

## 9.3.3. Fed-Batch Operation



# What is a Fed-Batch Operation?

**A Variable-Volume Semi-Batch Operation  
with Feed but Withdrawal only at the End**

A Semi-Batch Operation in Which the Feed Containing Sources of Carbon, Nitrogen, and Others are Fed either Intermittently or Continuously During the Course of Otherwise a Batch Operation

# Why a Fed-Batch Operation?

- To Overcome Substrate Inhibition
- To Overcome Glucose Effect
- To Overcome Catabolite Repression
- To Utilize Auxotrophs
- To Achieve High Cell and Metabolite Density
- To Extend Operational Period
- To Alleviate High Broth Viscosity
- To Make Up for Water Loss by Evaporation

To Increase Reaction Rates and/or Yields  
and Overcome Physical Difficulties

# Products Using Fed-Batch Operation

- Antibiotics
- Baker`s Yeast
- Enzymes
- Microbial Cells
- Natural Lipids
- Nucleotides
- Organic Acids
- r-DNA Products
- Solvents
- Vitamins
- Yeasts

# Specific Growth Rate

$$\mu = \frac{1}{XV} \frac{d(XV)}{dt}$$

- Batch

$$\mu = \frac{1}{X} \frac{dX}{dt}$$

- Fed-Batch

$$\mu = \frac{1}{X} \frac{dX}{dt} + \frac{1}{V} \frac{dV}{dt}$$

# Growth Yield

$$Y = \frac{\Delta X}{\Delta S}$$
$$= - \frac{dX}{dS}$$

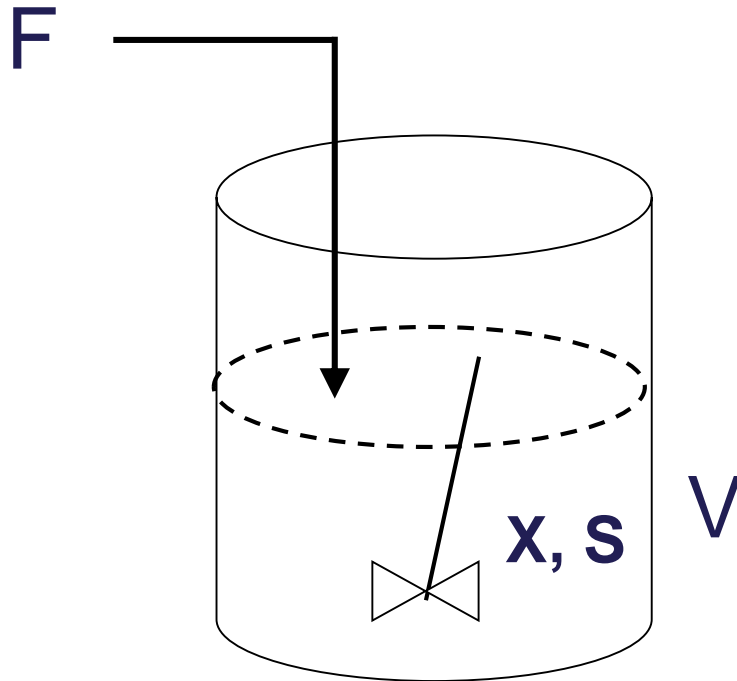
# Mass Balance

$$\text{Acc} = \text{In} - \text{Out} + \text{Gen} - \text{Con}$$

**Accumulation rate = Input rate – Output rate + Generation rate – Consumption rate**

$$\frac{d ( )}{d t} =$$

# Fed-Batch Operation



$F$  (L/h) : Flow Rate

$V$  (L) : Working Volume

$X$  (g/L) : Cell Concentration

$S$  (g/L) : Substrate Concentration



# Mass Balances

- cell

$$\frac{d(XV)}{dt} = \mu XV \text{ --- --- (1)}$$

- substrate

$$\frac{d(SV)}{dt} = S_F F - \frac{1}{Y} \mu XV \text{ --- --- (2)}$$

- Total

$$\frac{dV}{dt} = F \text{ --- --- --- --- (3)}$$

# Determination of Feed Rate

(using mass balance equations)

- cell

$$\frac{d(XV)}{dt} = \mu XV \rightarrow \frac{dX}{dt} = \left(\mu - \frac{F}{V}\right)X \text{ -----(1)}$$

- substrate

$$\frac{d(SV)}{dt} = S_F F - \frac{1}{Y} \mu XV \rightarrow \frac{dS}{dt} = (S_F - S) \frac{F}{V} - \frac{\mu X}{Y} \text{ -----(2)}$$

- Total

$$\frac{dV}{dt} = F \text{ -----(3)}$$

With  $\frac{dS}{dt} = 0$

$$(2) \rightarrow F = \frac{\mu X}{Y} \frac{V}{S_F - S} \text{ .....(4)}$$

# Determination of Feed Rate

(using mass balance equations)

- cell

$$\frac{d(XV)}{dt} = \mu XV$$

$$XV = X_0 V_0 e^{\mu t} \dots\dots(5)$$

$$(4) \rightarrow F = \frac{\mu X}{Y} \frac{V}{S_F - S} = \frac{\mu X_0 V_0}{Y (S_F - S)} e^{\mu t}$$

(5)

# ***E. coli* Fed-Batch Operation with Exponential Feeding**



# Productivity (g product/L hr)

## ■ Productivity

$$Pd = \frac{\frac{CellMass}{Volume} (X) \times SpecificExpression(Ps)}{CultureTime}$$

## ■ Necessary condition

- High cell density culture
- High specific expression

# To Maximize Productivity

- **High cell density culture**
  - **By-product: acetic acid**
    - Synthetic media:  $\mu = 0.35 \text{ hr}^{-1}$
    - Complex media:  $\mu = 0.2 \text{ hr}^{-1}$
- **High specific expression**
  - **Expression vs. specific growth rate**
    - Low  $\mu$ , high product
  - **Proteolytic degradation**

