

# Automata Theory

Midterm Exam : 23 October 2008

1. Find a DFA that is equivalent to the following NFA.
2. Find a regular grammar for  $\Sigma = \{0, 1\}$  that generates the set of all strings with at least one 1.
3. Prove or disprove that  $L = \{a^n : n = 3 + 4k, k = 0, 1, 2, \dots\}$  is regular.
4. Prove or disprove that  $L = \{w \in \{a, b\}^* : N_a(w) \neq N_b(w)\}$  is regular.
5. Let  $G$  be the following grammar.

$$S \rightarrow aSb \mid bSa \mid SS \mid \epsilon$$

Let  $L_{ab} = \{w \in \{a, b\}^* : N_a(w) = N_b(w)\}$ . Prove that  $L(G) = L_{ab}$ .

6. Let  $L = \{0^n 1^n : n \geq 0\}$ . Describe  $L^2$  by using the set notation. Find a context-free grammar for  $L^2$ .