Homework #4 - Solutions

Due: May 21, 2018 (Mon), in class

1. Determine the removal efficiency for a sedimentation basin with an overflow rate of 2 m/h in treating a wastewater containing particles whose settling velocities are distributed as given in the table below. Plot the particle histogram for the influent and effluent wastewater. (10점)

settling velocity, m/h	No. of particles
0.0-0.5	10
0.5-1.0	29
1.0-1.5	47
1.5-2.0	65
2.0-2.5	74
2.5-3.0	60
3.0-3.5	28
3.5-4.0	13
4.0-4.5	5

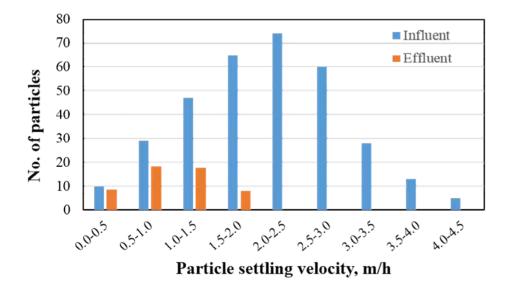
Answer)

Construct a table using the data above:

Avg. settling	No. of particles	Fraction	No. of particles	No. of particles
vel., m/h		removed	removed	in effluent
0.25	10	0.125	1.25	8.75
0.75	29	0.375	10.875	18.125
1.25	47	0.625	29.375	17.625
1.75	65	0.875	56.875	8.125
2.25	74	1.000	74	0
2.75	60	1.000	60	0
3.25	28	1.000	28	0
3.75	13	1.000	13	0
4.25	5	1.000	5	0
Total	331		278.4	52.6

removal efficiency = $278.4/331 \times 100(\%) = 84.1\%$

Particle histogram:



2. The following data were obtained from a test program in a batch reactor designed to evaluate a new aeration system. Using these data, determine the K_La and the equilibrium dissolved oxygen concentration in the test tank. (10^A)

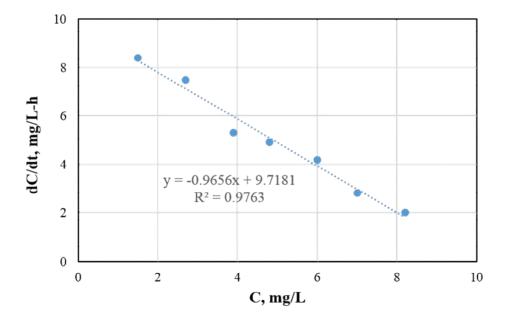
DO concentration, C, mg/L	dC/dt, mg/L-h
1.5	8.4
2.7	7.5
3.9	5.3
4.8	4.9
6.0	4.2
7.0	2.8
8.2	2.0

Answer)

Absorption of gas in a batch reactor:

$$\frac{dC}{dt} = K_L a (C_s - C_t) = K_L a C_s - K_L a C_t$$

Plotting C vs. dC/dt, we get the following regression:





 $K_L a = 0.966 \ h^{-1}$

$$C_s = \frac{9.718 \ mg/L - h}{0.966 \ hr^{-1}} = 10.1 \ mg/L$$

- 3. 우리나라에서는 2013년 수질 및 수생태계 보호에 관한 법률 개정에 따라 공공하수처 리시설의 총 인(total phosphorus; T-P) 배출허용기준이 2014년부터 2016년까지 단계적 으로 대폭 강화되었다. 이에 따라 국내에 하수처리시설에 인 제거를 위한 고도처리가 본격적으로 도입되고 있다. 현재 화학적 총인처리시설을 가동 중이거나 설치 또는 기 획 중인 하수처리장 사례 하나를 조사하여 적용된 처리공정의 원리를 간략하게 설명 하시오. (15점)
- 4. Briefly (in one or two paragraphs for each) describe the following two biological treatment processes for wastewater treatment: i) rotating biological contactor (RBC) and ii) upflow anaerobic sludge blanket (UASB). (10점)
- 5. A CSTR without solids recycle is used to treat a wastewater containing 100 mg/L phenol at 20°C. Using the following kinetic coefficients at 20°C, determine i) the minimal hydraulic retention time (HRT) in days at which the biomass can be washed out faster than they can grow, ii) the minimum HRT at 10°C, assuming the temperature coefficient θ is 1.07 for k and 1.04 for b, iii) the effluent phenol and biomass concentration at an HRT of 7.0 d at 20°C.

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k = 0.80 g phenol/g VSS/d
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 $K_s = 0.15 \ mg \ phenol/L$

Y = 0.45 g VSS/g phenol

 $b = 0.08 \ / d$

Hint 1: When there's no solids recycle, SRT should be the same as HRT.

Hint 2: The modified van't Hoff-Arrhenius relationship, $k_2/k_1 = \theta^{(T_2 - T_1)}$, applies to both k and b. Assume Y and K_s are not functions of temperature.