# Feed Flow Rate Control in Fed-Batch Operation

- **Feedback Control**
- **Feed Forward Control**
  - $\mu \uparrow$ , acetic acid  $\uparrow$ , growth  $\downarrow$ , expression  $\downarrow$

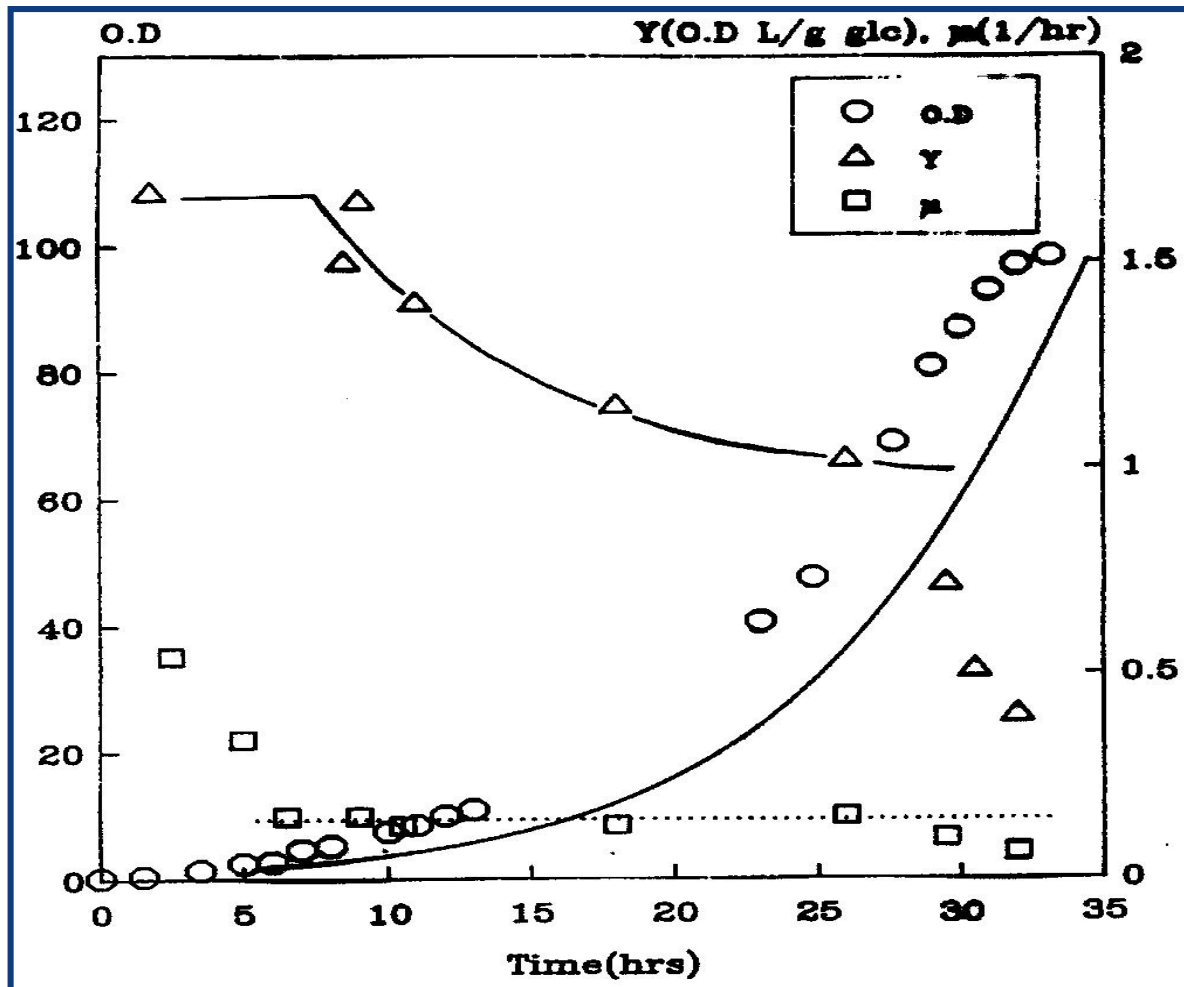
$$\mu = \frac{\mu_m S}{K_S + S}$$

# Exponential Feeding

$$F = \frac{X_0 \times V_0 \times \mu \times e^{\mu t}}{S_F \times Y}$$



