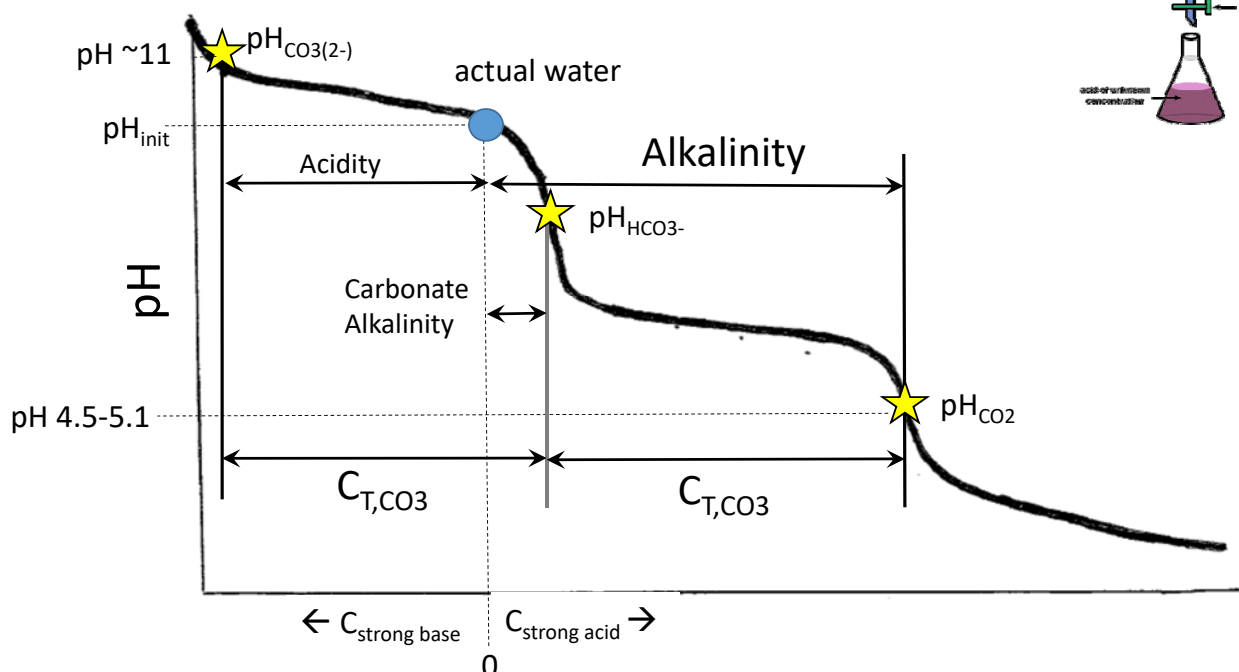


Advanced Water Quality

Class 16: Coordination Chemistry

Review of last week

- Analytical definitions of alkalinity and acidity = concentration of strong acid (alkalinity) or strong base (acidity) required to titrate solution to the carbonate equivalence points.



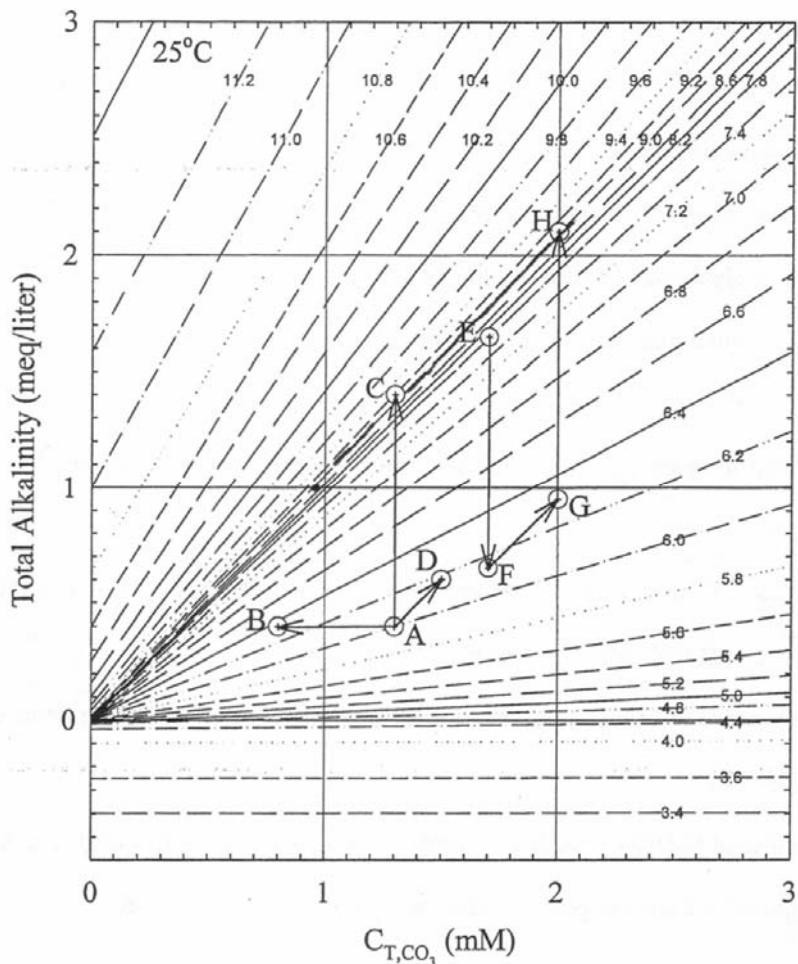
Chemical Definition of Alkalinity

If we assume carbonate acid/base chemistry dominates (90% of natural waters)

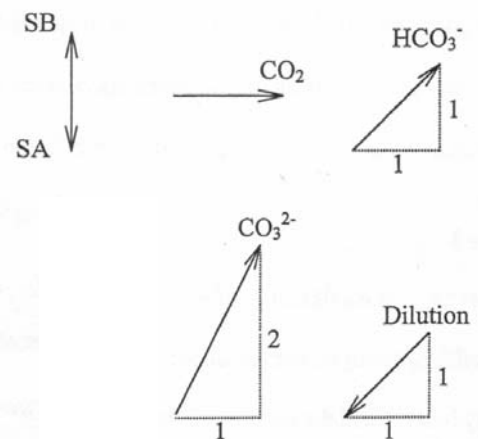
$$\text{Tot ALK (eq/L)} = \underbrace{\sum[\text{BC}]}_{\text{ANC to pH}_{\text{CO}_2}} - \underbrace{\sum[\text{SA}]}_{\text{Inert ion "imbalance"}} = \underbrace{[\text{HCO}_3^-] + 2[\text{CO}_3^{2-}] + [\text{OH}^-] - [\text{H}^+]}_{\text{Sum of titratable bases to pH}_{\text{CO}_2}}$$

