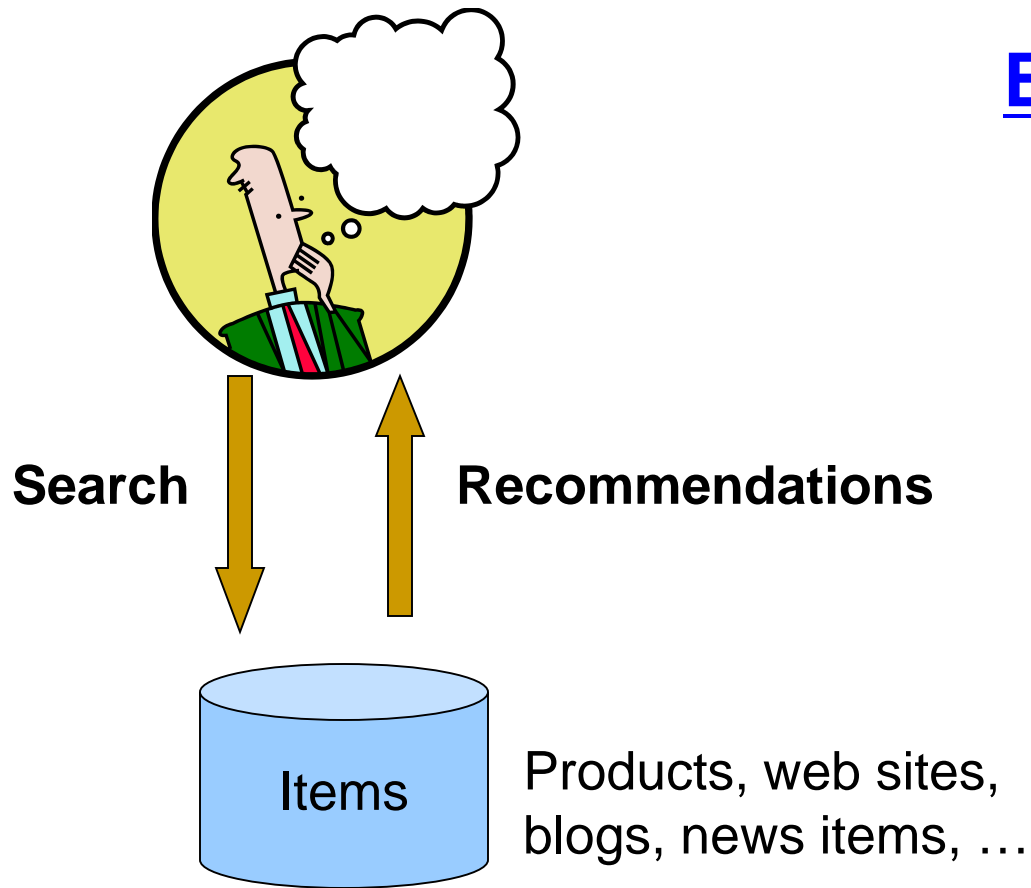


## ■ Customer Y

- ❑ Does search on Metallica
- ❑ Recommender system suggests Megadeth from data collected about customer X

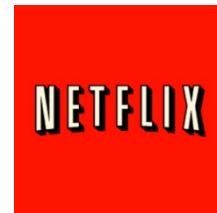


# Recommendations



## Examples:

amazon.com.



**movie lens**  
helping you find the *right* movies





# Offline vs. Online Recommendation

- **Offline recommendation: popular item**
  - Wall-mart: shelf space contains only 'popular' items
  - Also: TV networks, movie theaters,...
- **Web enables near-zero-cost dissemination of information about products**
  - Can recommend scarce items, too
- **More choice necessitates better filters**
  - Recommendation engines
  - How **Into Thin Air (1998)** made **Touching the Void (1988)** a bestseller: <http://www.wired.com/wired/archive/12.10/tail.html>



# Sidenote: The Long Tail



Sources: Erik Brynjolfsson and Jeffrey Hu, MIT, and Michael Smith, Carnegie Mellon; Barnes & Noble; Netflix; RealNetworks  
Source: Chris Anderson (2004)



# Types of Recommendations

## ■ Editorial and hand curated

- List of favorite cities
- List of “essential” items for travel

## ■ Simple aggregates

- Top 10, Most Popular, Recent Uploads

## ■ Tailored to individual users

- Amazon, Netflix, ...