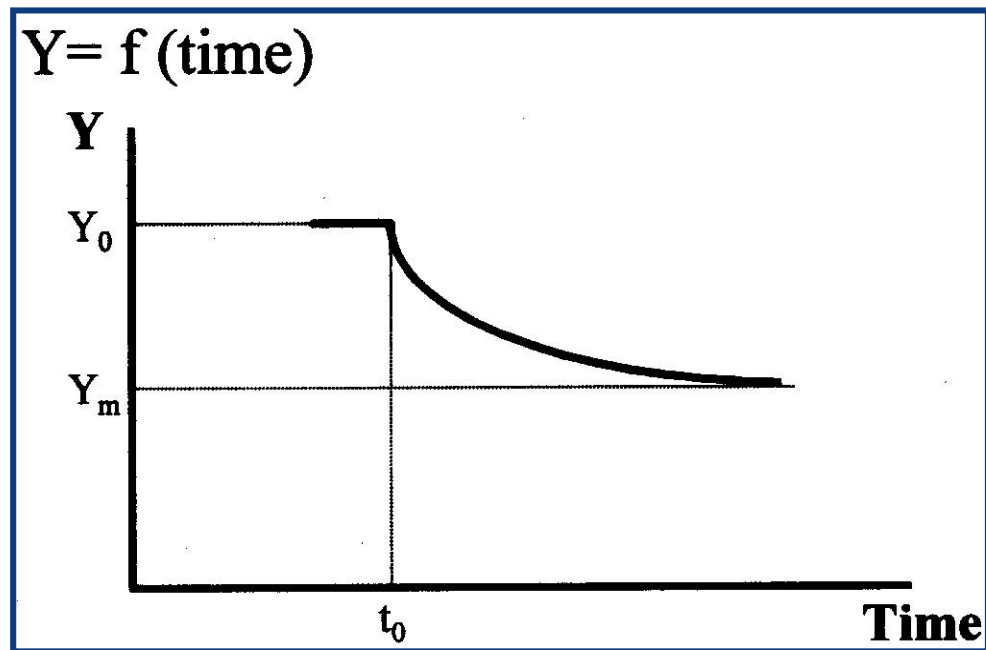
# Fed-Batch Operation



# Growth Yield

**Yield**

**Time Variable**



# Growth Yield

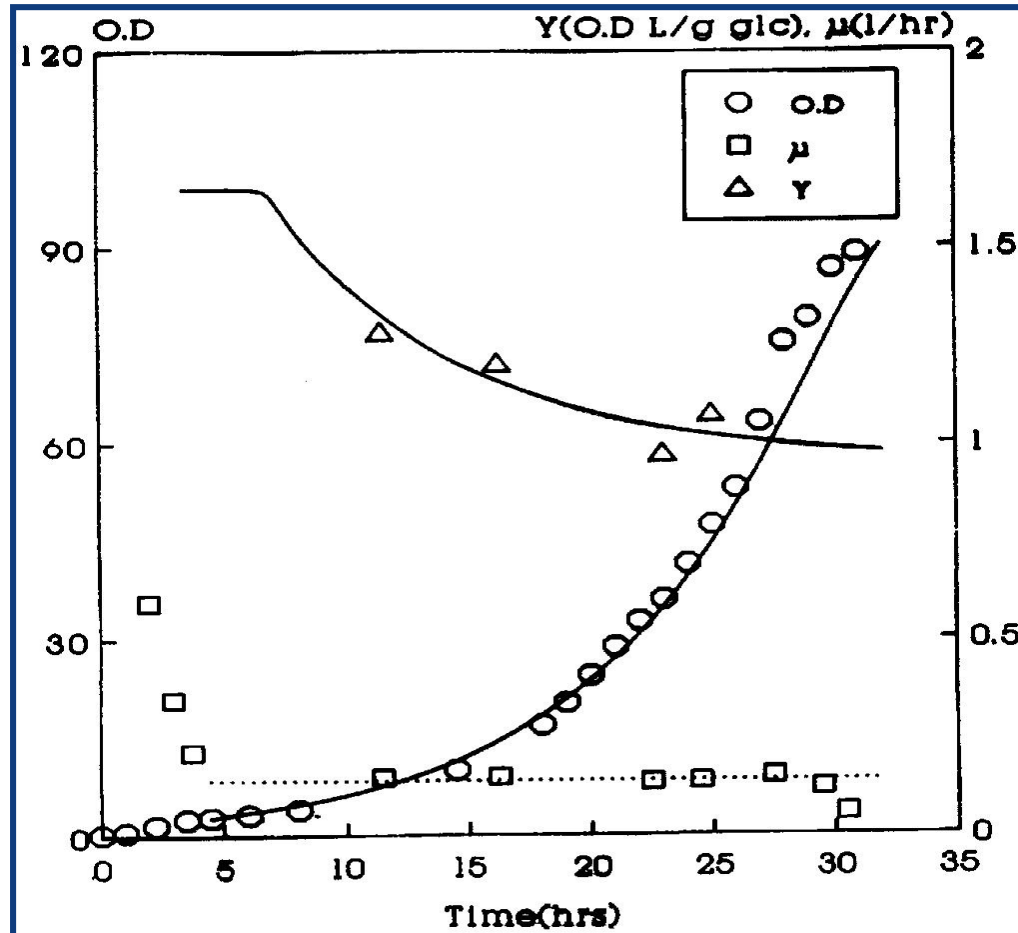
**Yield**

**Time Variable**

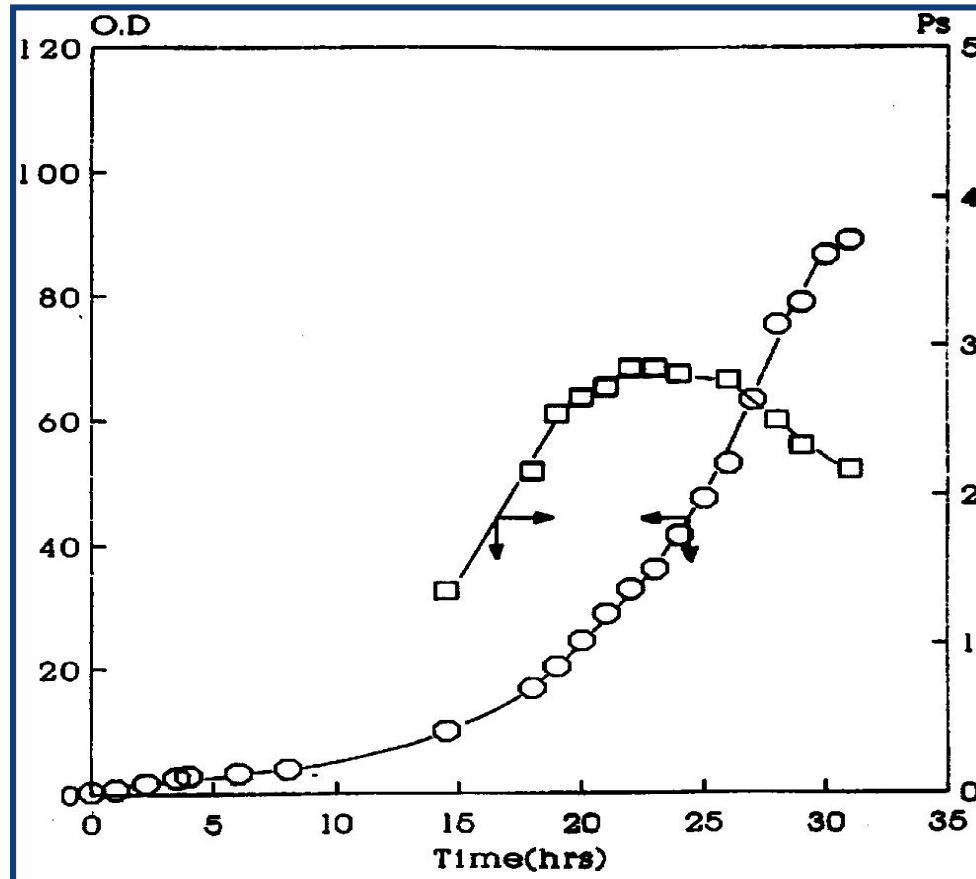
$$\frac{dY}{dt} = \frac{1}{ty} (Ym - Y), t = t_0, Y = Y_0$$

