

Analog Electronic Circuits
Department of Electrical and Computer Engineering
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Final exam

December 21, 2020

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A sheet of one-sided, A4-size note is allowed.

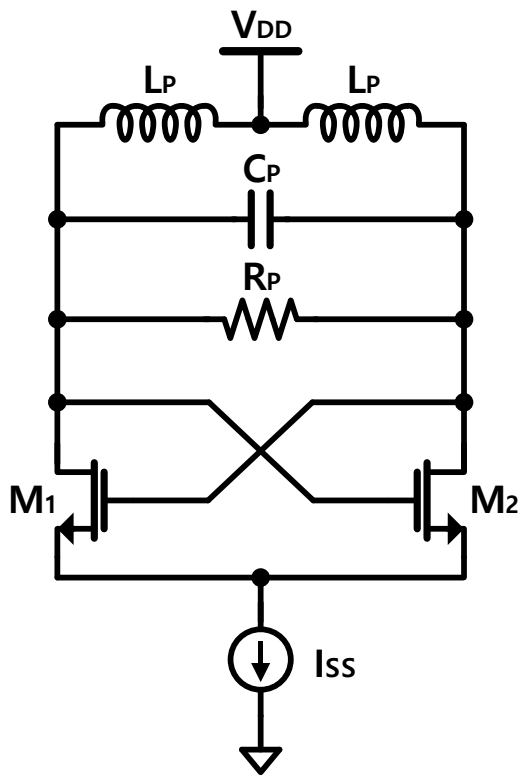
Roster Number (학번):

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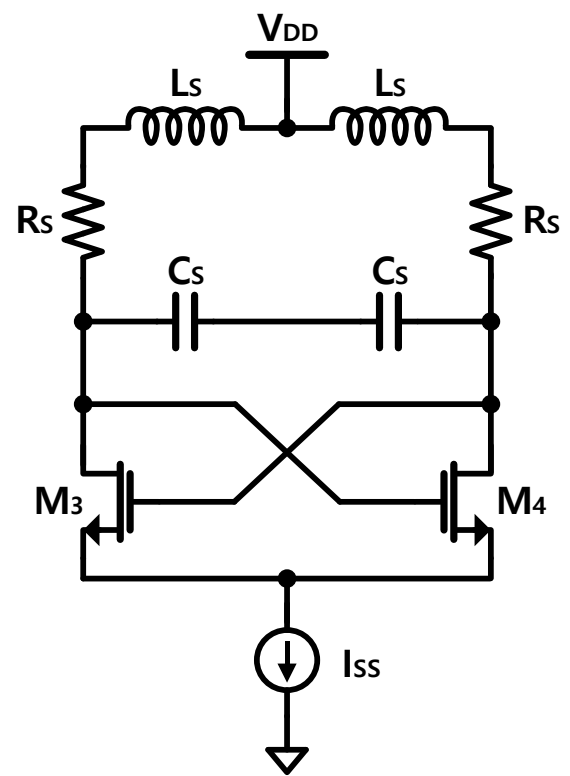
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Problem	Max Score	Score
1	18	
2	12	
3	10	
4	20	
5	15	
6	25	
Total	100	

[1] Answer the following questions. Assume all the transistors are identical and $r_o = \infty$.



