

Introduction to Electromagnetism

The Electromagnetic Model

(1-1, 1-2, 1-3)

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The Electromagnetic Model

Electromagnetics?

The study of the effects of electric charges at rest and in motion

Inductive or deductive approach?

The course book uses deductive or axiomatic approach:

Elegant and orderly

Three essential steps for building an electromagnetic theory:

- First: Defining the **basic quantities** of electromagnetics
- Second: **Rules of operation** (vector algebra, vector calculus, & partial differential equations)
- Third: **Fundamental postulates** to deal with electromagnetic fields

Two basic quantities in our electromagnetic model:

- **Source** quantities
 - **Field** quantities
- } The cause and effect are not always distinct!

Source Quantities

- Electric charge: q or Q (C) ← Conservation of electric charge
e.g. the charge of an electron: $-e = -1.60 \times 10^{-19}$ (C)
- Volume charge density: $\rho = \lim_{\Delta v \rightarrow 0} \frac{\Delta q}{\Delta v}$ (C/m³)
- Surface charge density: $\rho_s = \lim_{\Delta s \rightarrow 0} \frac{\Delta q}{\Delta s}$ (C/m²)
- Line charge density: $\rho_l = \lim_{\Delta l \rightarrow 0} \frac{\Delta q}{\Delta l}$ (C/m)
- Current (Rate of change of charge w.r.t. time): $I = \frac{dq}{dt}$ (C/s or A)
- Volume current density: \mathbf{J} (A/m²)
- Surface current density: \mathbf{J}_s (A/m)

Fundamental Field Quantities

Symbols and Units	Field Quantity	Symbol	Unit
Electric	Electric field intensity	E	V/m
	Electric flux density (Electric displacement)	D	C/m ²
Magnetic	Magnetic flux density	B	T
	Magnetic field intensity	H	A/m

Constitutive relations:

The relations between **E** and **D** and between **B** and **H**

SI Units and Universal Constants

SI (International System of Units): MKSA system

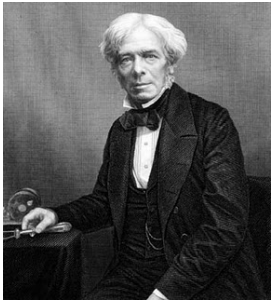
Quantity	Unit	Abbreviation
Length	<u>m</u> eter	m
Mass	<u>k</u> ilogram	kg
Time	<u>s</u> econd	s
Current	<u>a</u> mpere	A

Universal constants:

Quantity	Symbol	Value	Unit
Velocity of light in free space	c	$\sim 3 \times 10^8$	m/s
Permeability of free space	μ_0	$4\pi \times 10^{-7}$	H/m
Permittivity of free space	ϵ_0	$\sim 1/36\pi \times 10^{-9}$	F/m

$$\rightarrow c = \frac{1}{\sqrt{\epsilon_0 \mu_0}} \quad (\text{m/s})$$

Maxwell's Equations



Michael Faraday
(1791–1867)

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Andre Marie Ampere
(1775 - 1835)



Carl Friedrich Gauss
(1777 - 1855)

Static fields until Chap. 7

$$\nabla \times \mathbf{E} + \frac{\partial \mathbf{B}}{\partial t} = 0$$

$$\nabla \times \mathbf{H} - \frac{\partial \mathbf{D}}{\partial t} = \mathbf{J}$$

$$\nabla \cdot \mathbf{D} = \rho$$

$$\nabla \cdot \mathbf{B} = 0$$

Faraday's law

Ampère's law

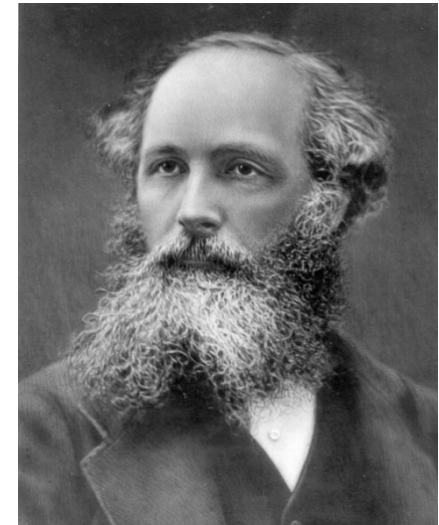
Gauss's law

No free magnetic monopole (?)

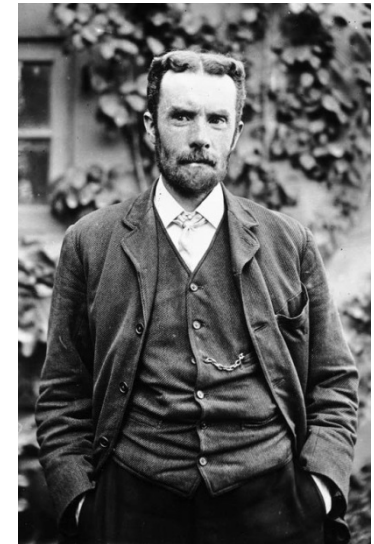
$$\mathbf{D} = \varepsilon \mathbf{E} = \varepsilon_0 \mathbf{E} + \mathbf{P}$$

$$\mathbf{H} = \frac{\mathbf{B}}{\mu} = \frac{\mathbf{B}}{\mu_0} - \mathbf{M}$$

Constitutive relations



James Clerk Maxwell
(1831–1879)



Oliver Heaviside
(1850–1925)