$$Y = 0.7 \text{Exp} \{ -(t - 8) / 8 \} + 0.95$$

# Fed-Batch Operation



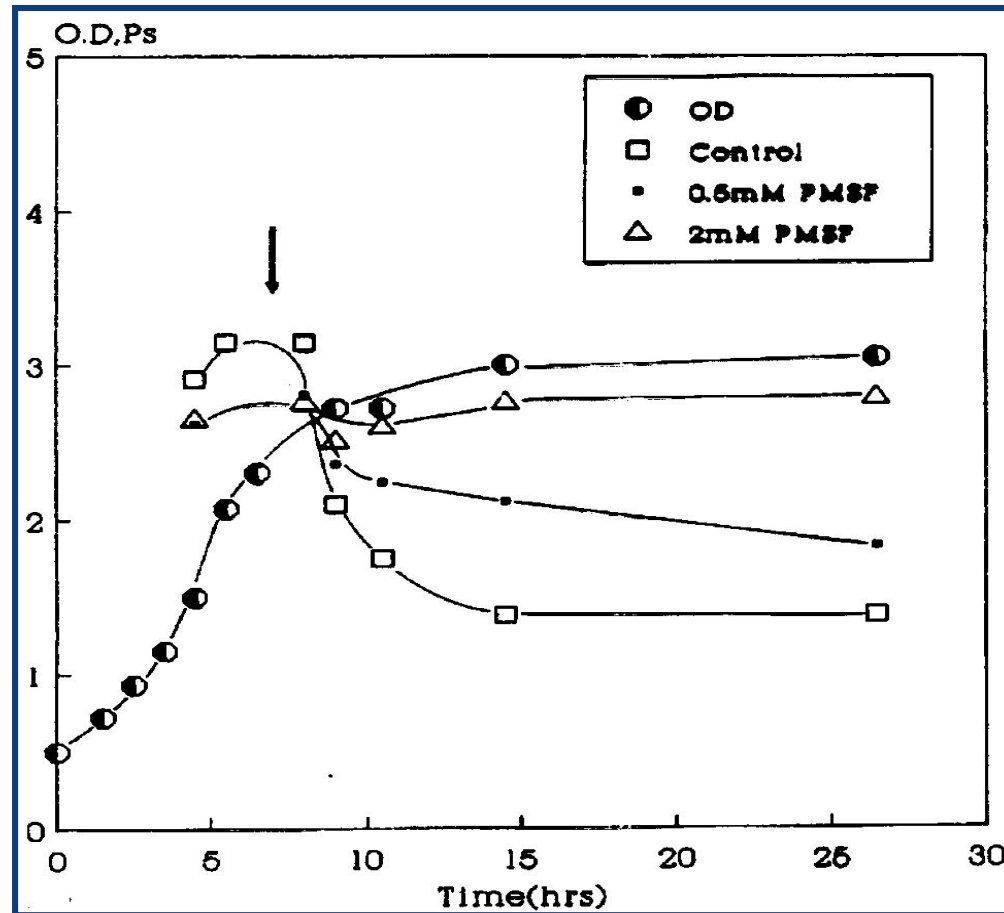
# Fed-Batch Operation



# Why does the specific expression rate decrease with the increase of cell density?

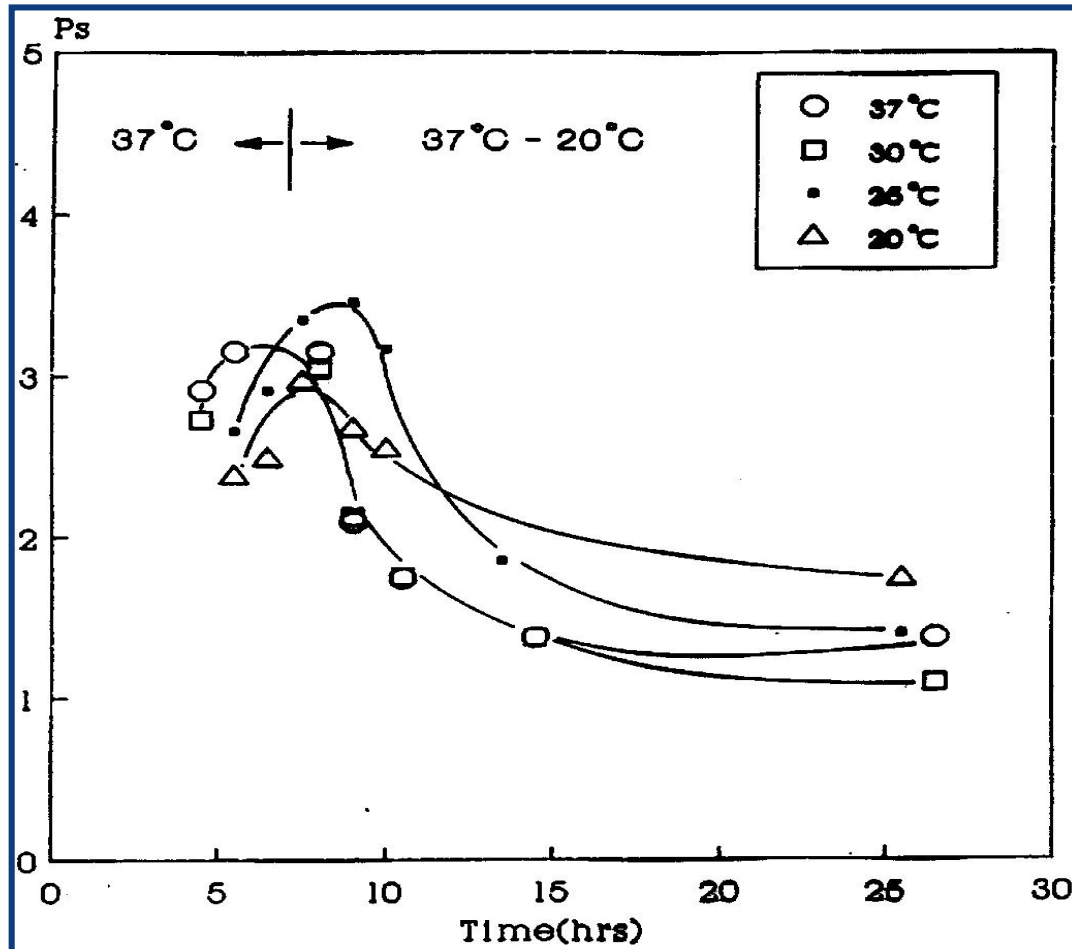
1.  $P_{O_2}$  limitation
  2. Glucose accumulation
  3. Acetic acid accumulation
  4. N source limitation
  5. P source limitation
  6.  $MgSO_4$  limitation
