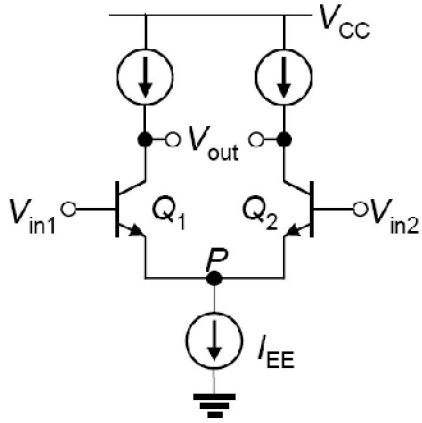


Quiz 1	Subject	Professor	Student ID#	Student Name	Score
Date: 2009.09.09	Microelectronics 2	Jong-Ho Lee			

1. Assume that bipolar transistors Q_1 and Q_2 are symmetric in the circuit shown below. The transistors have an output resistance r_o due to a finite Early voltage V_A . Answer for the following questions.



$$\begin{aligned} \Delta V_{BE1} &= \Delta V - \Delta V_P \\ \Delta V_{BE2} &= -\Delta V - \Delta V_P \\ g_{m1} &= g_{m2} = g_m \\ \Delta I_{c1} &= g_m(\Delta V - \Delta V_P) \\ \Delta I_{c2} &= -g_m(\Delta V + \Delta V_P) \\ \Delta I_{c1} + \Delta I_{c2} &= 0 \\ g_m(\Delta V - \Delta V_P) &= g_m(\Delta V + \Delta V_P) \\ \text{Therefore, } \Delta V_P &= 0 \end{aligned}$$

For small changes at inputs, the g_m 's are the same, and the respective increase and decrease of IC1 and IC2 are the same, node P must stay constant to accommodate these changes. **Therefore, node P can be viewed as AC ground.**

Method2.

(a) Compute the differential gain of the circuit, where ideal current sources are used as loads to maximize the gain.

Answer)

The output impedance of the ideal current source is infinite. So $R_{out} = r_o (= r_{o1} = r_{o2})$, using half-circuit analysis.

$$A_v = -g_m r_o$$

(b) Repeat (a), but assume the output impedance of the ideal current sources for loads has a finite impedance r_o (not ideal).

Answer)

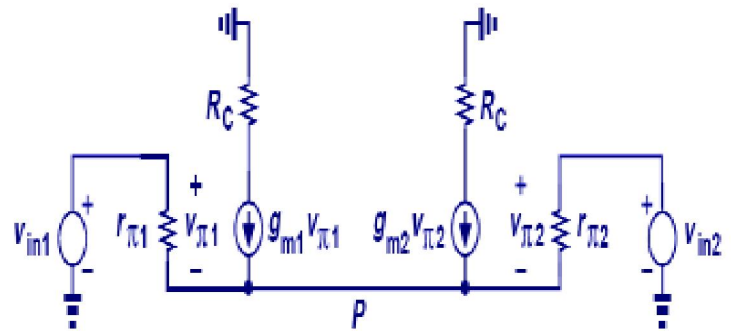
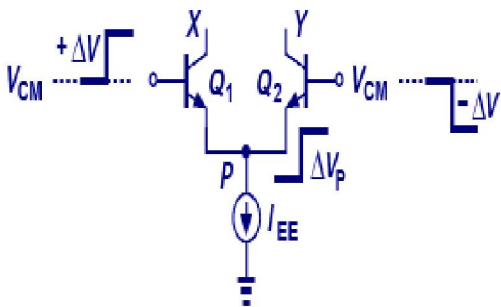
$$R_{out} = r_o // r_o = \frac{r_o}{2}$$

$$A_v = -g_m \frac{r_o}{2}$$

(c) Show that the node P is virtual ground.

Answer)

Method1.



$$\begin{aligned} v_{in1} - v_{\pi 1} &= v_p = v_{in2} - v_{\pi 2} \\ \frac{v_{\pi 1}}{r_{\pi 1}} + g_{m1} v_{\pi 1} + \frac{v_{\pi 2}}{r_{\pi 2}} + g_{m2} v_{\pi 2} &= 0 \\ \text{With } r_{\pi 1} &= r_{\pi 2}, \text{ and } g_{m1} = g_{m2}, v_{\pi 1} = -v_{\pi 2} \\ \text{Since } v_{in1} &= -v_{in2}, 2v_{in1} = 2v_{\pi 1} \\ \mathbf{V_p} &= v_{in1} - v_{\pi 1} = 0 \end{aligned}$$

There can be many other solutions for this problem.