Circuit A



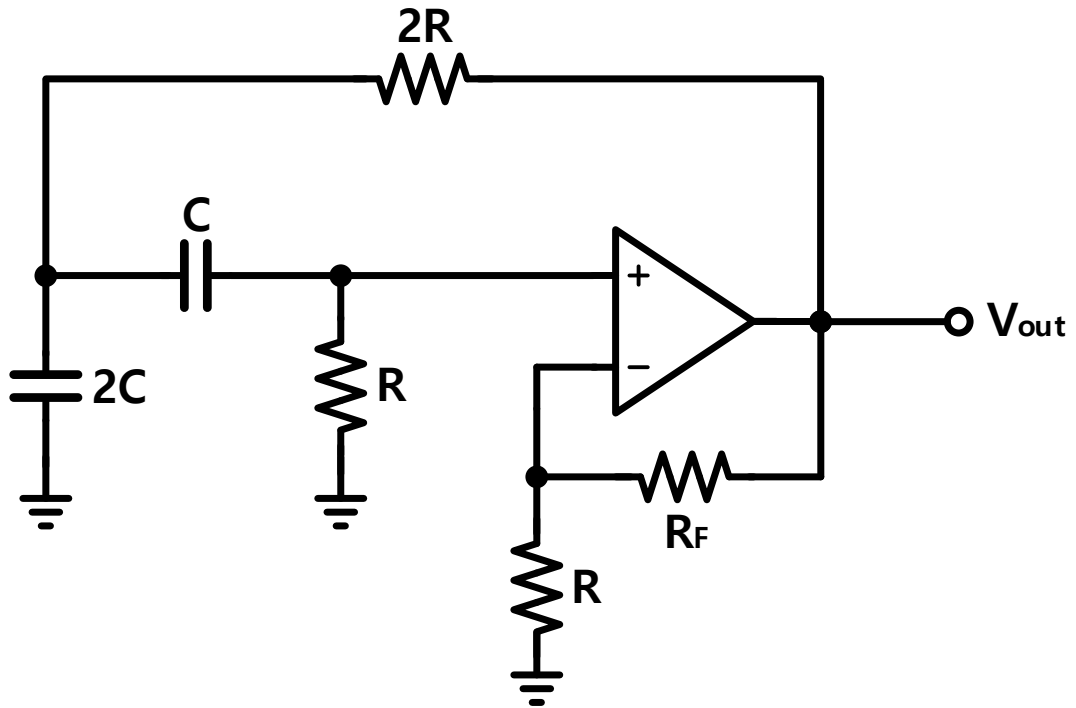
Circuit B

A. Find the oscillation frequency of the LC oscillator shown in Circuit A.

B. Determine the values of R_S , L_S , and C_S in terms of R_P , L_P , and C_P so that the impedance of Circuit B is the same as Circuit A. Use the oscillation frequency found from A. (Hint : Assume $R_P/2 \gg \omega L_P$)

C. Determine whether the LC oscillator oscillates when $g_m=1\text{mS}$, $R_S=1\Omega$, and $L_S=1\mu\text{H}$, and $C_S=1\text{nF}$.

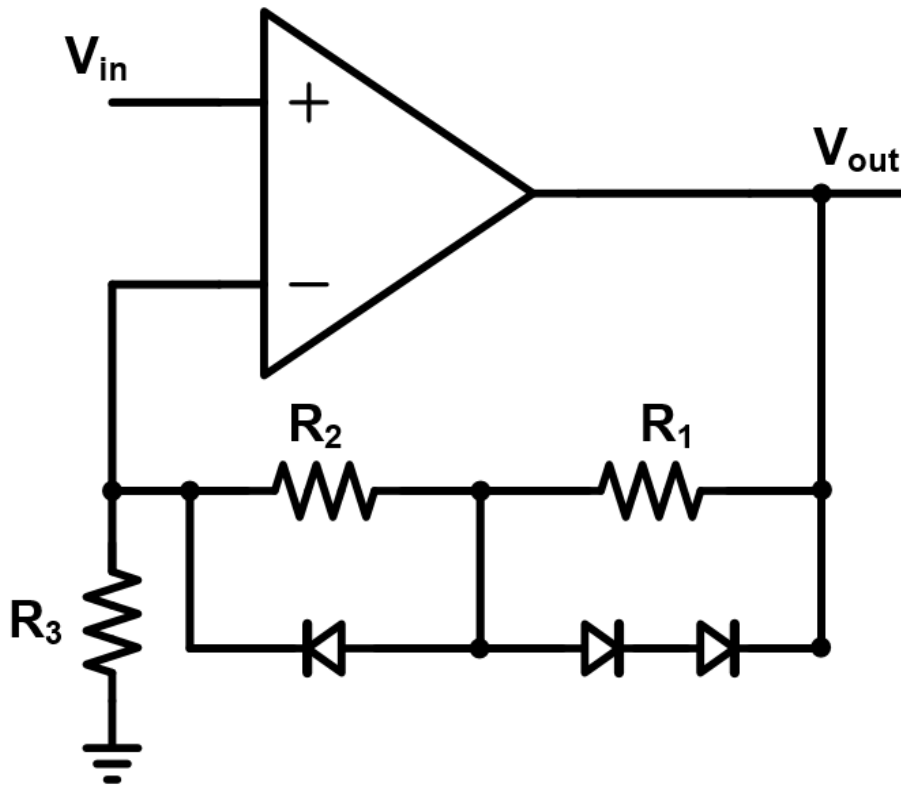
[2] Answer the following questions. Assume the amplifier is ideal.



