## Homework #1

## Due: Oct 05, 23:59

1. Derive an equation that describes the rate of an enzyme reaction (v)under uncompetitive inhibition as a function of  $v_m$ ,  $K_M$ , [S], [I], and  $K_I'$ where

 $v_M$  = maximum enzyme reaction rate under no inhibition

- $K_M$  = half-velocity constant under no inhibition
- [S] = substrate concentration
- [*I*] = uncompetitive inhibitor concentration
- $K'_{I} = k_{-4}/k_{4}$ , where  $k_{4}$  and  $k_{-4}$  are forward and backward reaction rate constants for the formation of the enzyme-substrate-inhibitor complex (ESI) from the enzyme-substrate complex (ES) and uncompetitive inhibitor (I), as illustrated in the following.

$$ES \! + \! I \xrightarrow[]{k_4}{\underset{k_{-4}}{\longleftrightarrow}} ESI$$

Use the equation you derived to explain how the maximum enzyme reaction rate and half-velocity constant changes due to the presence of an uncompetitive inhibitor.

(50 points)

2. You want to develop an eco-friendly and cost-effective process for removal of nitrate  $(NO_3)$  from groundwater. Your plan is to supply molasses, a byproduct of sugar manufacturing, as an e<sup>-</sup> donor to enhance denitrification in groundwater. Assuming that the molecular formular of molasses can be represented by  $C_{12}H_{22}O_{11}$  (same as that for sugar), answer the following.

- 1) Write the electron donor half reaction,  $R_d$ , in an electron-equivalent form. Use  $HCO_3^-$  as an only form of an oxidized carbon species. (15 points)
- 2) Write the energy reaction,  $R_e$ , in an electron-equivalent form. How much grams of molasses are needed per g of NO<sub>3</sub>-N consumed for the energy reaction? (15 points)
- 3) Write the cell formation half reaction,  $R_c$ , in an electron-equivalent form. Use the cell formula of  $C_5H_7O_2N$  and  $NO_3^-$  as a source of nitrogen (not  $NH_4^+$ ). Also use  $HCO_3^-$  as an only form of oxidized carbon species. (15 points)
- 4) Write the overall cell synthesis reaction,  $R_s$ , in an electron-equivalent form. Use the  $R_d$  derived from 1) and the  $R_c$  derived from 3). How much grams of molasses are needed per g of NO<sub>3</sub>-N consumed for the cell synthesis reaction? (15 points)
- 5) From the calculations you did for 2) and 4), which growth state do you think is more favorable for efficient use of molasses? (A) a rapidly growing state or (B) a slowly growing state? Briefly describe the reason for your selection. (10 points)
- 6) You are planning to control the molasses supply rate and other environmental conditions relevant to the bacterial growth such that a  $f_s$ value of 0.05 is achieved. Write the stoichiometry of the overall reaction occurring at this condition. For 1 g of NO<sub>3</sub>-N consumption, i) how much molasses will be consumed (in g molasses), ii) how much alkalinity will be produced (in g as CaCO<sub>3</sub>), and iii) how much biomass will be produced (in g biomass)? (30 points)