Implications of $\text{ALK} = \sum[\text{BC}] - \sum[\text{SA}]$

- No change in ALK when CO_2 transfers to/from water
- Increase ALK by adding a salt the increases $\sum[\text{BC}]$ more than $\sum[\text{SA}]$
- Decrease ALK by adding substance that increases $\sum[\text{SA}]$ more than $\sum[\text{BC}]$



Deffeyes Diagram



Prob 6: The sourcewater entering a drinking water treatment plant has pH 5.8 and alkalinity of 0.2 meq/L.

(a) What will be the new alkalinity and pH if 53 mg/L of soda ash (Na_2CO_3 -MW: 106) is added to the sourcewater?

$$[\text{Na}_2\text{CO}_3] = 53 \text{ mg}/106 = 0.5 \text{ mM}$$

At pH 5.8, $\text{ALK} \cong [\text{HCO}_3^-] = \alpha_1 C_{T,\text{CO}_3}$ where $\alpha_1 = 0.22$

$$C_{T,\text{CO}_3} = 9.1 \times 10^{-4} \text{ M}$$

$$C_{T,\text{final}} = 9.1 \times 10^{-4} \text{ M} + 5 \times 10^{-4} \text{ M} = 1.41 \times 10^{-3} \text{ M}$$

$$\text{ALK}_{\text{final}} = \text{ALK}_{\text{init}} + \text{ALK}_{\text{Na}_2\text{CO}_3} = 0.2 \text{ meq/L} + 2 \times 0.5 \text{ meq/L} = 1.2 \times 10^{-3} \text{ M}$$

pH = 7.1 from new C_T and ALK

Today's NEW Topic

- The aqueous chemistry of metal ions
 1. Coordination chemistry concepts and terms
 2. Factors affecting the strength of metal-ligand interactions
 3. Describing metal-ligand complexation equilibria complexes
 1. Metal-ligand complexation
 2. Metal ion hydrolysis – formation of dissolved $\text{M}(\text{OH})_x^y$ complexes
 3. Solving complexation Equilibria

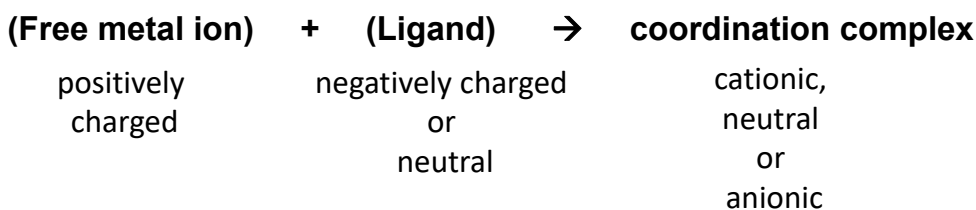
Coordination chemistry and metal speciation

Periodic Table of the Elements

The periodic table shows elements from Hydrogen (1) to Oganesson (118). It includes the Lanthanide Series (57-71) and Actinide Series (89-103). A legend at the bottom identifies the color-coded groups: Alkali Metal, Alkaline Earth, Transition Metal, Basic Metal, Semimetals, Nonmetals, Halogens, Noble Gas, Lanthanides, and Actinides.

Coordination chemistry

In aqueous systems, metal ions are present as coordination complexes with ligand molecules



Metal	Ligand × CN	Coordination complex
Mg ²⁺	H ₂ O × 6	Mg(H ₂ O) ₆ ²⁺
Co ²⁺	Cl ⁻ × 4	CoCl ₄ ²⁻
Ni ²⁺	OH ⁻ × 1 + H ₂ O × 5	Ni(OH)(H ₂ O) ₅ ⁺
Pd ²⁺	PPh ₃ × 2, Cl ⁻ × 2	Pd(PPh ₃) ₂ Cl ₂
Mn ⁷⁺	O ²⁻ × 4	MnO ₄ ⁻

Coordination number (CN):
of metal-ligand coordination bond from the central metal ion.

Metal Ion-Ligand Coordination Bonds

- Lewis acid (e^- pair acceptor) – base (e^- pair donor) interactions
- Ligands are Lewis bases (have free e^- pair to donate to form coordination bond)
- Metal ions are Lewis acids (have empty orbitals to accept e^- pair to form coordination bond)

Common ligands in environmental chemistry

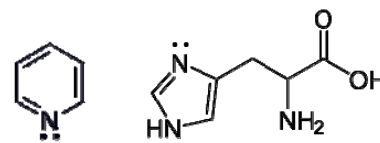
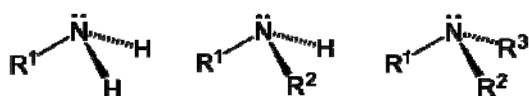
Halide ions: F^- , **Cl^-** , Br^- , I^-

O-donors: **H_2O** , **OH^-** , CO_3^{2-} , SiO_4^{4-} , PO_4^{3-} , SO_4^{2-}

carboxylates ($R-COO^-$), phenolates (PhO^-)

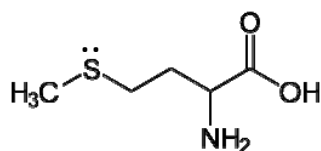
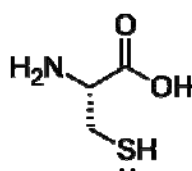
N-donors: NH_3

amines ($R-NH_2$, R_2NH , R_3N), heterocyclic N (e.g. pyridine, imidazole)

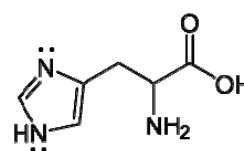


S-donors: H_2S , HS^-

cysteine, methionine

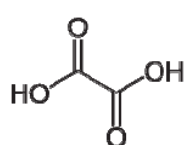


histidine

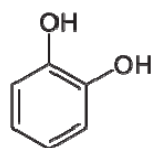


Ligands also classified by the number of metal binding sites they possess

- Monodentate – single binding site
- Multidentate – bond to metal simultaneously with multiple donor e⁻ pairs