# Formal Model

- $X$  = set of **Customers**
- $S$  = set of **Items**
- **Utility function**  $u: X \times S \rightarrow R$ 
  - $R$  = set of ratings
  - $R$  is a totally ordered set
  - e.g., **0-5** stars, real number in **[0,1]**



# Utility Matrix

	Avatar	LOTR	Matrix	Pirates
Alice	1		0.2	
Bob		0.5		0.3
Carol	0.2		1	
David				0.4



# Key Problems

- **(1) Gathering “known” ratings for matrix**
  - How to collect the data in the utility matrix
  
- **(2) Extrapolate unknown ratings from the known ones**
  - Mainly interested in high unknown ratings
    - We are not interested in knowing what you don't like but what you like
  
- **(3) Evaluating extrapolation methods**
  - How to measure success/performance of recommendation methods



# (1) Gathering Ratings

## ■ Explicit

- Ask people to rate items
- Doesn't work well in practice – people can't be bothered

## ■ Implicit

- Learn ratings from user actions
  - E.g., purchase implies high rating
- What about low ratings?
  - “not buying an item” = “don't like the item” ?



## (2) Extrapolating Utilities

- **Key problem:** Utility matrix  $U$  is **sparse**
  - Most people have not rated most items
  - **Cold start:**
    - New items have no ratings
    - New users have no history
- **Three approaches to recommender systems:**
  - **1)** Content-based
  - **2)** Collaborative
  - **3)** Latent factor based



# Outline

Overview

  **Content-based Recommender System**

Collaborative Filtering

Evaluation & Complexity



# Content-based Recommendations

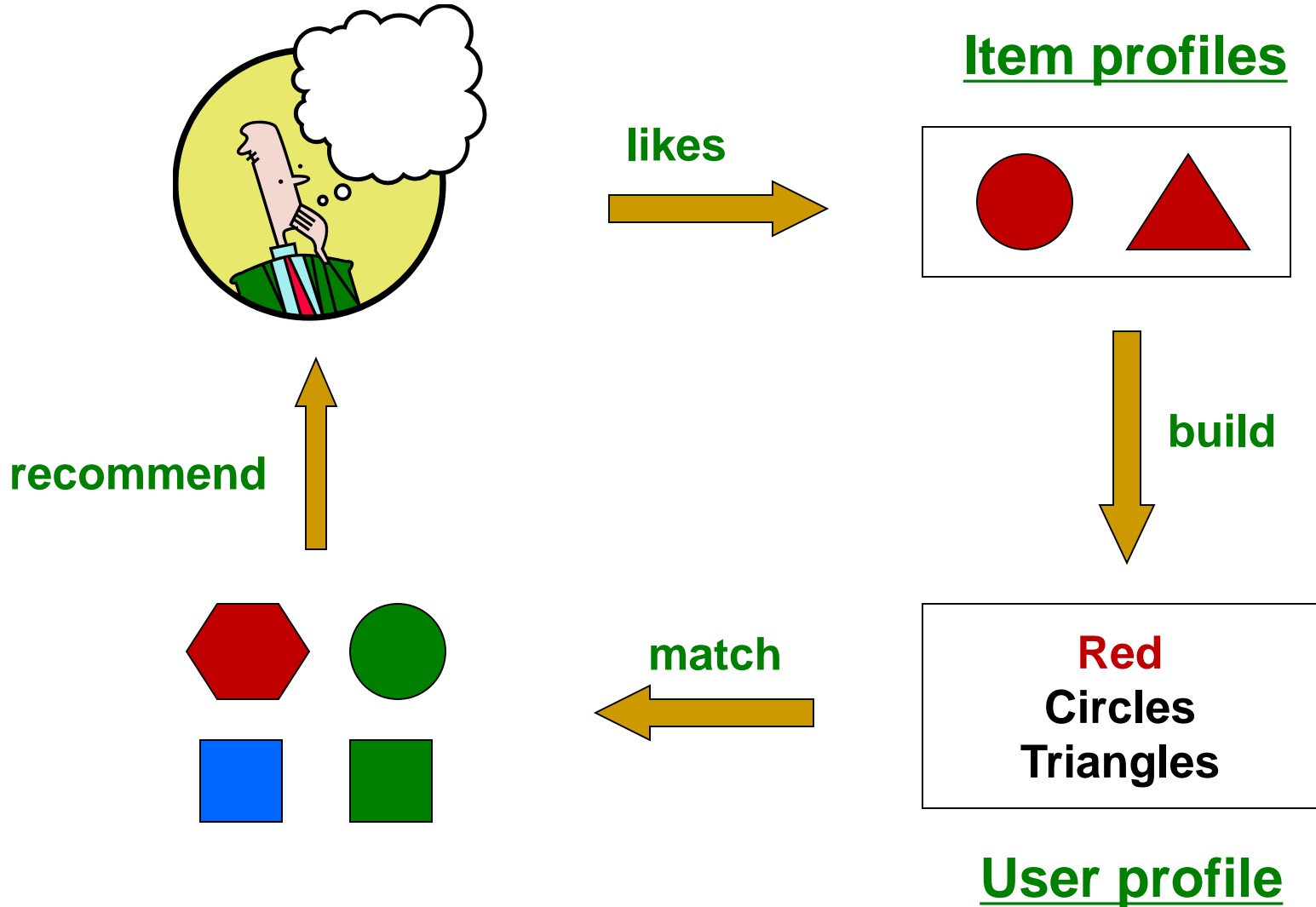
- **Main idea:** Recommend items to customer  $x$  similar to previous items rated highly by  $x$ 
  - Andy enjoyed watching “Avengers 2”. Andy will also like “Captain America Civil War” as well since they are similar in content