A. Derive the transfer function of the loop gain.

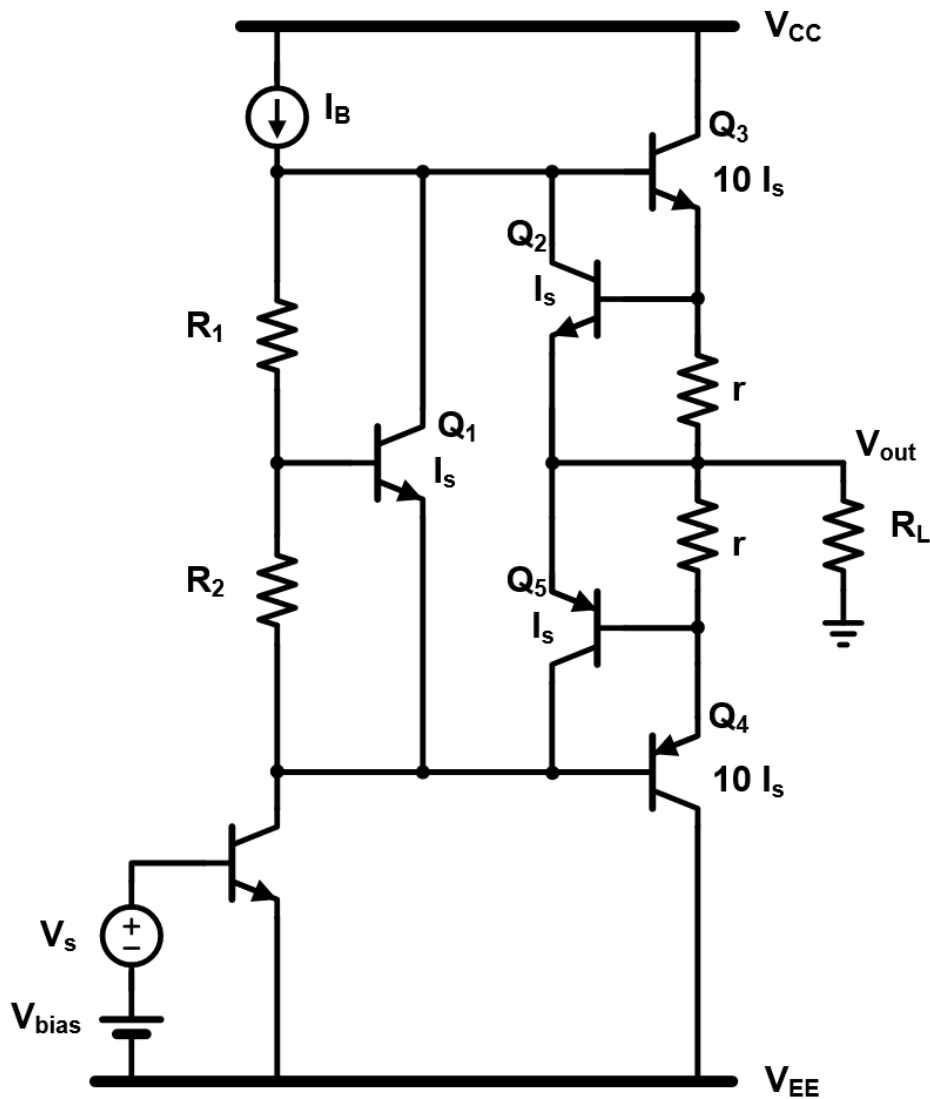
B. Find the minimum value of R_F for starting oscillation. Assume $R=1\text{k}\Omega$, $C=1\mu\text{F}$.

