

Student ID# _____ Name: _____

[1] A Nyquist plot of a unity-feedback system with the feedforward transfer function $G(s)$ is shown in Figure 7-159.

If $G(s)$ has one pole in the right-half s plane, is the system stable?

If $G(s)$ has no pole in the right-half s plane, but has one zero in the right-half s plane, is the system stable?

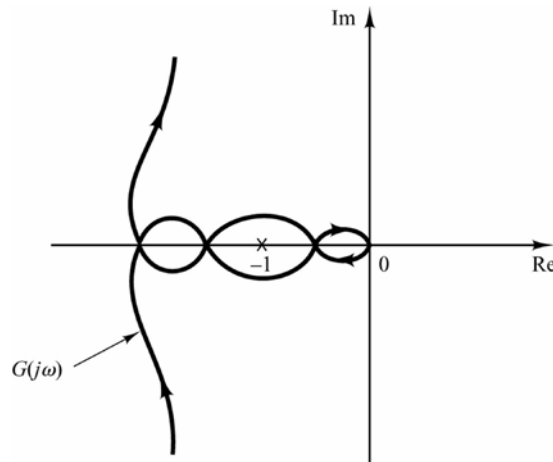


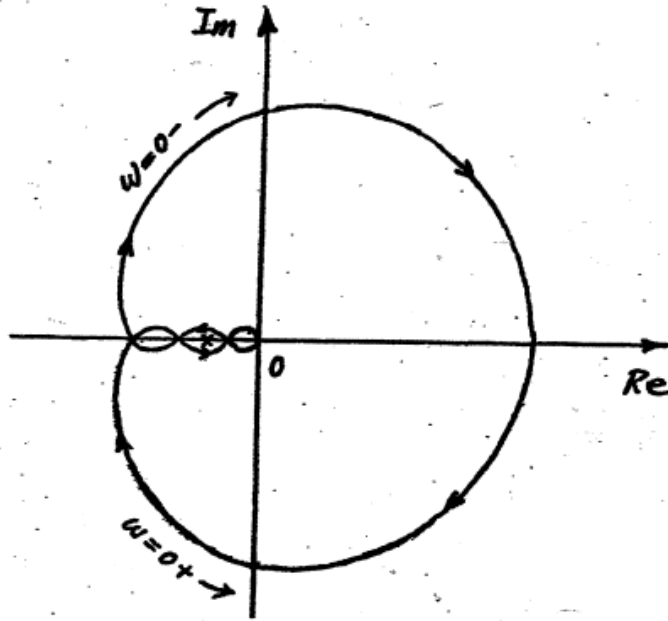
Figure 7-159 Nyquist Plot

solution

Consider the case where $G(s)$ has one pole in the right-half s plane. From the Nyquist plot of $G(j\omega)$ shown below, the $-1+j0$ point is encircled by the $G(j\omega)$ locus once clockwise and once counterclockwise. Hence, $N=0$. Since $G(s)$ has one pole in the right-half s plane, we have $P=1$. Since

$$Z = N + P = 0 + 1 = 1$$

The system is unstable.



Next, consider the case where $G(s)$ has no pole in the right-half s plane, but has one zero in the right-half s plane. The $-1+j0$ point is encircled by the $G(j\omega)$ locus once clockwise and once counterclockwise. Hence, $N = 0$. Since $G(s)$ has no poles in the right-half s plane, we have $P=0$. Therefore,

$$Z = N + P = 0 + 0 = 0$$

The system is stable. (Note that the presence of a zero of $G(s)$ in the right-half s plane does not affect the stability of the system.)