## *Example:*

- **Movie recommendations**
  - Recommend movies with same actor(s), genre, ...
- **Websites, blogs, news**
  - Recommend other sites with “similar” content



# Plan of Action







# Item Profiles

- For each item, create an **item profile**
- **Profile is a set (vector) of features**
  - **Movies:** author, title, actor, ...
  - **Text:** Set of “important” words in document
- **How to pick important features?**
  - Usual heuristic from text mining is **TF-IDF**  
(Term frequency \* Inverse Doc Frequency)
    - **Term ... Feature**
    - **Document ... Item**



# Sidenote: TF-IDF

$f_{ij}$  = frequency of term (feature)  $i$  in doc (item)  $j$

$$TF_{ij} = \frac{f_{ij}}{\max_k f_{kj}}$$

**Note:** we normalize TF to discount for “longer” documents

$n_i$  = number of docs that mention term  $i$

$N$  = total number of docs

$$IDF_i = \log \frac{N}{n_i}$$

**TF-IDF score:**  $w_{ij} = TF_{ij} \times IDF_i$

**Doc profile** = set of words with highest **TF-IDF** scores, together with their scores



# User Profiles and Prediction

## ■ User profile possibilities:

- Weighted average of rated item profiles
- **Variation:** weight by difference from average rating for item
- ...

## ■ Prediction heuristic:

- Given user profile  $\mathbf{x}$  and item profile  $\mathbf{i}$ , estimate

$$u(\mathbf{x}, \mathbf{i}) = \cos(\mathbf{x}, \mathbf{i}) = \frac{\mathbf{x} \cdot \mathbf{i}}{\|\mathbf{x}\| \cdot \|\mathbf{i}\|}$$



# Pros: Content-based Approach

- **+: No need for data on other users**
  - No cold-start or sparsity problems
- **+: Able to recommend to users with unique tastes**
- **+: Able to recommend new & unpopular items**
  - No first-rater problem
- **+: Able to provide explanations**
  - Can provide explanations of recommended items by listing content-features that caused an item to be recommended



# Cons: Content-based Approach

- **–: Finding the appropriate features is hard**
  - E.g., images, movies, music
- **–: Recommendations for new users**
  - **How to build a user profile?**
- **–: Overspecialization**
  - Never recommends items outside user's content profile
  - People might have multiple interests
  - **Unable to exploit quality judgments of other users**