[3] Draw a $V_{in} - V_{out}$ curve of the circuit below. Specify the slope, condition of V_{in} or V_{out} when the diode turned on. (The voltage when the diode is turned on is $V_{D,ON}$)



[4] Consider the following output stage circuit. (Assume $V_A = \infty$)

$V_T = 26\text{mV}$, $I_s = 1 \times 10^{-13}\text{A}$, $R_L = 10\Omega$.



A. Find the resistor r , to limit the output current with 8 A. Assume Q2, Q5 is active when collector current is 1mA and $|V_{CC}|, |V_{EE}|$ are enough big.

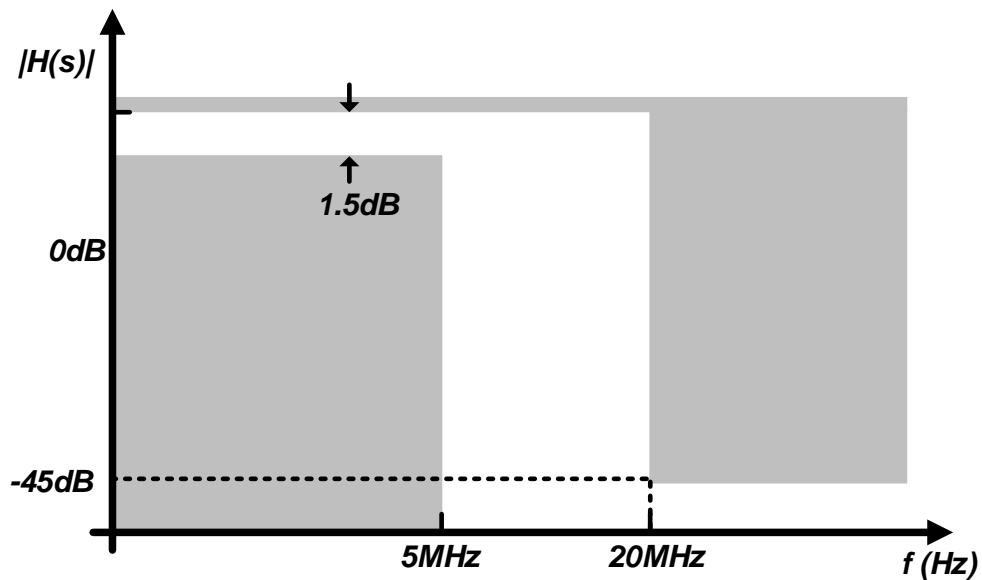
B. Find the minimum bias current I_B to deliver 80W power on 10Ω load with sinusoidal signal. Assume $\beta = 100$.

C. Find the R_1 using the bias current I_B of problem B, when the Quiescent current at the output is

100mA. (Quiescent current is the current when it is producing an output of zero, $V_{out} = 0$)
Assume $R_2 = 1k\Omega$, $r = 0\Omega$, and β of Q_1 is big enough, that is, $I_{C1} \approx I_{E1}$.)

- D. Find the power efficiency when $V_{out} = 10 \sin \omega t$ when $V_{CC} = -V_{EE} = 42V$?
Ignore the power dissipation at pre-driver and assume that each transistor carries a negligible current around $V_{out} = 0$ and turns off for half of the period.

[5] Answer the following questions.



Transfer function & Poles of the Butterworth Response

$$|H(j\omega)| = \frac{1}{\sqrt{1 + \left(\frac{\omega}{\omega_0}\right)^{2n}}}$$

$$p_k = \omega_0 \exp\left(\frac{j\pi}{2}\right) \exp\left(j\frac{(2k-1)\pi}{2n}\right), k = 1, 2, \dots, n$$

Transfer function & Poles of the Chebyshev Response

$$|H_{PB}(j\omega)| = \frac{1}{\sqrt{1 + \epsilon^2 \cos^2\left(ncos^{-1}\left(\frac{\omega}{\omega_0}\right)\right)}} \quad |H_{SB}(j\omega)| = \frac{1}{\sqrt{1 + \epsilon^2 \cosh^2\left(ncosh^{-1}\left(\frac{\omega}{\omega_0}\right)\right)}}$$

