## Final Examination

## June 12th, 2008

1. The orientation and normal linear frequencies of 3 joint sets are as shown in the following table. Obtain the trend and plunge of a scanline showing the least total linear frequency of joints as well as the least total linear frequency. (20)

| Joint | Dip direction <br> $(\mathrm{a})$ | Dip $(\beta)$ | Normal linear <br> frequency $\left(\mathrm{m}^{-1}\right)$ |
| :---: | :---: | :---: | :---: |
| 1 | 230 | 86 | 2 |
| 2 | 247 | 78 | 3 |
| 3 | 65 | 80 | 1 |

2. The probability density function of the total spacing along a vertical scanline is a linearly decreasing function whose maximum total spacing is 6 m . Calculate the RQD from a rock core of 5 m length. (25)
3. Show that the mean trace length is proportional to the second moment of joint diameter and is inversely proportional to the mean diameter when the joints are modeled as Poisson discs. (25)
4. Show that the following estimator is still applicable to the case where the maximum joint trace length is greater than the maximum observable length of a rectangular window ( . (30)

1A. When a cartesian coordinate system is adopted so that $x, y$ and $z$ axes are parallel to east, north and upward, respectively,

| Joint | $X$ | $Y$ | $Z$ | Intersecti- <br> on | $X$ | $Y$ | $Z$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | -0.764 | -0.641 | 0.07 | S 12 | -0.335 | 0.301 | -0.893 |
| 2 | -0.9 | -0.382 | 0.208 | S 13 | 0.402 | -0.556 | -0.727 |
| 3 | -0.893 | -0.416 | -0.174 | S 23 | 0.407 | -0.909 | 0.088 |

- The least total linear frequency will be obtained by one of the three joint intersection vectors:
$\times, \times$ and $\times$
$-\cos \theta:$
J1- S12: 0.0, J2- S12: 0.0, J3- S12: $0.329->=1 \times 0.329=0.329 \mathrm{~m}^{-1}$
J2- S13: $0.301->\quad=3 \times 0.301=0.903 \mathrm{~m}^{-1}$
J1- S23: $0.244->=2 \times 0.244=0.488 \mathrm{~m}^{-1}$
- Trend/plunge of (- 0.335, 0.301, - 0.893):
$\sin P=-Z, P=A \sin (-Z), T=A \sin (X / \cos P)$
$\underline{\text { Plunge }}=63.25^{\circ}$, T rend $=-48.1^{\circ}=311.9^{\circ}$

2A.

- PDF of spacing $x$ :

Complete function: $y=(-x+6) / 18$ at $0 \sim 6 \mathrm{~m}$
Curtailed function: $y=(-x+6) / 17.5$ at $0 \sim 5 \mathrm{~m}$

- Mean spacing:
- Total frequency $=1 /=0.525 \mathrm{~m}^{-1}$
$3 A$.

Which makes

When - is combined with above relation we can get

4A.
$N_{i}=\lambda_{a} A_{l}^{c} f(l) d l$
therefore, $N_{a i l l}^{c}=\int_{0}^{t_{x}} N_{i}^{c}=\lambda_{a} \int_{0}^{t_{x}} A_{i}^{c} f(i) d l$.
Putting $A_{l}^{c}=\cos \theta \sin \theta l^{2}-(W \sin \theta+H \cos \theta) l+W H$ to above,

The same process is applied to transecting traces for as follows.

$$
N_{l}^{t}=\lambda_{a} A_{l}^{t} f(l) d l
$$

When $\geq$

$$
N_{l}^{t}=\lambda_{a} A_{t}^{t} f(l) d l
$$

For $\geq$