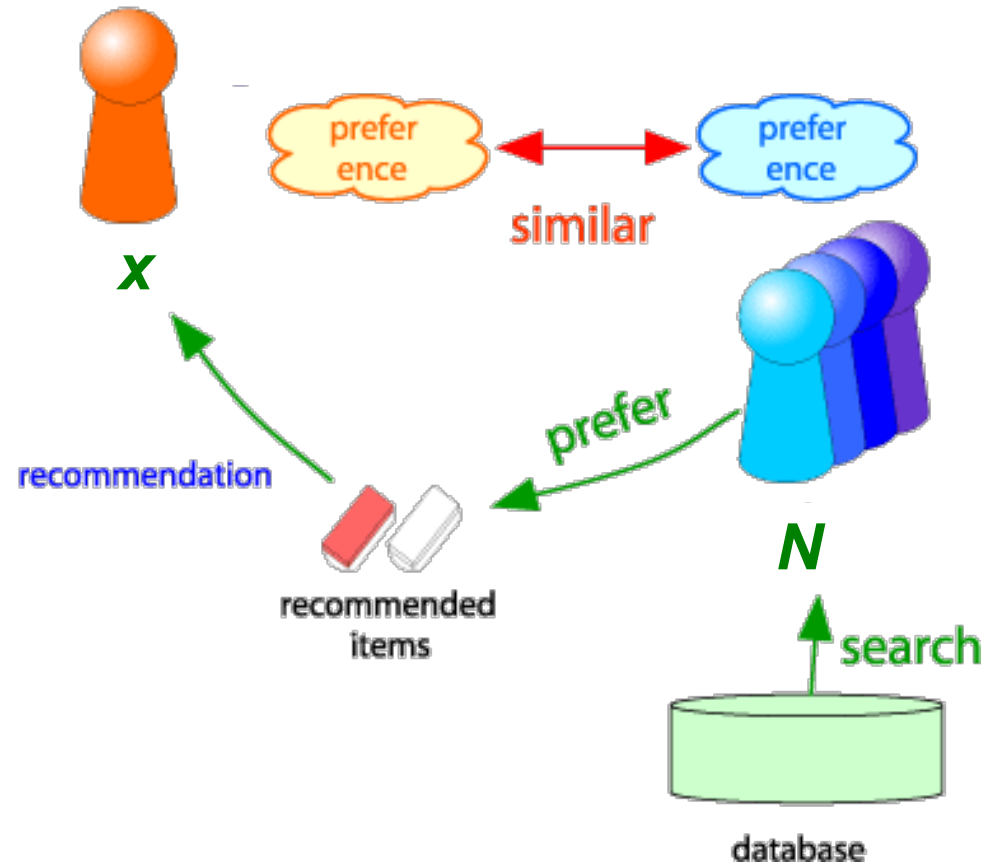
# Outline

- Overview
- Content-based Recommender System
- Collaborative Filtering**
- Evaluation & Complexity



# Collaborative Filtering

- Consider user  $x$
- Find set  $N$  of other users whose ratings are “**similar**” to  $x$ 's ratings
- Estimate  $x$ 's ratings based on ratings of users in  $N$



Note that contents of items are not used here.



# Finding "Similar" Users

$$r_x = [*, \_, \_, *, ***]$$

$$r_y = [*, \_, **, **, \_]$$

- Let  $r_x$  be the vector of user  $x$ 's ratings

- Jaccard similarity measure**

- Problem: Ignores the value of the rating

- Cosine similarity measure**

- $\text{sim}(x, y) = \cos(r_x, r_y) = \frac{r_x \cdot r_y}{\|r_x\| \cdot \|r_y\|}$

- Problem: low rating is not penalized much

- Pearson correlation coefficient**

- $S_{xy}$  = items rated by both users  $x$  and  $y$

$$\text{sim}(x, y) = \frac{\sum_{s \in S_{xy}} (r_{xs} - \bar{r}_x)(r_{ys} - \bar{r}_y)}{\sqrt{\sum_{s \in S_{xy}} (r_{xs} - \bar{r}_x)^2} \sqrt{\sum_{s \in S_{xy}} (r_{ys} - \bar{r}_y)^2}}$$

