

Precision Metrology 24- Roughness Parameters for Surface

Cut-off length(λ_c), or Sampling length(L_c):

Sampling length of profile to eliminate longer spacing errors such as waviness and form error from the measured profile. Mechanical filter, electrical filter, mathematical filter can attenuate the raw data measured.

Evaluation length, or Traversing length (L):

The length for roughness evaluation, or the length to be traversed for roughness measurement, typically set to $5\lambda_c$.

The ISO 4288-1996 gives guidelines;

Recommended Cut-off (ISO 4288-1996)				
Periodic Profiles	Non-Periodic Profiles		Cut-off	Sampling Length/ Evaluation Length
Spacing Distance RSm (mm)	Rz (μm)	Ra (μm)	λc (mm)	λc (mm)/L
>0.013-0.04	T ₀ 0.1	T ₀ 0.02	0.08	0.08/0.4
>0.04-0.13	>0.1-0.5	>0.02-0.1	0.25	0.25/1.25
>0.13-0.4	>0.5-10	>0.1-2	0.8	0.8/4
>0.4-1.3	>10-50	>2-10	2.5	2.5/12.5
>1.3-4.0	>50	>10	8	8/40

Source: www.occonors.co.th

Surface parameters [ISO 4287, KSB0161]

Amplitude parameters: Vertical characteristics of roughness profile

Spacing parameters: Spacing of irregularity of roughness profile along a line of test

Hybrid parameters: Hybrid of Amplitude parameters and Spacing parameters, and is important in a functional view point

1. Amplitude parameters

R_p : Maximum Peak of roughness profile

R_v : Minimum Valley of roughness profile

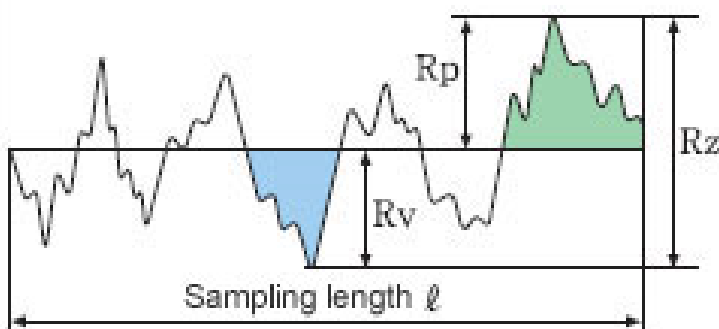
R_{max} , R_t : Maximum Peak to Valley over the several cut-off lengths, that is $R_p - R_v$

R_z : Ten points Height of Irregularities

= Avg. of 5 Heights of Peaks - Avg. of 5 Lowest Valleys

$= [R_{p1} + R_{p2} + R_{p3} + R_{p4} + R_{p5}] / 5 -$

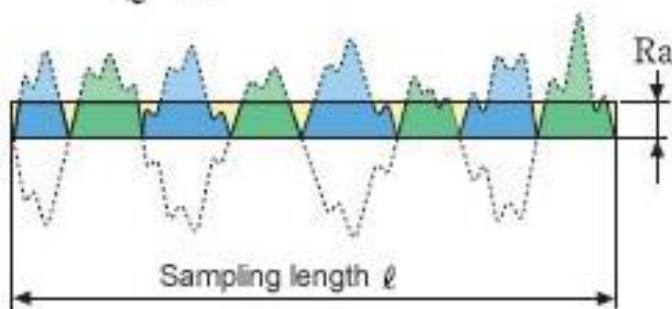
$[R_{v1} + R_{v2} + R_{v3} + R_{v4} + R_{v5}] / 5$



Source: www.olympus-ims.com

Ra: Average roughness

$$Ra = \frac{1}{\ell} \int_0^{\ell} |Z(x)| dx$$



Source: www.olympus-ims.com

$$Ra = \int |Z(x) - \underline{Z}| dx / L$$

where $\underline{Z} = \int Z(x) dx / L = \text{CLA (Centre Line Average)}$

In digital form; $Ra = [|Z_1| + |Z_2| + \dots + |Z_n|] / N$

For a sinusoidal profile with amplitude A ,

$$Ra = 2A/\pi \approx 0.636A,$$

:The most popular parameters for surface roughness

together with R_{max} ;