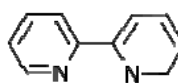
oxalate



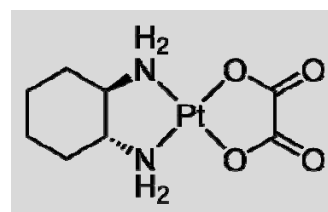
catechol



ethylenediamine
(en)

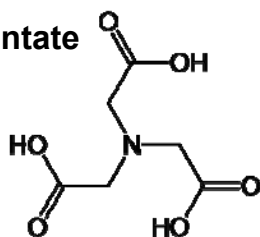


2,2'-bipyridine
(bpy)

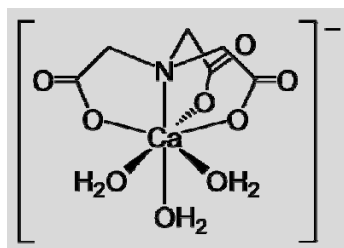


- Chelating agents – form very strong multidentate complexes with metal ions

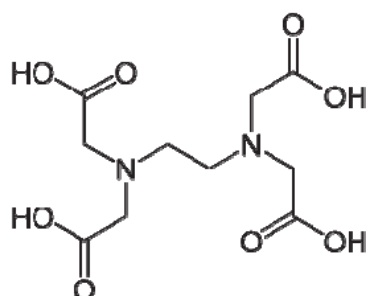
Tetradentate



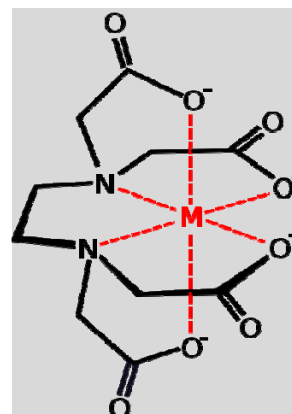
Nitrilotriacetic acid
(NTA)



Hexadentate



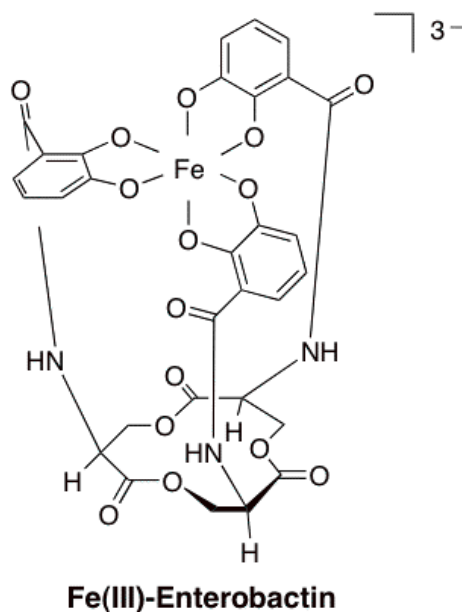
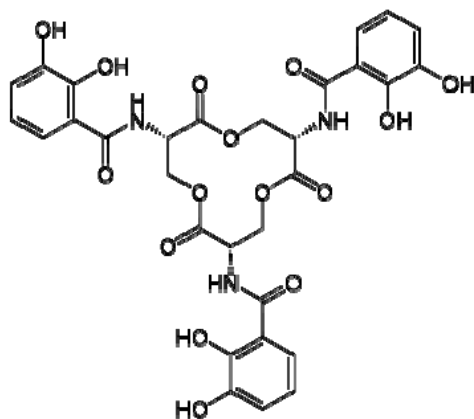
Ethylenediaminetetraacetic acid
(EDTA)



Multidentate ligands in nature

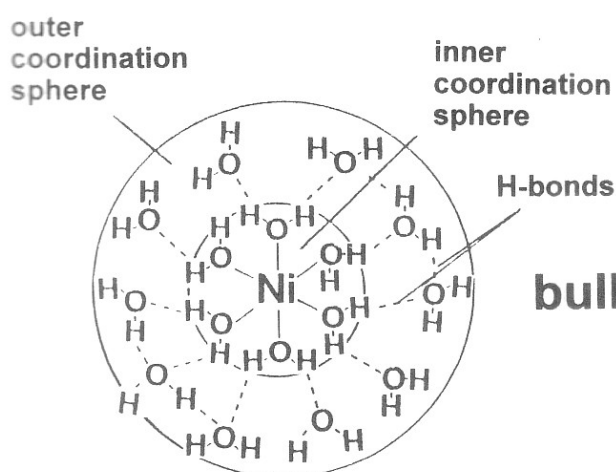
Siderophores (Greek: "iron carrier") are small, high-affinity iron chelating compounds secreted by microorganisms.

Enterobactin is the strongest siderophore known to bind Fe^{3+}
 ($K_{\text{ent-Fe}} = 10^{52}$, compared to $K_{\text{EDTA-Fe}} \sim 10^{25}$ compared to $K_{\text{acetate-Fe}} \sim 10^4$)



Metal ions in aqueous solution

- Typically represent metal ions such as Ni^{2+} as though they are bare ions
- Reality – Ni^{2+} is coordinated to multiple H_2O molecules by default