  7. Plasmid instability
  8. Degradation by protease
- Low  $\mu$ ,  
Slow feeding,  
Pure oxygen
- Ammonium phosphate  
feeding
- $MgSO_4$  feeding
-

# Effect of PMSF on Protein Degradation.



PMSF (Phenyl Methane Sulfonyl Fluoride)

# Effect of Culture Temperature on Protein Degradation





# Product Degradation by Protease

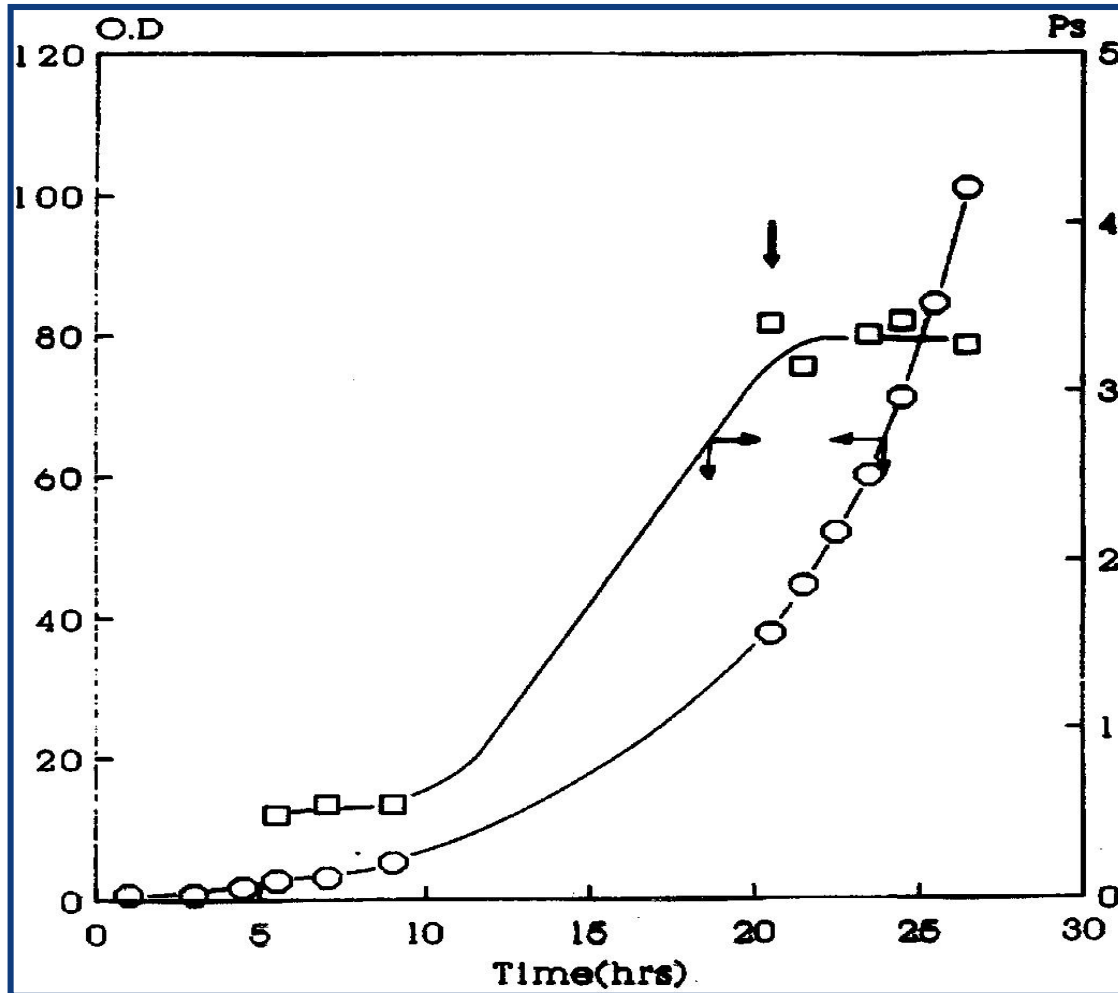
- Protease is induced under stressful conditions