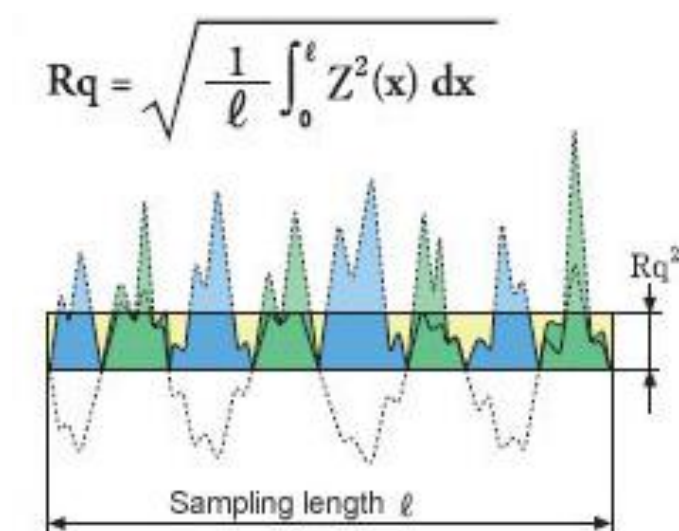
$R_{max} \approx (4-7) R_a$ for normal machining,

$R_{max} \approx (7-14) R_a$ for grinding and lapping

:Representative parameter for surface roughness,
otherwise specified

:Peak, Valley are considered with the same significance,
while the peak may be more significant for practical
cases

R_q : RMS(Root Mean Square) average roughness



Source:www.olympus-ims.com

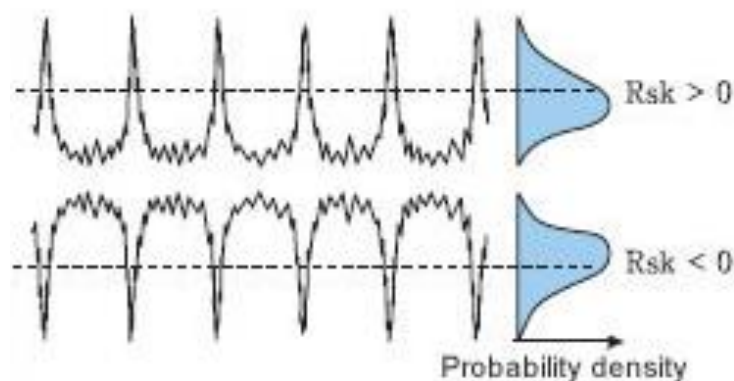
$$Rq = \sqrt{\int [Z(x) - \underline{Z}]^2 dx / L} \cong \sqrt{[Z_1^2 + Z_2^2 + \dots + Z_n^2] / N};$$

where \underline{Z} is the CLA

$Rq = A/\sqrt{2}$ for a sinusoidal profile with amplitude A ;

Rsk: Skewness

$$Rsk = \frac{1}{Rq^3} \left[\frac{1}{\ell} \int_0^{\ell} Z^3(x) dx \right]$$



Source: www.olympus-ims.com

$$Rsk = \int \left[\frac{Z(x) - \underline{Z}}{Rq} \right]^3 dx / L$$

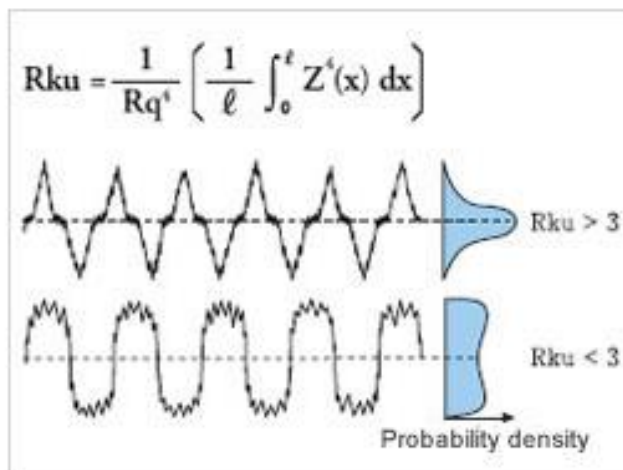
$$= [Z_1^3 + Z_2^3 + \dots + Z_n^3] / Rq^3 / N$$