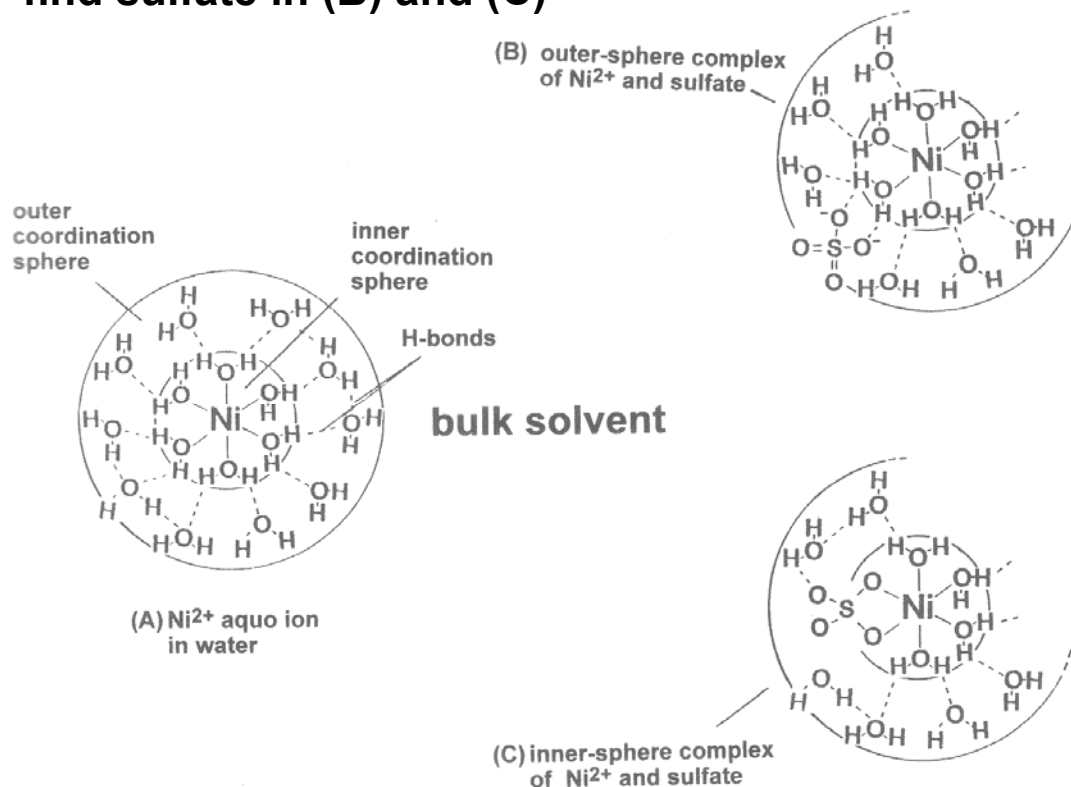
“Free ion” species
 “Hexaquo” species
 “Hydrated” species

bulk solvent

Ni^{2+} is formally $\text{Ni}(\text{H}_2\text{O})_6^{2+}$

Outer- versus Inner-Sphere Complexes

-find sulfate in (B) and (C)



Metal-ligand complexation equilibria

- Ligand exchange with coordinated H_2O typically shown without formally showing the coordinated H_2O molecules

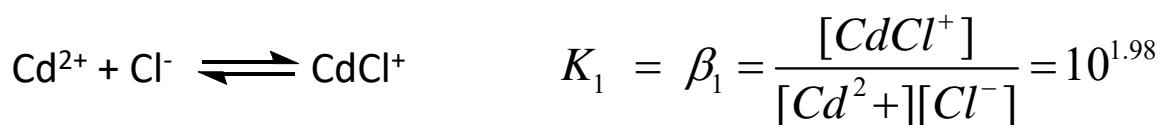


$$K_1 \text{ and } \beta_1 = \frac{[\text{CdCl}^+]}{[\text{Cd}^{2+}][\text{Cl}^-]} = 10^{1.98}$$

- Likewise, we can consider stepwise formation of higher order Cd(II) complexes with Cl⁻ (like stepwise deprotonation)



- Alternatively, we often find it useful to write the expressions in terms of complex formation from the “component” species:



$$C_{\text{T,Cd}} = [\text{Cd}^{2+}] + [\text{CdCl}^+] + [\text{CdCl}_2] + [\text{CdCl}_3^-]$$

$$C_{\text{T,Cl}} = [\text{Cl}^-] + [\text{CdCl}^+] + 2[\text{CdCl}_2] + 3[\text{CdCl}_3^-]$$

- ▶ This is the form used by programs like Visual Minteq

Problem: Determine the concentration of each Cd species with 0.01 M Cd²⁺ is added to a salt brine containing 2.0 M Cl⁻. *Neglect ionic strength and pH effects for this problem.*

Simplification:

[Cl⁻] is the dominant species of C_{T,Cl} (thus it is 2.0 M)

Metal ion hydrolysis

- H₂O is the default ligand in aqueous solution



- Hydrolysis = splitting of water (H₂O → OH⁻ + H⁺)
- Metal ion hydrolysis: metal ion promotes splitting of coordinated water molecules
- Metal ion hydrolysis stoichiometry: metal ions acting like Bronsted acids (i.e., H⁺ donor)

- Metal ions promote hydrolysis of coordinated H₂O mCs because M-O bond weakens the O-H bond
 - makes coordinated H₂O more acidic than H₂O mCs in bulk solution
- Most metal ions can only promote donation of 1 proton from each coordinated water

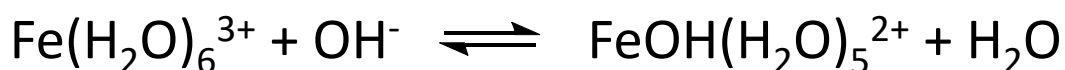


- Some metal ions have such strong M-O interactions that both H⁺ are donated to solution, forming “oxyanion” metals:



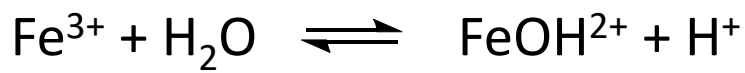
Metal ion hydrolysis equilibria represented in different ways

1. Ligand exchange reaction between OH⁻ from bulk solution and a metal-coordinated H₂O molecule:



$$K_1 = \frac{[\text{FeOH}^{2+}]}{[\text{Fe}^{3+}][\text{OH}^-]} = 10^{11.81}$$

2. Transfer of a H^+ from a coordinated H_2O molecule to a bulk H_2O molecule (reality):



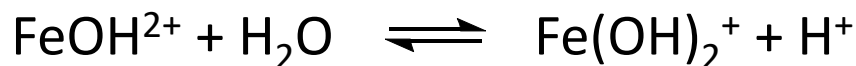
$$^*K_1 = \frac{[FeOH^{2+}][H^+]}{[Fe^{3+}]}$$

*K_1 and K_1 values related by $K_w = [H^+][OH^-]$

$$^*K_1 = K_1 K_w = \frac{[FeOH^{2+}]}{[Fe^{3+}][OH^-]} \times [H^+][OH^-]$$

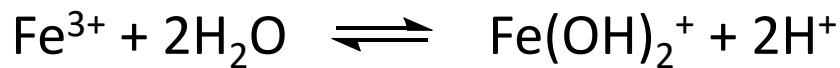
$$^*K_1 = 10^{11.81} 10^{-14} = 10^{-2.19}$$

Formation of complexes with multiple coordinated OH^- can be represented in successive steps (like acid-base pKa values)



$$^*K_2 = \frac{[Fe(OH)_2^+][H^+]}{[FeOH^{2+}]} = 10^{-3.48}$$

Or we can represent as complex formation from component species (M^{n+} , H^+):



$${}^*\beta_2 = {}^*K_2 \times {}^*K_1 = \frac{[Fe(OH)_2^+][H^+]^2}{[Fe^{3+}]}$$

$${}^*\beta_2 = 10^{-5.67}$$

Similarly, we can represent successive complexation of OH^- (K_1 , K_2 , ...) or complex formation from M^{n+} and OH^- (β_1 , β_2 , ...)

