

Problem Statement

- A tank having a volume of **0.85 cubic meter** initially contains water as a two phase liquid vapor mixture at **260 degree celsius** and a quality of **0.7**. Saturated water vapor at **260 degree celsius** is **slowly withdrawn** through a **pressure regulating valve at the top of the tank** as **energy is transferred by heat to maintain the pressure constant in the tank**. This continues until the tank is filled with saturated vapor at **260 degree celsius**. Determine the **amount of heat transfer in kJ**.
Neglect all kinetic and potential energy

Solution

$$\bullet \frac{dE}{dt} = \dot{Q} - \cancel{\dot{m}_1 h_1} + \dot{m}_1 \left(h_1 + \cancel{\frac{V_1^2}{2}} + \cancel{\frac{gZ_1}{2}} \right) - \dot{m}_2 \left(h_2 + \cancel{\frac{V_2^2}{2}} + \cancel{\frac{gZ_2}{2}} \right)$$

$$\bullet \frac{dE}{dt} = \dot{Q} + \dot{m}_1 h_1 - \dot{m}_2 h_2$$

• Since nothing is coming inside the tank
thus $\dot{m}_1 h_1 = 0$

$$\bullet \text{Therefore } \frac{dE}{dt} = \dot{Q} - \dot{m}_2 h_2$$

Solution

- $\frac{dE}{dt} = \dot{Q} - \dot{m}_2 h_2$
- $\frac{dm_{cv}}{dt} = -\dot{m}_2$
- $\frac{dE}{dt} = \dot{Q} + \frac{dm_{cv}}{dt} h_2$
- $\Delta E = \Delta Q + h_2 \Delta m_{cv} \dots 1$
- Initial mass inside the tank is calculated as
since the vapor and water are in saturated
state so from the steam table at 260 degree
celsius.

Solution

- $v_m = v_l * 0.3 + (v_g * 0.7)$
- $= (0.001276 * 0.3) + (0.7 * 0.04276) = 0.029906$
 m^3/kg
- Thus $0.85 / 0.029906$ gives 28.422 kg
- Similarly mass when it is pure steam inside is $0.85 / 0.04276 = 20.14$ kg
- h_2 is saturated steam enthalpy at 260 degree celsius , 2796.6 kJ/kg

Solution

- ΔE is calculated from specific internal energy and the initial and final mass of the system
- Specific internal energy (initially):
 $(0.3 \times 1128.4) + (0.7 \times 2599) = 2157.8 \text{ kJ/kg}$
- Specific internal energy (after) = 2599 kJ/kg
- Thus plugging everything in 1
- We get **$Q = 14.16 \text{ kJ}$**