1. When calculating the population density of electrons for a metal by using (7.26), a value much larger than immediately expected results. Why does the result, after all, make sense? (Take σ =5×10⁵ 1/ Ω cm; v_F =10⁸ cm/s and τ =3.1×10⁻¹⁴ s).

$$\begin{split} \sigma &= \frac{1}{3} e^2 v_f^2 \tau N(E_F) \\ N(E_F) &= \frac{3\sigma}{e^2 v_f^2 \tau} = \frac{3 \times 5 \times 10^5}{(4.803 \times 10^{-10})^2 (10^8)^2 (3 \times 10^{-14})} = 2.167 \times 10^{22} \\ unit : \frac{1/\Omega cm}{(cm^{1.5} g^{0.5}/s)^2 (cm/s)^2 s} = \frac{9 \times 10^{11}/s}{cm^3 (g/s^2) (cm^2/s)} = \frac{9 \times 10^{11} \times 1.602 \times 10^{-12}}{1e \, V \cdot cm^3} \\ \therefore 2.167 \times 10^{22} \times \frac{(9 \times 10^{11}) (1.602 \times 10^{-12})}{e \, V \cdot cm^3} = 3.125 \times 10^{22}/e \, V \cdot cm^3 = 1.95 \times 10^{47}/J \cdot m^3 \end{split}$$

2. Consider the conductivity equation obtained from the classical electron theory. According to this equation, a bivalent metal, such as zinc, should have a larger conductivity than a monovalent metal, such as copper, because zinc has about twice as many free electrons as copper. Resolve this discrepancy by considering the quantum mechanical equation for conductivity.

- 주교재 P88-89 참고