Typically, $-3 \leq Rsk \leq 3$, and

Symmetric profile if $R_{sk}=0$

Less wear and better load capacity if $R_{sk}<0$

Rku: Kurtosis



Source:www.olympus-ims.com

$$R_{ku} = \int \left[\frac{Z(x) - \underline{Z}}{Rq} \right]^4 dx / L$$

$$= [Z_1^4 + Z_2^4 + \dots + Z_n^4] / Rq^4 / N$$

Normal surface (Normal distribution) if $Rku=3$

Sharp surface if $Rku>3$

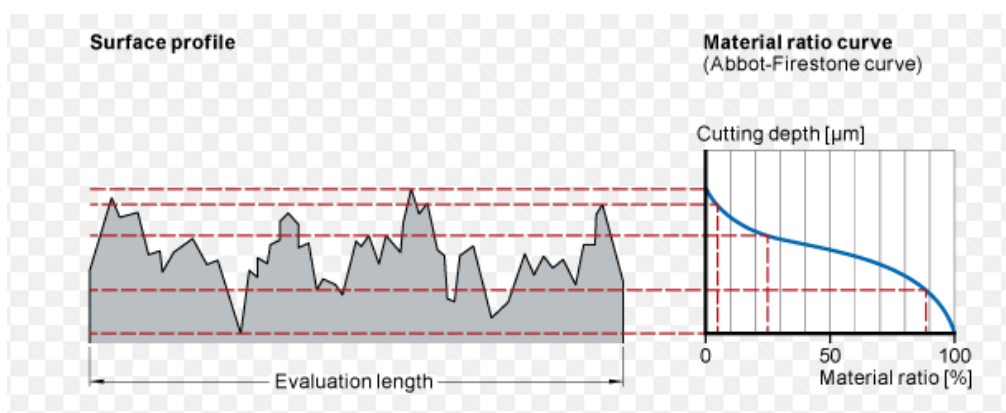
Dull surface if $Rku<3$

Bearing ratio, Material ratio, or Abbott Firestone Curve

:H vs T_p plot

Where, $T_p = [b_1 + b_2 + \dots + b_n] / L \times 100$ (%)

And b_n is the length of the n'th profile over the certain height, H



Source:www.skf.com

Straight line: Normal surface

Convex Curve: Less wear, Better load capacity

Concave Curve: More wear, Less load capacity

2. Spacing parameters

HSC: High Spot Count

Number of High Spots over the reference height during the evaluation length. Higher HSC surface with the same Ra give more dense profile.

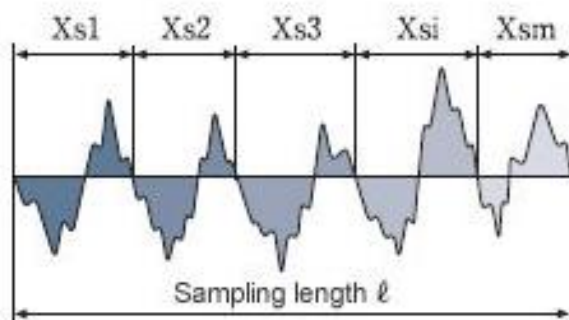
PC: Peak Count

Number of Peaks and Valleys exceeding the bandwidth from the reference height.

S_m or RS_m : Average spacing between profiles

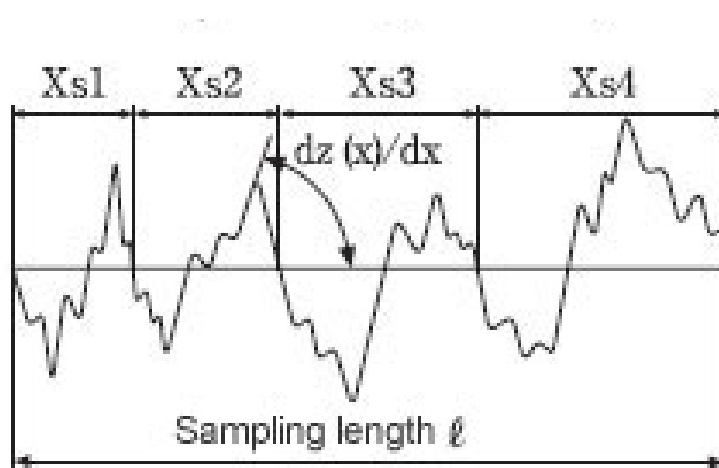
Average spacing of profile irregularities over length L

$$RS_m = \frac{1}{m} \sum_{i=1}^m X_{si}$$



Source: www.olympus-ims.com

3. Hybrid Parameters



Source: www.olympus-ims.com

Lr: Ratio of profile length to the nominal length

$$L_r = \int \sqrt{1 + \{dz/dx\}^2} / L \leq 1.01, \text{ typically}$$

Application: painting, plating, coating

Average slope of profiles, Δa and Δq

$$\Delta a = \int | dz/dx | dx / L \approx \Sigma | \delta z / \delta x | / N$$

$$\Delta q = \sqrt{\int (dz/dx)^2 dx / L} \approx \sqrt{[\Sigma (\delta z / \delta x)^2 / N]}$$

Generally, the average slope is less than 8 deg.