How does the percentage of hydrolyzed species vary with changing pH conditions?

$${}^*\beta_x = \frac{[Fe(OH)_x^+][H^+]^x}{[Fe^{3+}]}$$

When pH increases,

- OH complex of metal increases.

When pH decreases,

- OH complex of metal decreases.

Can generate "rough" pC-pH diagram for metal ion hydrolysis by same rules we previously learned using the p^*K_i values

- Recall *K_i values are for successive proton donation steps

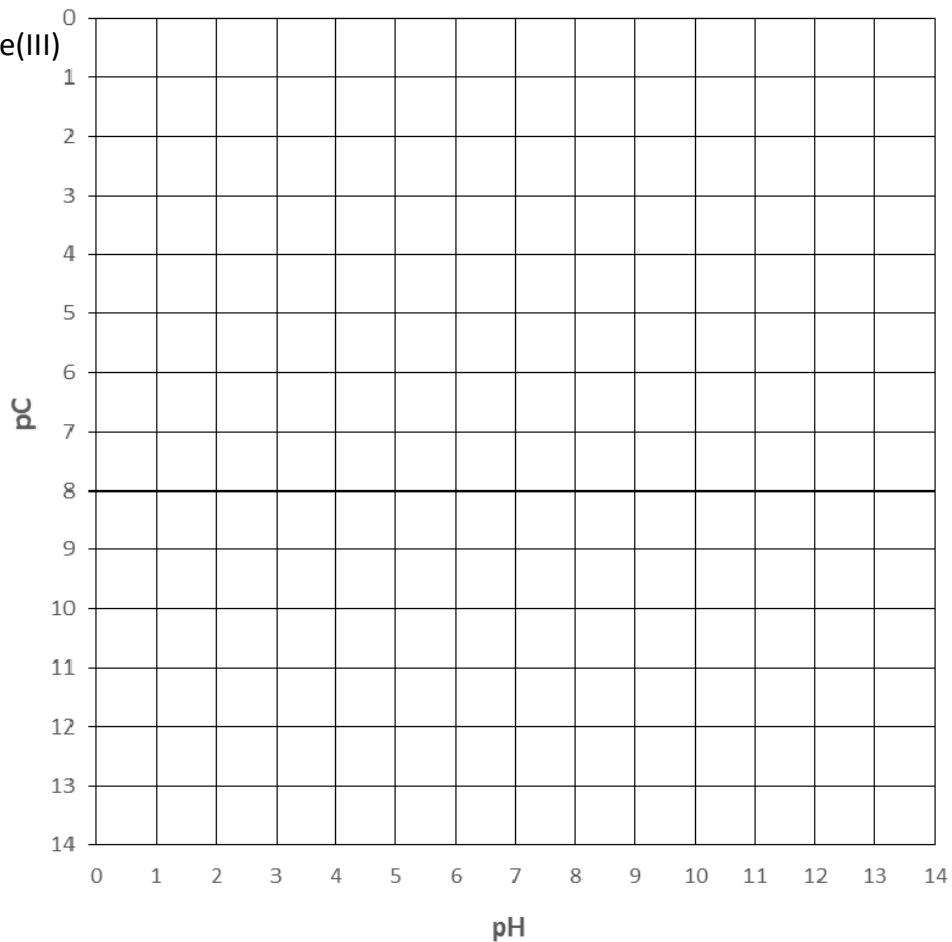
E.g., for 10^{-3} M Fe(III)

$$*K_1 = 10^{-2.19}$$

$$*K_2 = 10^{-3.48}$$

$$*K_3 = 10^{-7.93}$$

$$*K_4 = 10^{-8.00}$$



Can use mass balance with $*\beta_i$ expressions to solve for $[Fe^{3+}]$ as a master variable at each pH condition, then use $*\beta_i$ expressions to calculate $[Fe(OH)_x^y]$

$$C_{T,Fe(III)} = [Fe^{3+}] + [FeOH^{2+}] + [Fe(OH)_2^+] + [Fe(OH)_3^0] + [Fe(OH)_4^-]$$

$$C_{T,Fe(III)} = [Fe^{3+}] \left(1 + \frac{* \beta_1}{[H^+]} + \frac{* \beta_2}{[H^+]^2} + \frac{* \beta_3}{[H^+]^3} + \frac{* \beta_4}{[H^+]^4} \right)$$

$$\therefore [Fe^{3+}] = \frac{C_{T,Fe(III)}}{\left(1 + \frac{* \beta_1}{[H^+]} + \frac{* \beta_2}{[H^+]^2} + \frac{* \beta_3}{[H^+]^3} + \frac{* \beta_4}{[H^+]^4} \right)}$$

Plug this into Excel, vary pH, calculate $[Fe^{3+}]$

Then use $[Fe^{3+}]$ and $[H^+]$ at each pH condition to calculate $[Fe(OH)_x^y]$

