Engineering Math 2 Quiz 2

1. Is the following function analytic?

$$f(z) = \ln|z| + iArgz$$

2. Evaluate (showing the details and using partial fractions if necessary).

$$\oint_C \frac{dz}{z^2 + 1},$$

C: (a)
$$|z+i|=1$$
, (b) $|z-i|=1$

3. Integrate around C.

$$\frac{e^{z/2}}{(z-a)^4}$$
, C the circle $|z-2-i|=3$, counterclockwise

4. Find the center and the radius of convergence of the following power series.

$$\sum_{n=0}^{\infty} \frac{n^4}{2^n} z^{2n}$$