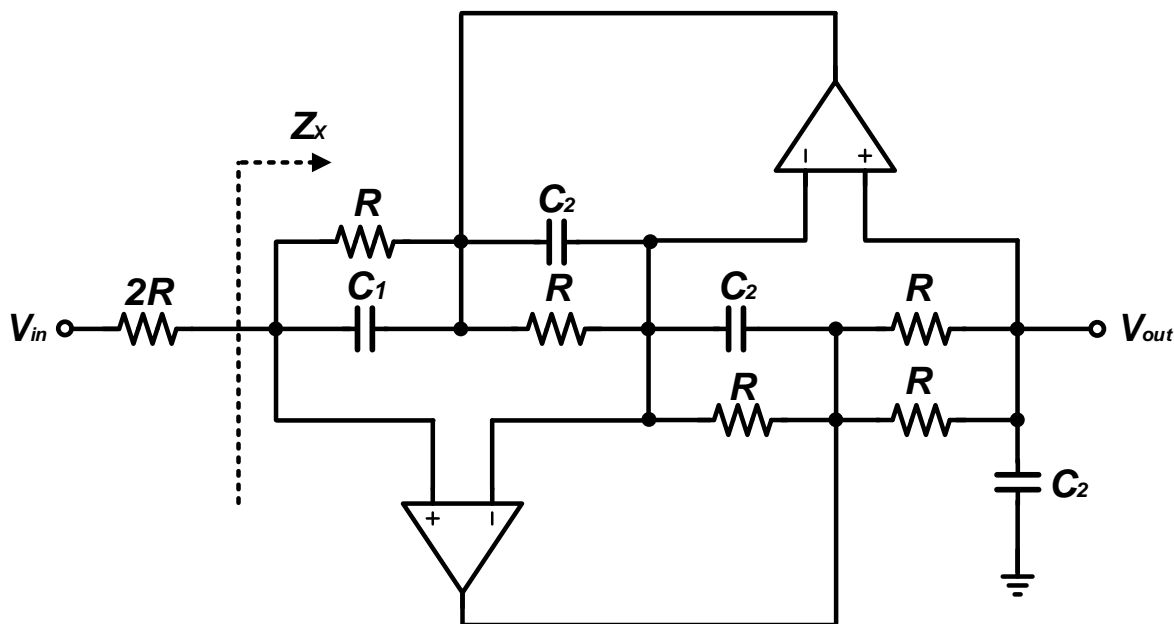
$$p_k = -\omega_0 \sin\frac{(2k-1)\pi}{2n} \sinh\left(\frac{1}{n} \sinh^{-1}\frac{1}{\epsilon}\right) + j\omega_0 \cos\frac{(2k-1)\pi}{2n} \cosh\left(\frac{1}{n} \sinh^{-1}\frac{1}{\epsilon}\right), k = 1, 2, \dots, n$$

Useful Equations

$$\sinh(x) = \frac{e^x - e^{-x}}{2}, \quad \cosh(x) = \frac{e^x + e^{-x}}{2}, \quad \sinh^{-1}(x) = \ln(x + \sqrt{x^2 + 1}), \quad \cosh^{-1}(x) = \ln(x + \sqrt{x^2 - 1})$$

- A. Determine the minimum order of each filter (Butterworth Response & Chebyshev Response). Assume the bandwidth of Chebyshev filter is 5MHz.
- B. Using determined value of n above, get the range of the optimal natural frequency (ω_o) of the Butterworth filter.

[6] Answer the following questions. Assume all op-amps are ideal.



A. Calculate $Z_X(s)$.

B. Derive the transfer function $H(s)$.

C. Determine the sensitivity of Q to a change in C_1 , $S_{C_1}^Q$, and the sensitivity of ω_n to a change in R , $S_R^{\omega_n}$.

D. Design a Chebyshev filter of the problem 4 having high Q factor based on this filter structure, 'General Impedance Converter'. Every R is 1k ohm and you need to get the value of C1, C2.