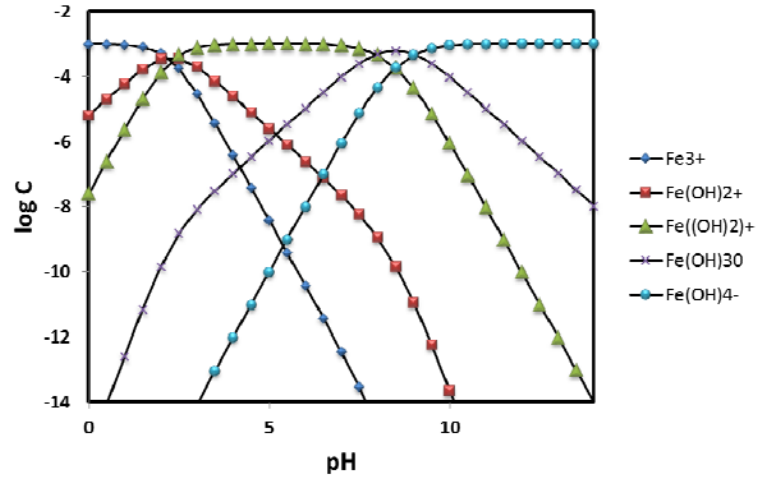
$$[FeOH^{2+}] = \frac{* \beta_1 [Fe^{3+}]}{[H^+]}$$

$$[Fe(OH)_3^0] = \frac{* \beta_3 [Fe^{3+}]}{[H^+]^3}$$

$$[Fe(OH)_2^+] = \frac{* \beta_2 [Fe^{3+}]}{[H^+]^2}$$

$$[Fe(OH)_4^-] = \frac{* \beta_4 [Fe^{3+}]}{[H^+]^4}$$

	CT,Fe	1.00E-03																		
	b1	6.50E-03																		
	b2	2.55E-05																		
	b3	2.7542E-13																		
	b4	2.5823E-22																		
pH	[H+]	[OH-]	Fe3+	Fe(OH)2+	Fe((OH)2)+	Fe(OH)30	Fe(OH)4-		pH	Fe3+	Fe(OH)2+	Fe((OH)2)+	Fe(OH)30	Fe(OH)4-						
0	1	1E-14	0.00099352	6.45914E-06	2.53032E-08	2.73637E-16	2.56552E-25		0	-3.0028253	-5.1898253	-7.5968253	-15.562825	-24.590825						
0.5	0.31623	3.162E-14	0.00097961	2.01397E-05	2.4949E-07	8.53205E-15	2.52961E-23		0.5	-3.0089464	-4.6959464	-6.6029464	-14.068946	-22.596946						
1	0.1	1E-13	0.00093672	6.08987E-05	2.38566E-06	2.57993E-13	2.41884E-21		1	-3.0283922	-4.2153922	-5.6223922	-12.588392	-20.616392						
1.5	0.03162	3.162E-13	0.00081231	0.000167002	2.06882E-05	7.07492E-12	2.0976E-19		1.5	-3.0902783	-3.7772783	-4.6842783	-11.150278	-18.678278						
2	0.01	1E-12	0.00052499	0.000341309	0.000133705	1.44593E-10	1.35565E-17		2	-3.2798523	-3.4668523	-3.8738523	-9.8398523	-16.867852						
2.5	0.00316	3.162E-12	0.00017848	0.000366944	0.00045457	1.55453E-09	4.60893E-16		2.5	-3.7483997	-3.4353997	-3.3423997	-8.8083997	-15.3364						
3	0.001	1E-11	3.0331E-05	0.000197189	0.000772472	8.35377E-09	7.83218E-15		3	-4.5181173	-3.7051173	-3.1121173	-8.0781173	-14.106117						
3.5	0.00032	3.162E-11	3.6199E-06	7.44212E-05	0.000921927	3.1528E-08	9.34753E-14		3.5	-5.4413033	-4.1283033	-3.0353033	-7.5013033	-13.029303						
4	0.0001	1E-10	3.8268E-07	2.48795E-05	0.000974632	1.054E-07	9.88191E-13		4	-6.4171591	-4.6041591	-3.0111591	-6.9771591	-12.005159						
4.5	3.2E-05	3.162E-10	3.8935E-08	8.00468E-06	0.000991617	3.39113E-07	1.00541E-11		4.5	-7.4096559	-5.0966559	-3.0036559	-6.4696559	-10.997656						
5	0.00001	1E-09	3.9122E-09	2.54345E-06	0.000996375	1.07751E-06	1.01024E-10		5	-8.4075772	-5.5945772	-3.0015772	-5.9675772	-9.9955772						
5.5	3.2E-06	3.162E-09	3.9099E-10	8.03836E-07	0.000995789	3.40539E-06	1.00964E-09		5.5	-9.4078325	-6.0948325	-3.0018325	-5.4678325	-8.9958325						
6	1E-06	1E-08	3.8834E-11	2.52473E-07	0.000989															
6.5	3.2E-07	3.162E-08	3.7959E-12	7.80405E-08	0.000966															
7	1E-07	0.0000001	3.5399E-13	2.30143E-08	0.000901															
7.5	3.2E-08	3.162E-07	2.9039E-14	5.97011E-09	0.000739															
8	1E-08	0.000001	1.7988E-15	1.16945E-09	0.000458															
8.5	3.2E-09	3.162E-06	7.2261E-17	1.48561E-10	0.000184															
9	1E-09	0.00001	1.7885E-18	1.16278E-11	4.55509E															
9.5	3.2E-10	3.162E-05	2.8746E-20	5.90995E-13	7.32123E															
10	1E-10	0.0001	3.4962E-22	2.273E-14	8.90429E															
10.5	3.2E-11	0.0003162	3.7459E-24	7.70109E-16	9.54008E															
11	1E-11	0.001	3.8317E-26	2.49108E-17	9.75861E															
11.5	3.2E-12	0.0031623	3.8596E-28	7.93482E-19	9.82963E															
12	1E-12	0.01	3.8684E-30	2.51499E-20	9.85229E															
12.5	3.2E-13	0.0316228	3.8713E-32	7.95891E-22	9.85947E															
13	1E-13	0.1	3.8722E-34	2.51741E-23	9.86174E															
13.5	3.2E-14	0.3162278	3.8724E-36	7.96132E-25	9.86246E															
14	1E-14	1	3.8725E-38	2.51765E-26	9.86269E															