(25점)

Answer)

Since $K_s \ll S^0$,

$$SRT_{\min} = \frac{1}{Yk - b} = \frac{1}{0.45 \ g \ VSS/g \ phenol \cdot \ 0.80 \ g \ phenol/g \ VSS/d - 0.08/d}$$

 $= 3.57 \ d$

ii)

 $k_{10} = k_{20} \, \cdot \, \theta^{(10 - 20)} = 0.8 \, \cdot \, 1.07^{-10} = 0.41 \; g \; phenol/g \; V\!S\!S\!/d$

 $b_{10} = b_{20} \, \cdot \, \theta^{(10\,-\,20)} = 0.08 \, \cdot \, 1.04^{-\,10} = 0.054/d$

$$SRT_{\min} = \frac{1}{Yk - b} = \frac{1}{0.45 \ g \ VSS/g \ phenol \cdot \ 0.41 \ g \ phenol/g \ VSS/d - 0.054/d}$$

 $= 7.66 \ d$

iii)

$$S = \frac{K_s(1+b \cdot SRT)}{SRT(Yk-b)-1}$$

 $= \frac{0.15 \ mg \ phenol/L \cdot (1 + 0.08/d \cdot 7.0 \ d)}{7.0 \ d \cdot (0.45 \ g \ VSS/g \ phenol \cdot 0.80 \ g \ phenol/g \ VSS/d - 0.08/d) - 1}$

 $= 0.24 \ mg \ phenol/L$

$$X_a = \left(\frac{SRT}{\tau}\right) \left[\frac{Y(S^0 - S)}{1 + b \cdot SRT}\right] = \frac{Y(S^0 - S)}{1 + b \cdot SRT}$$

 $=\frac{0.45 \ g \ VSS/g \ phenol \cdot (100-0.24) \ mg \ phenol/L}{1+0.08/d \cdot 7.0 \ d} \times 10^{-3} \ g \ phenol/mg \ phenol \times 10^{3} \ mg \ VSS/g \ VSS$

= 28.8 mg VSS/L

6. A complete-mix activated sludge process with secondary clarification and sludge recycle is used to treat a wastewater at a flowrate of 1,000 m³/d with a bsCOD of 2,000 mg/L. The MLSS concentration is 3,300 mg/L, MLVSS/MLSS ratio is 0.80, effluent TSS concentration is 20 mg/L, HRT is 24 h, recycle MLSS concentration is 10,000 mg/L, and waste sludge flowrate is $85.5 \text{ m}^3/\text{d}$. Using the given information, determine i) the system SRT, ii) the F/M ratio in g bsCOD/g VSS/d, iii) the observed yield in g TSS/g bsCOD, and iv) the true yield in g VSS/g bsCOD. Assume that the effluent bsCOD concentration is negligible compared to the influent concentration, and influent nbVSS is negligible. Use the following parameters.

 $b = 0.10 \ g \ VSS/g \ VSS/d$

 $f_d = 0.15 \ g \ VSS/g \ VSS$

(30점)

Answer)

i)

Applying the same logic as we used in class to get SRT of active biomass for TSS:

$$SRT = \frac{VX_{TSS}}{(Q - Q^w)X_{TSS}^e + Q^w X_{TSS}^r}$$
$$V = Q\tau = 1000 \ m^3/d \cdot 1 \ d = 1000 \ m^3$$
$$= \frac{1000 \ m^3 \cdot 3300 \ mg/L}{(1000 - 85.5) \ m^3/d \cdot 20 \ mg/L + 85.5 \ m^3/d \cdot 10000 \ mg/L} = 3.8 \ d$$

ii)

$$F/M = \frac{QS^0}{VX_{VSS}} = \frac{1000 \ m^3/d \cdot 2000 \ g \ bs \ COD/m^3}{1000 \ m^3 \cdot 3300 \ g \ TSS/m^3 \cdot 0.80 \ g \ VSS/g \ TSS} = 0.76 \ g \ bs \ COD/g \ VSS/d \ MSS/d \ MSS/g \ TSS = 0.76 \ g \ bs \ COD/g \ VSS/d \ MSS/d \ MSS/d \ MSS/g \ TSS = 0.76 \ g \ MSS/d \ \ MSS/d \ MSS/d \ MSS/d \ \ MSS/d \ MSS/d \ M$$

iii)

$$Y_{obs} = \frac{P_{X,TSS}}{Q(S^0 - S)} = \frac{X_{TSS} \cdot V}{Q(S^0 - S) \cdot SRT} = \left(\frac{\tau}{SRT}\right) \frac{X_{TSS}}{S^0}$$
$$= \frac{1}{3.8} \frac{d}{d} \cdot \frac{3300 \text{ mg } TSS/L}{2000 \text{ mg } bs COD/L} = 0.43 \text{ g } TSS/g \text{ } bs COD$$

iv)

$$Y_{obs} = 0.80 \ g \ VSS/g \ TSS \cdot 0.43 \ g \ TSS/g \ bs \ COD = 0.35 \ g \ VSS/g \ bs \ COD$$

$$Y_{obs} = \frac{Y}{1+b \cdot SRT} + \frac{f_d \cdot b \cdot Y \cdot SRT}{1+b \cdot SRT} = Y \cdot \frac{1+f_d \cdot b \cdot SRT}{1+b \cdot SRT}$$
$$Y = Y_{obs} \cdot \frac{1+b \cdot SRT}{1+f_d \cdot b \cdot SRT} = 0.35 \ g \ VSS/g \ bs \ COD \cdot \frac{1+0.10/d \cdot 3.8 \ d}{1+0.15 \cdot 0.10/d \cdot 3.8 \ d}$$

 $= 0.46 \ g \ VSS/g \ bs \ COD$