$r_x, r_y$  as sets:

$$r_x = \{1, 4, 5\}$$

$$r_y = \{1, 3, 4\}$$

$r_x, r_y$  as points:

$$r_x = \{1, 0, 0, 1, 3\}$$

$$r_y = \{1, 0, 2, 2, 0\}$$

$\bar{r}_x, \bar{r}_y \dots$  avg. rating of  $x, y$





# Similarity Metric

	HP1	HP2	HP3	TW	SW1	SW2	SW3
A	4			5	1		
B	5	5	4				
C				2	4	5	
D		3					3

- **Intuitively we want:**  $\text{sim}(A, B) > \text{sim}(A, C)$
- **Jaccard similarity:**  $1/5 < 2/4$
- **Cosine similarity:**  $0.386 > 0.322$

□ Problem: low rating is not penalized much

□ **Solution: subtract the (row) mean**

	HP1	HP2	HP3	TW	SW1	SW2	SW3
A	$2/3$			$5/3$	$-7/3$		
B	$1/3$	$1/3$	$-2/3$				
C				$-5/3$	$1/3$	$4/3$	
D		0					0

**sim A,B vs. A,C:  
 $0.092 > -0.559$**



# Rating Predictions

## From similarity metric to recommendations:

- Let  $r_x$  be the vector of user  $x$ 's ratings
- Let  $N$  (called 'k-nearest neighbors') be the set of  $k$  users most similar to  $x$  who have rated item  $i$

- **Prediction  $r_{xi}$  for item  $i$  of user  $x$ :**

- $r_{xi} = \frac{1}{k} \sum_{y \in N} r_{yi}$

Shorthand:

$s_{xy} = \text{sim}(x, y)$

- $r_{xi} = \frac{\sum_{y \in N} s_{xy} \cdot r_{yi}}{\sum_{y \in N} s_{xy}}$

- **Many other tricks possible...**



# Item-Item Collaborative Filtering

- So far: **User-user collaborative filtering**
- **Another view: Item-item**
  - For item  $i$ , find other similar items rated by user  $x$ 
    - Use the utility matrix for computing similarity
  - Estimate rating for item  $i$  based on ratings for similar items
  - Can use same similarity metrics and prediction functions as in user-user model

$$r_{xi} = \frac{\sum_{j \in N(i;x)} s_{ij} \cdot r_{xj}}{\sum_{j \in N(i;x)} s_{ij}}$$

$s_{ij}$ ... similarity of items  $i$  and  $j$   
 $r_{xj}$ ... rating of user  $x$  on item  $j$   
 $N(i;x)$ ... set items rated by  $x$  similar to  $i$



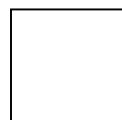
# Item-Item CF ( $|N|=2$ )

**users**

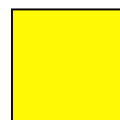
1   2   3   4   5   6   7   8   9   10   11   12

**movies**

1	1		3			5			5		4	
2			5	4			4			2	1	3
3	2	4		1	2		3		4	3	5	
4		2	4		5			4			2	
5			4	3	4	2					2	5
6	1		3		3			2			4	



- unknown rating



- rating between 1 to 5



# Item-Item CF ( $|N|=2$ )

**users**

1   2   3   4   5   6   7   8   9   10   11   12

**movies**

1	1		3		?	5			5		4	
2			5	4			4			2	1	3
3	2	4		1	2		3		4	3	5	
4		2	4		5			4			2	
5			4	3	4	2					2	5
6	1		3		3			2			4	



- estimate rating of movie **1** by user **5**



# Item-Item CF ( $|N|=2$ )

		users												
		1	2	3	4	5	6	7	8	9	10	11	12	
movies	1	1		3		?	5			5		4		sim(1,m) 1.00
	2			5	4			4			2	1	3	-0.18
	<u>3</u>	2	4		1	2		3		4	3	5		<u>0.41</u>
	4		2	4		5			4			2		-0.10
	5			4	3	4	2					2	5	-0.31
	<u>6</u>	1		3		3			2			4		<u>0.59</u>