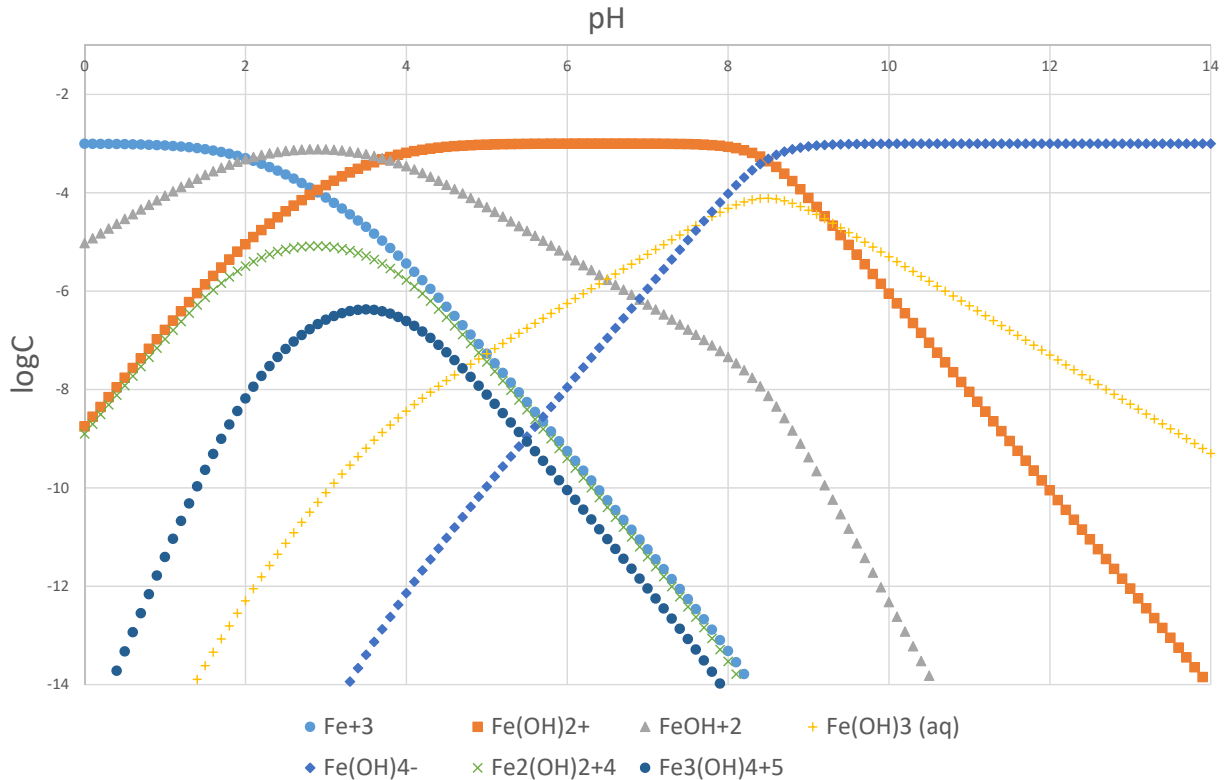


Visual MINTEQ - Selected sweep results

Problem no	pH	Fe ³⁺ Log Concentration	Fe(OH) ²⁺ Log Concentration	Fe(OH) ₃₀ Log Concentration	Fe(OH) ⁴⁻ Log Concentration
1	0.000	-3.004	8.754	5.034	-18.004
2	0.100	-3.005	8.555	4.925	-17.705
3	0.200	-3.007	8.357	4.827	-17.407
4	0.300	-3.008	8.158	4.728	-17.108
5	0.400	-3.010	7.960	4.630	-16.810
6	0.500	-3.013	7.763	4.533	-16.513
7	0.600	-3.016	7.566	4.436	-16.216
8	0.700	-3.020	7.370	4.340	-15.920
9	0.800	-3.025	7.175	4.245	-15.625
10	0.900	-3.032	6.982	4.152	-15.332
11	1.000	-3.040	6.790	4.060	-15.040
12	1.100	-3.050	6.600	3.970	-14.750
13	1.200	-3.062	6.412	3.882	-14.462
14	1.300	-3.076	6.226	3.796	-14.176
15	1.400	-3.094	6.044	3.714	-13.894
16	1.500	-3.116	5.866	3.636	-13.616
17	1.600	-3.142	5.692	3.562	-13.342
18	1.700	-3.172	5.522	3.492	-13.072
19	1.800	-3.208	5.358	3.428	-12.808
20	1.900	-3.250	5.200	3.370	-12.550
21	2.000	-3.298	5.048	3.318	-12.298

Execution time (s): 21.07031

Visual Minteq - Hydrolysis of 10^{-3} M Fe(III)



Consider hydroxy complexes + complexes with other ligands
(e.g., 1 mM Fe(III) + 1 mM phosphate)

$$C_{T,Fe(III)} = [Fe^{3+}] + [FeOH^{2+}] + [Fe(OH)_2^+] + [Fe(OH)_3^0] + [Fe(OH)_4^-] + [FeH_2PO_4^{2+}] + [FeHPO_4^+]$$

$$C_{T,Fe(III)} = [Fe^{3+}] \left(1 + \frac{\beta_1^*}{[H^+]} + \frac{\beta_2^*}{[H^+]^2} + \frac{\beta_3^*}{[H^+]^3} + \frac{\beta_4^*}{[H^+]^4} + \beta_{FeH_2P} [H^+]^2 [PO_4^{3-}] + \beta_{FeHP} [H^+] [PO_4^{3-}] \right)$$

