

Homework #2  
 Due: November 2 (Tuesday), 2021

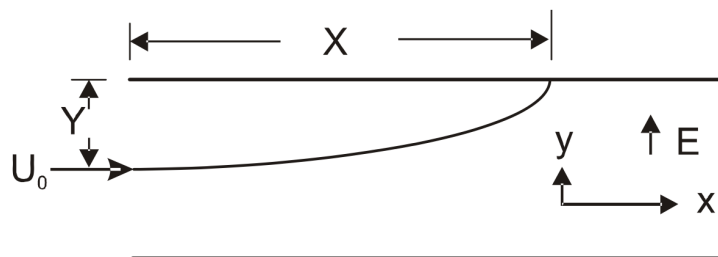
\*You may submit your homework to TA (chl\_ghdtjr@naver.com) by email or submit to 313-222.

1. A spherical droplet is rotating with an angular velocity  $\omega_i$  as it moves with a translational velocity of  $U_i$  at its center of mass. Assume that the droplet is evaporating uniformly. Is the expression of  $mdU_i/dt = F_i$ , where  $F_i$  is the force acting on the particle, still applicable? Determine by applying the Reynolds transport theorem to the rotating, evaporating droplet.

2. A droplet is injected with a velocity  $v_o$  into a quiescent medium (no motion). The droplet evaporates according to the  $D^2$ -law and Stokes drag is applicable. The drag force is the only force acting on the droplet (no gravity) and the mass flux is uniform over the surface.

- Derive an equation for the droplet velocity and distance as a function of  $v_o$ ,  $t$  and  $\tau_V/\tau_m$ . The definitions of the time constant is the same as we dealt in the class.
- Setting  $t = \tau_m$ , evaluate the distance traveled for  $\tau_V/\tau_m \ll 1.0$  and  $\tau_V/\tau_m \gg 1.0$ .

3. A charged particle is injected into a channel with quiescent fluid and a uniform electric field strength. The initial velocity of the particle is  $U_o$  and the distance from the injection point to the wall (collecting surface) is  $L$ . Find the axial distance the particle will travel before it impacts the wall in terms of electric field strength,  $E$ , the aerodynamic response time of the particle, the charge to mass ratio on the particle ( $q/m$ ), the initial velocity and the distance to the wall. Neglect gravitational effects.



4. Consider a flow of evaporating particles in a one-dimensional ( $x$ -direction) duct. The particles evaporate according to the  $D^2$ -law and are always in kinetic equilibrium with the gas. The number flow rate  $\dot{n}$  of the particles is constant so  $\dot{n} = n\tilde{v}A = n\langle u \rangle A = const$ , where  $n$  is the particle number density. The particle volume fraction is sufficiently small that the continuous phase volume fraction can be taken as unity,  $\alpha_c \approx 1.0$ .

- Find an expression for the mass source term in the form of  $S_m = -n\dot{m} = f(Z_o, \frac{\langle u \rangle_o}{\langle u \rangle}, \rho_c, \tau_m, \frac{D}{D_o})$ , where  $Z_o$ ,  $\langle u \rangle_o$ , and  $D_o$  are the loading, velocity and particle

diameter at the beginning station in the tube. The evaporation time constant is  $\tau_m$  and  $\rho_c$  is the gas density.

- Using the continuous phase continuity equation,  $\frac{\Delta}{\Delta x}(\rho_c \langle u \rangle) = S_m$ , find how the velocity varies with time in the form of  $\frac{\langle u \rangle}{\langle u \rangle_0} = f(Z_0, \frac{t}{\tau_m})$  and find the velocity ratio when evaporation is complete. When you complete the expression for  $S_m$  you will find a velocity  $\langle u \rangle$  in the denominator which when combined with the continuity equation allows you to express  $\langle u \rangle \frac{\Delta}{\Delta x}(\rho_c \langle u \rangle) = \rho_c \frac{\Delta \langle u \rangle}{\Delta t}$ .