**Neighbor selection:**  
Identify movies similar to movie 1, rated by user 5

**Similarity computation:**

- 1) Subtract mean rating  $m_i$  from each movie  $i$   
 $m_1 = (1+3+5+5+4)/5 = 3.6$   
 row 1: [-2.6, 0, -0.6, 0, 0, 1.4, 0, 0, 1.4, 0, 0.4, 0]
- 2) Compute cosine similarities between rows



# Item-Item CF ( $|N|=2$ )

		users												
		1	2	3	4	5	6	7	8	9	10	11	12	sim(1,m)
movies	1	1		3		?	5			5		4		1.00
	2			5	4			4			2	1	3	-0.18
	<u>3</u>	2	4		1	2		3		4	3	5		<u>0.41</u>
	4		2	4		5			4			2		-0.10
	5			4	3	4	2					2	5	-0.31
	<u>6</u>	1		3		3			2			4		<u>0.59</u>

Compute similarity weights:

$$s_{1,3}=0.41, s_{1,6}=0.59$$



# Item-Item CF ( $|N|=2$ )

users

	1	2	3	4	5	6	7	8	9	10	11	12
1	1		3		2.6	5			5		4	
2			5	4			4			2	1	3
<u>3</u>	2	4		1	2		3		4	3	5	
4		2	4		5			4			2	
5			4	3	4	2					2	5
<u>6</u>	1		3		3			2			4	

movies

Predict by taking weighted average:

$$r_{1.5} = (0.41 \cdot 2 + 0.59 \cdot 3) / (0.41 + 0.59) = 2.6$$

$$r_{ix} = \frac{\sum_{j \in N(i;x)} s_{ij} \cdot r_{jx}}{\sum s_{ij}}$$





# CF: Common Practice

Before:

$$r_{xi} = \frac{\sum_{j \in N(i;x)} s_{ij} r_{xj}}{\sum_{j \in N(i;x)} s_{ij}}$$

- Define **similarity**  $s_{ij}$  of items  $i$  and  $j$
- Select  $k$  nearest neighbors  $N(i; x)$ 
  - Items most similar to  $i$ , that were rated by  $x$
- Estimate rating  $r_{xi}$  as the weighted average:

$$r_{xi} = b_{xi} + \frac{\sum_{j \in N(i;x)} s_{ij} \cdot (r_{xj} - b_{xj})}{\sum_{j \in N(i;x)} s_{ij}}$$

baseline estimate for  $r_{xi}$

$$b_{xi} = \mu + b_x + b_i$$

- $\mu$  = overall mean movie rating
- $b_x$  = rating deviation of user  $x$   
= (avg. rating of user  $x$ ) -  $\mu$
- $b_i$  = rating deviation of movie  $i$   
= (avg. rating of movie  $i$ ) -  $\mu$



# CF: Baseline Predictor

- Mean movie rating: **3.7 stars**
- *The Sixth Sense* is **0.5** stars above avg.
- Joe rates **0.2** stars below avg.  
⇒ **Baseline estimation:**  
*Joe will rate **The Sixth Sense** 4 stars*





# Item-Item vs. User-User

	Avatar	LOTR	Matrix	Pirates
Alice	1		0.8	
Bob		0.5		0.3
Carol	0.9		1	0.8
David			1	0.4

- In practice, it has been observed that item-item often works better than user-user
- **Why?** Items are simpler, users have multiple tastes



# Pros/Cons of Collaborative Filtering

- **+ Works for any kind of item**
  - No feature selection needed
- **- Cold Start:**
  - Needs enough users in the system to find a match
- **- Sparsity:**
  - The user/ratings matrix is sparse
  - Hard to find users that have rated the same items
- **- First rater:**
  - Cannot recommend an item that has not been previously rated (e.g., new items, esoteric items)
- **- Popularity bias:**
  - Cannot recommend items to someone with unique taste
  - Tends to recommend popular items