Application:

Mechanical -> Good interfacial strength and Hertz stress with lower slope; Lower friction and adhesion with lower slope

Optical -> Better reflectivity with lower slope

Average wavelength, λ_a , λ_q

$$\lambda_a = 2\pi R_a / \Delta a$$

$$\lambda_q = 2\pi R_q / \Delta q$$

Application: Larger wavelength profile will give less wear for the similar average roughness

Comparison with ∇ and Ra

$\nabla\nabla\nabla\nabla \Rightarrow 0.025-0.2 \text{ Ra}$

$\nabla\nabla\nabla \Rightarrow 0.4-1.6 \text{ Ra}$

$\nabla\nabla \Rightarrow 3.2-6.3 \text{ Ra}$

$\nabla \Rightarrow 12.5-25 \text{ Ra}$

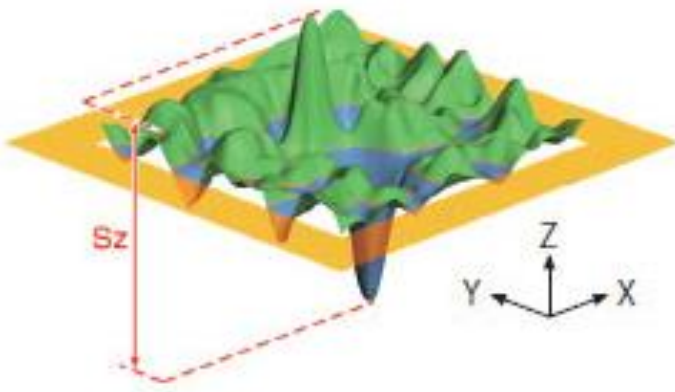
3D Surface Parameters

:To define 3D roughness parameters in terms of ISO 25178, that is 3D version of 2D parameters

S_p , S_v : Maximum peak, Valley over the surface

S_z , or S_{max} : Maximum peak to valley over the surface,

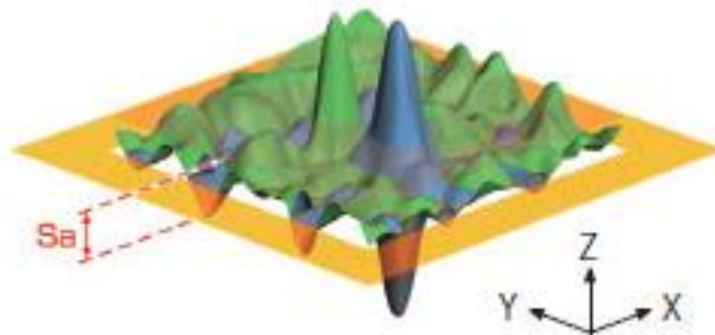
$S_z = S_p - S_v$



Source:www.olympus-ims.com

Sa: Average 3D surface roughness

$$S_a = \frac{1}{A} \iint_A |Z(x,y)| dx dy$$

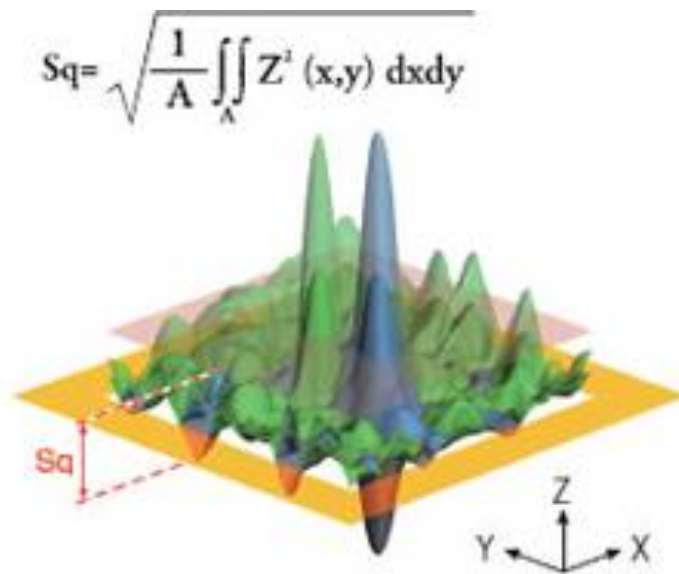


Source:www.olympus-ims.com

$$S_a = \iint |Z(x,y) - \underline{Z}| \, dx dy / A,$$

where $\underline{Z} = \iint |Z(x,y)| \, dx dy / A =$ mean surface height

Sq:Average RMS 3D surface roughness



$$S_q = \sqrt{\frac{1}{A} \iint Z^2(x,y) \, dx dy}$$

Source:www.olympus-ims.com

$$S_q = \sqrt{\iint (Z(x,y) - \underline{Z})^2 \, dx dy / A}$$

where $\underline{Z} =$ mean surface height

Similarly, other 3D parameters can be defined;

$$\text{3D Skewness, } S_{sk} = \iint [Z(x,y) - \underline{Z}]^3 / S_q^3 \, dx dy / A$$

$$\text{3D Kurtosis, } S_{ku} = \iint [Z(x,y) - \underline{Z}]^4 / S_q^4 \, dx dy / A$$