- Depletion of Carbon or Nitrogen source
- High Temperature
- Expose to ethanol, UV

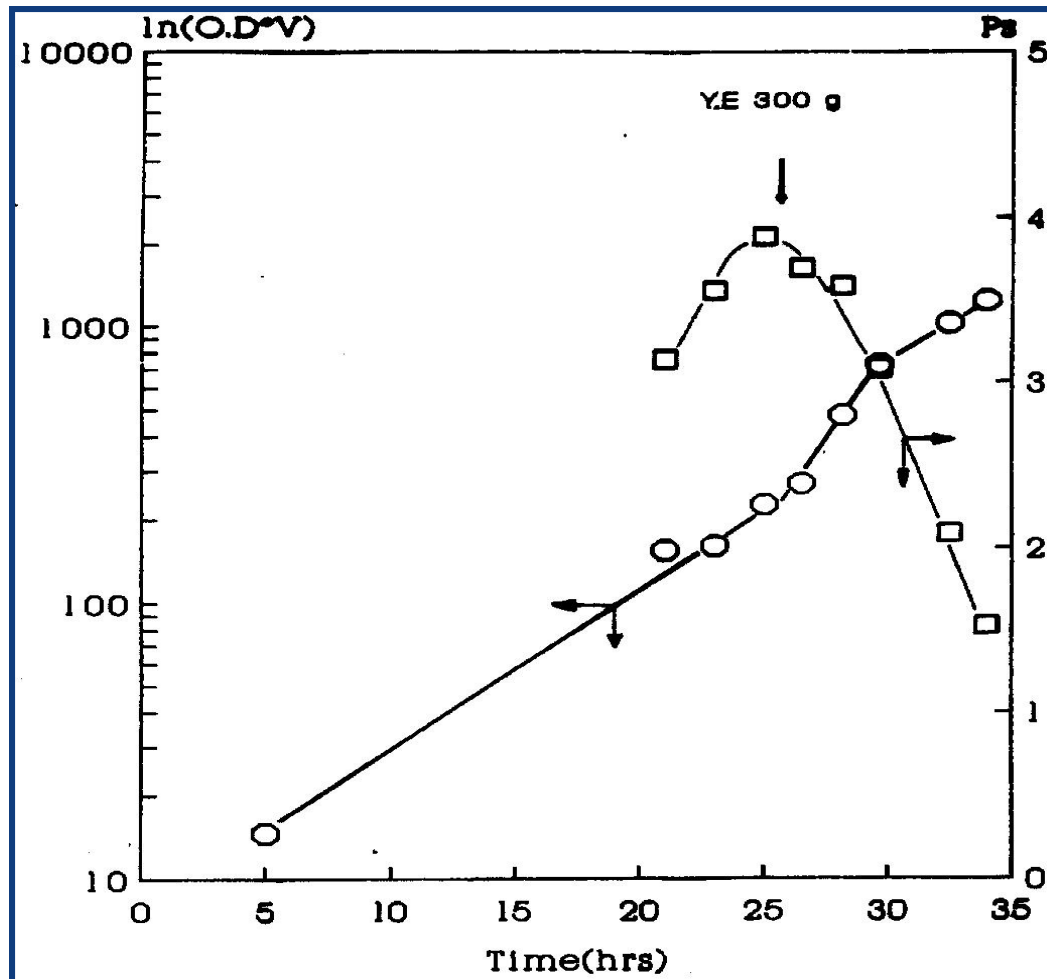
# Composition of Modified Medium

| Component  | Concentration   |                  |                  |
|--|-----------------|------------------|------------------|
|  | Starting medium | Feeding medium 1 | Feeding medium 2 |
| Yeast Extract (g/L)  | 1.0             | -                | 100              |
| $\text{KH}_2\text{PO}_4$ (g/L)                             | 15.0            | -                | -                |
| $\text{MgSO}_4 \cdot 7\text{H}_2\text{O}$ (g/L)            | 4.0             | -                | 15.5             |
| Glucose  | 2.0             | 400              | 400              |
| $\text{FeSO}_4 \cdot 7\text{H}_2\text{O}$ (mg/L)           | -               | 200              | 200              |
| $\text{CaCl}_2 \cdot 2\text{H}_2\text{O}$ (mg/L)           | -               | 1300             | 1300             |
| $\text{MnSO}_4 \cdot 5\text{H}_2\text{O}$ (mg/L)           | -               | 67               | 67               |
| $\text{CoCl}_2 \cdot 6\text{H}_2\text{O}$ (mg/L)           | -               | 13               | 13               |
| $\text{ZnSO}_4 \cdot 7\text{H}_2\text{O}$ (mg/L)           | -               | 67               | 67               |
| $\text{CuCl}_2 \cdot 5\text{H}_2\text{O}$ (mg/L)           | -               | 13               | 13               |
| $\text{Na}_2\text{MoO}_4 \cdot 2\text{H}_2\text{O}$ (mg/L) | -               | 13               | 13               |

