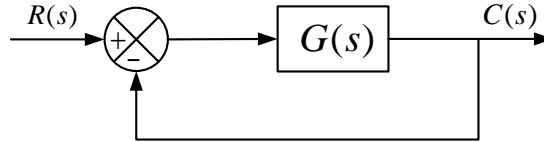


1. Lead Compensator Design / Simulation



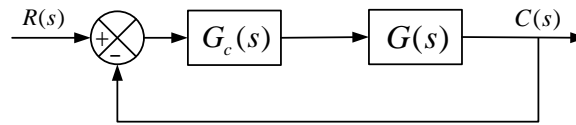
- Open-loop Transfer function : $G(s) = \frac{4}{s(s+2)}$

- Closed-loop Transfer function : $\frac{C(s)}{R(s)} = \frac{4}{s^2 + 2s + 4} = \frac{4}{(s+1+j\sqrt{3})(s+1-j\sqrt{3})}$

- Closed-loop Poles : $s = -1 \pm j\sqrt{3}$

- Closed-loop Properties : $\zeta = 0.5, \quad \omega_n = 2 \text{ rad/s}, \quad K_v = 2 \text{ sec}^{-1}$

▪Compensated System



- $G_c(s) = K_c \frac{s + \frac{1}{T}}{s + \frac{1}{\alpha T}}$: lead compensator

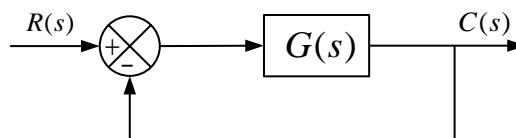
- Desired Properties : $\zeta = 0.5, \quad \omega_n = 4 \text{ rad/s}, \quad K_v : \text{not given}$

1) Find α, T, K_c .

2) Compare step input responses of the compensated system with uncompensated system using MATLAB.

2. The transfer function of the closed-loop control system shown in the figure below is

$$G(s) = \frac{4}{s(s+0.5)}$$



Desired specifications of the compensated system are as follows:

$\zeta = 0.5, \quad \omega_n = 5 \text{ rad/s}, \quad K_v = 80 \text{ sec}^{-1}$.

(1) Design a lead-lag compensator

(2) Plot root locus of the compensated and uncompensated systems.

(3) Compare step and ramp responses of the compensated and uncompensated systems.