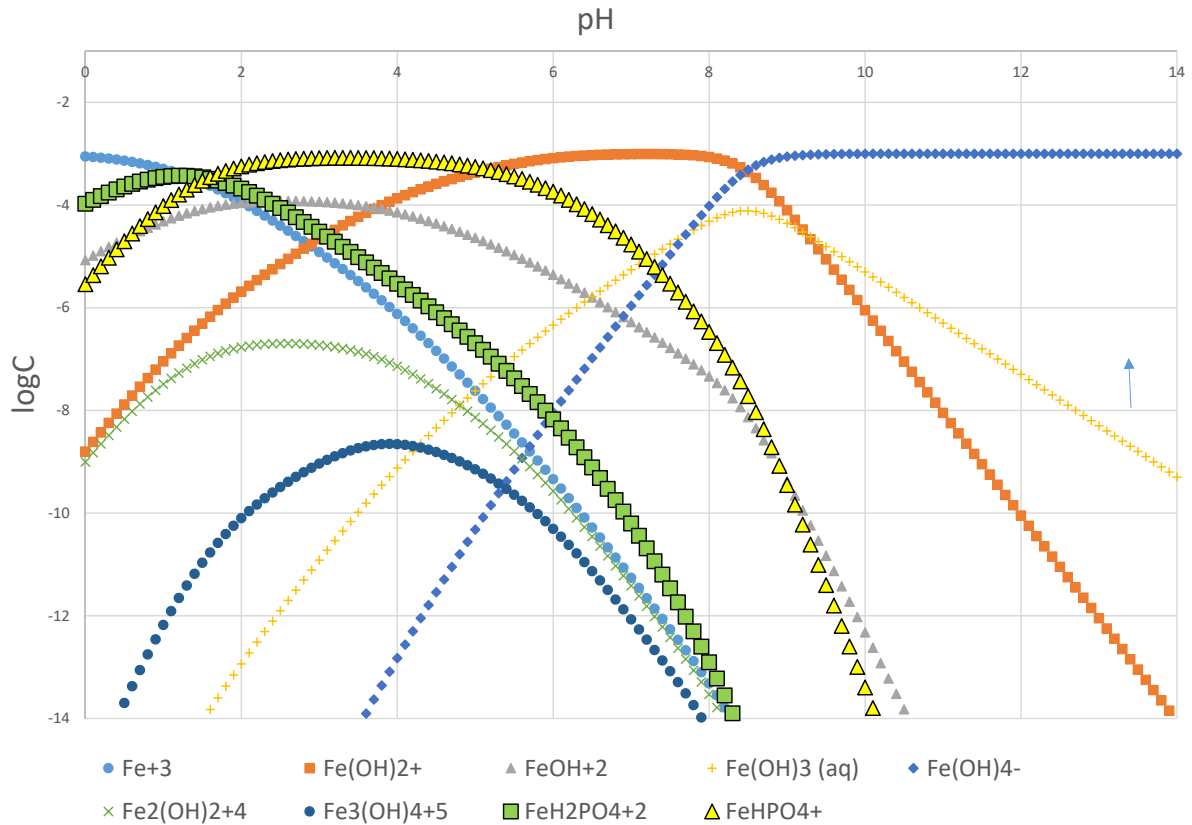
$$\therefore [Fe^{3+}] = \frac{C_{T,Fe(III)}}{\left(1 + \frac{\beta_1^*}{[H^+]} + \frac{\beta_2^*}{[H^+]^2} + \frac{\beta_3^*}{[H^+]^3} + \frac{\beta_4^*}{[H^+]^4} + \beta_{FeH_2P} [H^+]^2 [PO_4^{3-}] + \beta_{FeHP} [H^+] [PO_4^{3-}] \right)}$$

$$[FeOH^{2+}] = \frac{\beta_1^* [Fe^{3+}]}{[H^+]} \qquad [Fe(OH)_4^-] = \frac{\beta_4^* [Fe^{3+}]}{[H^+]^4}$$

$$[Fe(OH)_2^+] = \frac{\beta_2^* [Fe^{3+}]}{[H^+]^2} \qquad [FeHPO_4^+] = \beta_{FeHP} [Fe^{3+}] [H^+] [PO_4^{3-}]$$

$$[Fe(OH)_3^0] = \frac{\beta_3^* [Fe^{3+}]}{[H^+]^3} \qquad [FeH_2PO_4^{2+}] = \beta_{FeH_2P} [Fe^{3+}] [H^+]^2 [PO_4^{3-}]$$

Visual Minteq – Hydrolysis of 10^{-3} M Fe(III) + 1 mM phosphate



Consider hydroxy complexes + complexes with other ligands (e.g.,
1 mM Fe(III) + 1 mM phosphate)

$$C_{T,Fe(III)} = [Fe^{3+}] + [FeOH^{2+}] + [Fe(OH)_2^+] + [Fe(OH)_3^0] + [Fe(OH)_4^-] + [FeH_2PO_4^{2+}] + [FeHPO_4^+]$$

$$C_{T,Fe(III)} = [Fe^{3+}] \left(1 + \frac{\beta_1^*}{[H^+]} + \frac{\beta_2^*}{[H^+]^2} + \frac{\beta_3^*}{[H^+]^3} + \frac{\beta_4^*}{[H^+]^4} + \beta_{FeH_2P} [H^+]^2 [PO_4^{3-}] + \beta_{FeHP} [H^+] [PO_4^{3-}] \right)$$

$$\therefore [Fe^{3+}] = \frac{C_{T,Fe(III)}}{\left(1 + \frac{\beta_1^*}{[H^+]} + \frac{\beta_2^*}{[H^+]^2} + \frac{\beta_3^*}{[H^+]^3} + \frac{\beta_4^*}{[H^+]^4} + \beta_{FeH_2P} [H^+]^2 [PO_4^{3-}] + \beta_{FeHP} [H^+] [PO_4^{3-}] \right)}$$

$$[FeOH^{2+}] = \frac{\beta_1^* [Fe^{3+}]}{[H^+]}$$

$$[Fe(OH)_4^-] = \frac{\beta_4^* [Fe^{3+}]}{[H^+]^4}$$

$$[Fe(OH)_2^+] = \frac{\beta_2^* [Fe^{3+}]}{[H^+]^2}$$

$$[FeHPO_4^+] = \beta_{FeHP} [Fe^{3+}] [H^+] [PO_4^{3-}]$$

$$[Fe(OH)_3^0] = \frac{\beta_3^* [Fe^{3+}]}{[H^+]^3}$$

$$[FeH_2PO_4^{2+}] = \beta_{FeH_2P} [Fe^{3+}] [H^+]^2 [PO_4^{3-}]$$

How do I know $[PO_4^{3-}]$ as a function of pH?

Hint

- Is $C_{T,PO_4} \gg C_{T,Fe(III)}$ or is PO_4^{3-} a very weakly binding ligand?

Yes: Try assuming that the presence of Fe(III) has no significant effect on the dominant PO_4^{3-} speciation, and calculate $[PO_4^{3-}]$ as a function of pH with no Fe(III) present (*a simple acid-base calculation*)

No: Sorry, but very difficult to solve manually, need to use an iterative tool like Visual Minteq to solve.

Summary

- The aqueous chemistry of metal ions
 1. Coordination chemistry concepts and terms
 2. Metal-ligand complexation equilibria
 3. Metal ion hydrolysis
 4. Solving metal ion complexation equilibrium problems.