# Hybrid Methods

- **Implement two or more different recommenders and combine predictions**
  - Perhaps using a linear model
- **Add content-based methods to collaborative filtering**
  - Item profiles for “new item problem”
    - User-user CF: no one has ever rated the new item
    - Item-item CF: one cannot find similar items to the new item
  - Demographics to deal with “new user problem”
    - User-user CF: cannot find similar users to the new user
    - Item-item CF: cannot find similar items to the item of interest



# Outline

- Overview
- Content-based Recommender System
- Collaborative Filtering
-   **Evaluation & Complexity**



# Evaluation

movies

users

1	3	4			
	3	5			5
		4	5		5
		3			
		3			
2			2		2
				5	
	2	1			1
	3			3	
1					



# Evaluation

movies

users

1	3	4			
	3	5			5
		4	5		5
		3			
		3			
2			?		?
				?	
	2	1			?
	3			?	
1					

Test Data Set

The diagram illustrates a user-movie rating matrix. The vertical axis is labeled 'users' and the horizontal axis is labeled 'movies'. The matrix contains numerical ratings for some user-movie pairs and question marks for others. A blue arrow points to the bottom-right section of the matrix, labeled 'Test Data Set', which includes the ratings for user 2 and user 1 across the last three movies.





# Evaluating Predictions

## ■ Compare predictions with known ratings

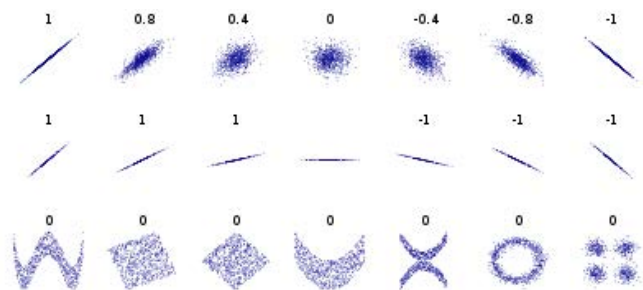
### □ Root-mean-square error (RMSE)

- $\sqrt{\sum_{xi}(r_{xi} - r_{xi}^*)^2}$  where  $r_{xi}$  is predicted,  $r_{xi}^*$  is the true rating of  $x$  on  $i$

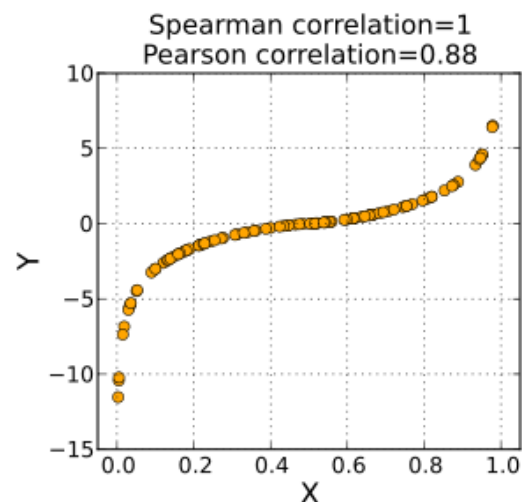
### □ Precision at top 10: error in top 10 highest predictions

### □ Rank Correlation:

- Spearman's *correlation* between system's and user's complete rankings



Pearson correlation coefficient



Rank correlation coefficient=1

(From  
Wikipedia)



# Problems with Error Measures

- **Narrow focus on accuracy sometimes misses the point**
  - E.g., Prediction diversity
- **In practice, we care only to predict high ratings:**
  - RMSE might penalize a method that does well for high ratings and badly for others



# Collaborative Filtering: Complexity

- Expensive step is finding  $k$  most similar customers:  $O(|X|)$ 
  - $X$  ... set of customers
- **Too expensive to do at runtime**
  - Could pre-compute
- Pre-compute finding similar customers
  - Near-neighbor search in high dimensions (**LSH**)
  - Clustering
  - Dimensionality reduction (later)



# Tip: Add Data

- **Simple method on large data is better than complex method on small data**

- Leverage all the data
- Don't try to reduce data size in an effort to make fancy algorithms work

- **Add more data**

- e.g., add IMDB data on genres

- **More data beats better algorithms**

<http://anand.typepad.com/datawocky/2008/03/more-data-usual.html>



# Questions?