

1. 입방정 결정(cubic crystal)의 자기 이방성 에너지 (magnetic anisotropy energy) E_a 는 아래와 같이 나타낼 수 있다.

$$E_a = K_0 + K_1(a_1^2 a_2^2 + a_2^2 a_3^2 + a_3^2 a_1^2) + K_2 (a_1^2 a_2^2 a_3^2) + \dots$$

여기서 a_1, a_2, a_3 는 각각 direction cosine들로 각 결정 축(crystal axis)과 M_s 방향 사이에 이루는 각도의 cosine값들이다.

(a) Fe결정(BCC 구조)의 $\langle 100 \rangle, \langle 110 \rangle, \langle 111 \rangle$ 결정 축 방향들에 대해 E_a 를 계산하라. Fe결정의 자기이방성계수는 $K_1 = 0.48 \times 10^5 \text{ joule/m}^3, K_2 = 0.05 \times 10^5 \text{ joule/m}^3$ 이다.

(b) 위의 계산 결과를 토대로 볼 때 Fe결정의 easy axis와 hard axis는 각각 어느 방향인가?

2. A magnetic field is applied in the base plane of cobalt. The easy axis direction is the unique axis. Using $K_u = 4.1 \times 10^5 \text{ J/m}^3$ and $M_s = 1.42 \times 10^6 \text{ A/m}$, calculate the field needed to rotate the magnetic moments (a) into the base plane (*i.e.*, perpendicular to the unique axis) and (b) 45° from the hexagonal axis.

3. (a) Find the saturation magnetostriction λ_s of Ni single crystal in the direction $\langle 110 \rangle$, where $\lambda_{100} = -46 \times 10^{-6}$ and $\lambda_{111} = -24 \times 10^{-6}$ for the Ni crystal. In cubic crystals, the saturation magnetostriction is given by $\lambda_s = \frac{3}{2} \lambda_{100}(a_1^2 \beta_1^2 + a_2^2 \beta_2^2 + a_3^2 \beta_3^2 - \frac{1}{3}) + 3\lambda_{111}(a_1 a_2 \beta_1 \beta_2 + a_2 a_3 \beta_2 \beta_3 + a_3 a_1 \beta_3 \beta_1)$. Where, a_1, a_2, a_3 are direction cosines between crystal axes and the magnetization direction (*i.e.*, M_s), $\beta_1, \beta_2, \beta_3$ are direction cosines between measuring direction of λ_s and the crystal axes.

(b) Show the saturation magnetostriction λ_s for a cubic polycrystal is given by $\lambda_s = (2\lambda_{100} + 3\lambda_{111})/5$, assuming completely random domains, and calculate λ_s for Ni polycrystals.