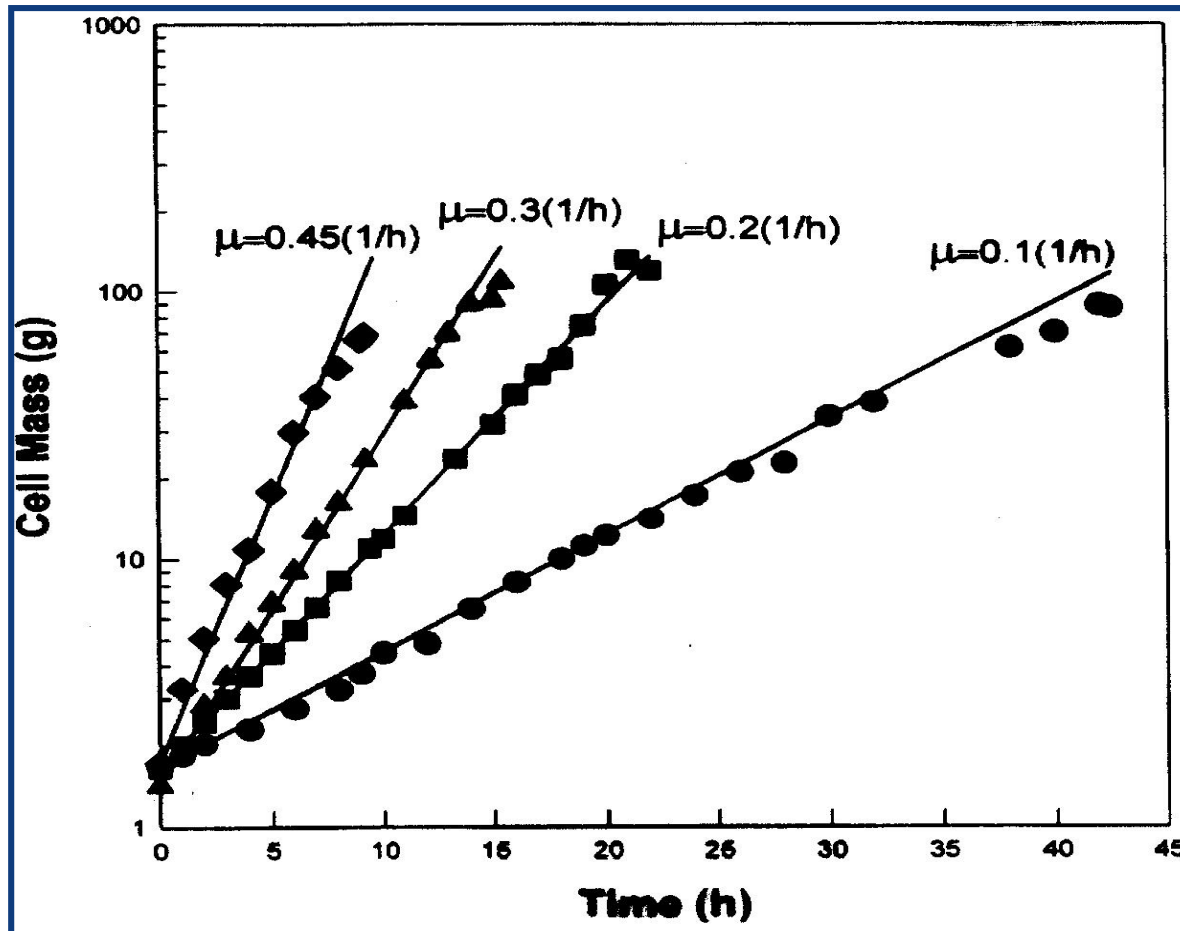
# Fed-Batch Operation with YE



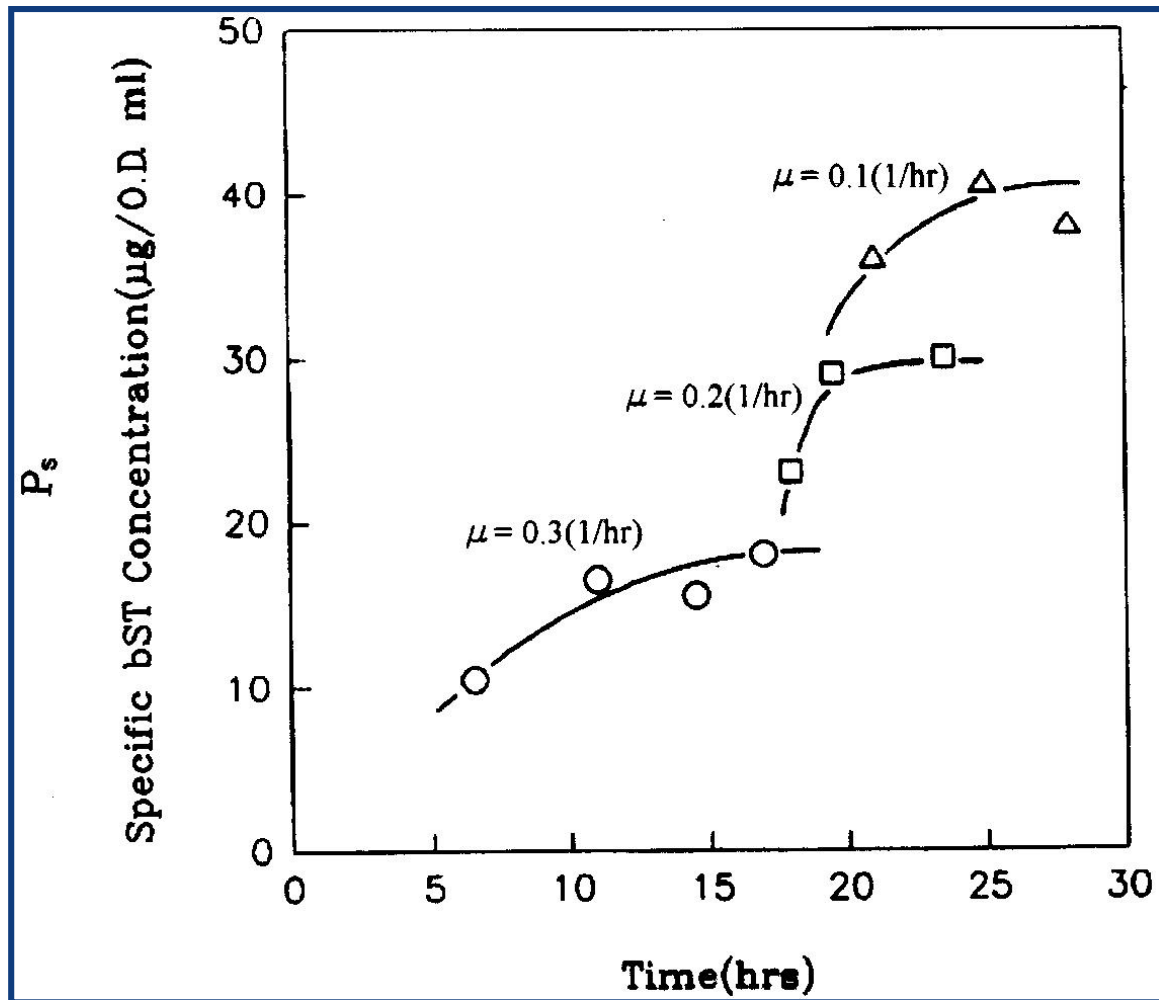
# Fed-Batch Operation with YE



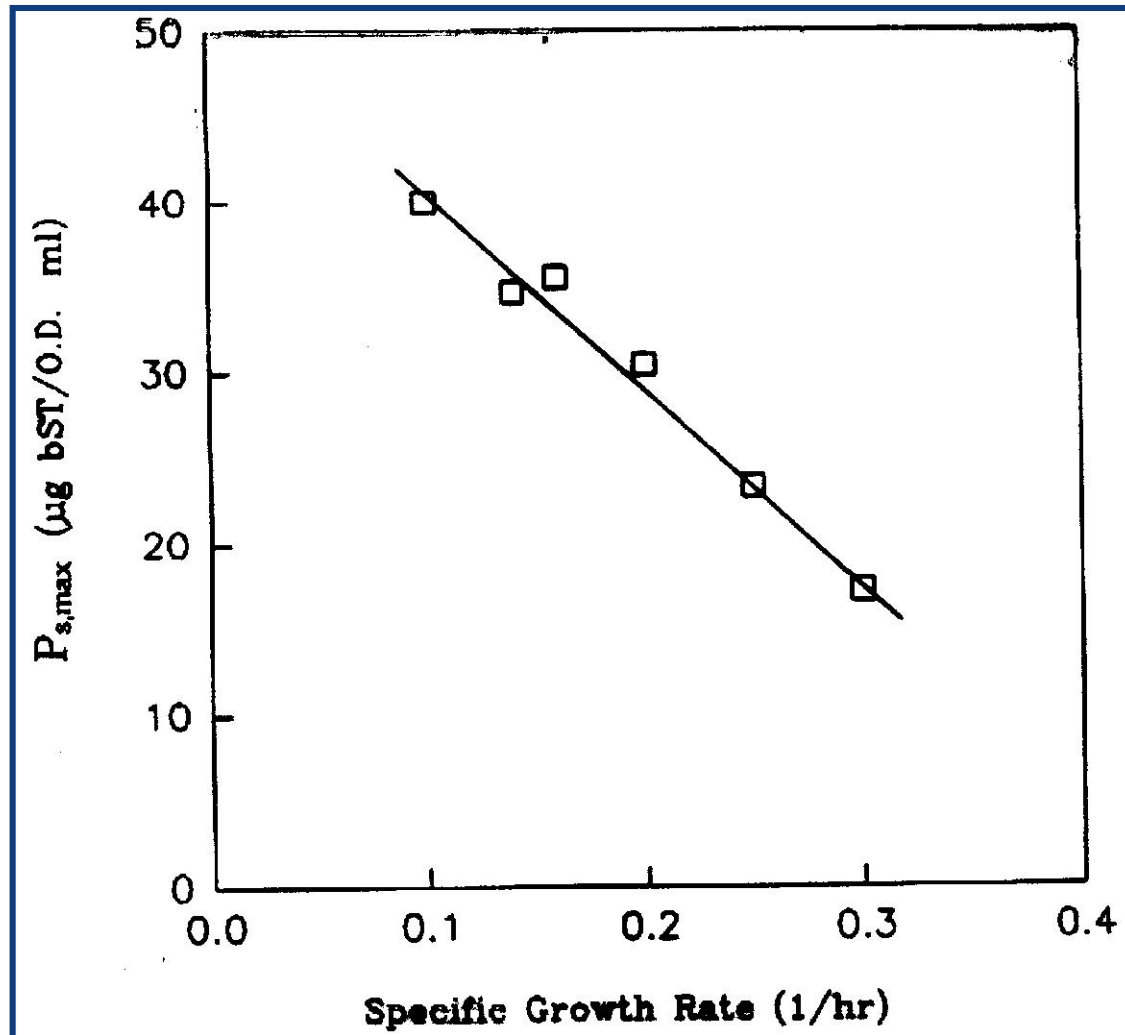
# Fed-Batch Operation with Controlled Specific Growth Rate



# Fed-Batch Operation with Controlled Specific Growth Rate



# Effect of Specific Growth Rate on Expression



# Productivity Maximization

$$P_{s,max} = -13.2\mu + 5.96$$

$$Pd = \frac{XP_{s,max}}{t}$$

$$[XV = X_0V_0e^{\mu t} \longrightarrow t = \frac{1}{\mu} \ln\left(\frac{XV}{X_0V_0}\right)]$$

$$= \frac{X\mu P_{s,max}}{\ln\left(\frac{XV}{X_0V_0}\right)}$$

- *Maximization of Pd*

→ *Maximization of  $(\mu P_{s,max})$*

$$\mu P_{s,max} = -13.2\mu^2 + 5.96\mu$$

Optimum  $\mu = 0.23$  (1/hr)



# Optimum Specific Growth Rate for Maximum Productivity

