

# Midterm Examination

Oct. 30th, 2008

1. Convert strike/dip to dip direction/dip. (10)

- 1) N40 E/36 SE      130/36
- 2) N52 W/45 SW      218/45
- 3) N60 E/50 NW      330/50
- 4) N66 W/27 NE      24/27

2. Explain the process of calculating the volume of a convex block. (10)

Selecting an apex      take faces not including the apex      divide each face into triangles      make tetrahedrons with the apex and each triangle

3. Dip direction and dip of joint A, B and C are 110/50, 230/70, and 304/60, respectively. There are two blocks on the joints: one is on joint A and the other is on joint B and C (wedge failure). 1) Show that the block on joint A slides down along the dip direction and dip of joint A, and 2) obtain the sliding direction (trend and plunge) of the block on joint A and B when the blocks slide down the joints by their own weight. (20)

1) Block on A:

$$\hat{s} // (\hat{n} \times \hat{R}) \times \hat{n}$$

$$\hat{n} = (\sin 50 \sin 110, \sin 50 \cos 110, \cos 50) = (0.7198, -0.2620, 0.642)$$

$$\hat{R} = (0, 0, -1)$$

$$(\hat{n} \times \hat{R}) = (0.262, 0.7198, 0)$$

$$(\hat{n} \times \hat{R}) \times \hat{n} = (0.4627, -0.1684, -0.5868) \rightarrow (0.604, -0.2198, -0.76)$$

$$\text{Plunge} = \sin^{-1}(0.766) = 50, \text{Trend} = \sin^{-1}(0.604/\cos 50) = 110$$

2)

$$\hat{n}_1 \times \hat{n}_2 = (\sin 70 \sin 230, \sin 70 \cos 230, \cos 70) \times (\sin 60 \sin 304, \sin 60 \cos 304, \cos 60)$$

$$= (-0.7198, -0.604, 0.342) \times (-0.718, 0.4843, 0.5) = (-0.4676, 0.1143, -0.7823)$$

$$\rightarrow (-0.5091, 0.1244, -0.8517)$$

$$\text{Plunge} = \sin^{-1}(0.8517) = 58.4, \text{Trend} = \sin^{-1}(-0.4676/\cos 58.4) = 296.8$$

4. Prove that a small circle on a projection sphere is projected to a circle on a projection plane by stereographic projection. (20)

• Sphere:  $\sin \alpha \cos \beta x + \sin \alpha \sin \beta y + \cos \alpha z = R \cos \delta$   
 +:  $x^2 + y^2 + z^2 = R^2$   
 球心:  $x = x_0, y = y_0, z = R \cos \alpha$

球面方程:  $x = \frac{2R^2 x_0}{x_0^2 + y_0^2 + R^2}, y = \frac{2R^2 y_0}{x_0^2 + y_0^2 + R^2}, z = \frac{R(R^2 - x_0^2 - y_0^2)}{x_0^2 + y_0^2 + R^2}$

代入球心:  $2R^2 \sin \alpha \cos \beta x_0 + 2R^2 \sin \alpha \sin \beta y_0 + R(R^2 - x_0^2 - y_0^2) \cos \alpha = R \cos \delta (x_0^2 + y_0^2 + R^2)$

$(\cos \alpha + \cos \delta) x_0^2 - 2R \sin \alpha \cos \beta x_0 + (\cos \alpha + \cos \delta) y_0^2 - 2R \sin \alpha \sin \beta y_0 = R^2 (\cos \delta - \cos \alpha)$

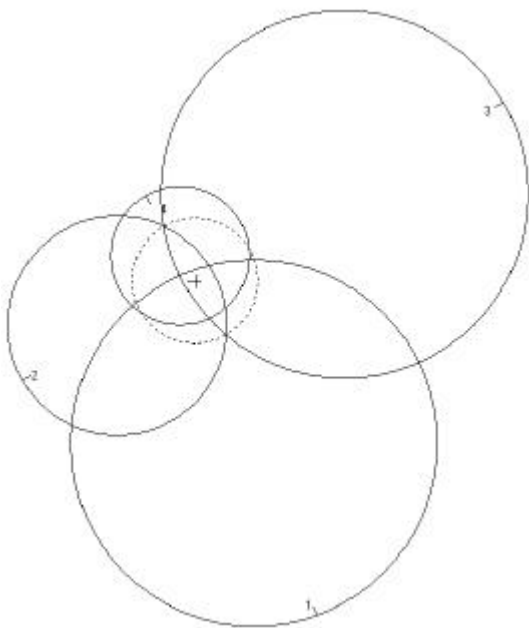
$(x_0 - \frac{R \sin \alpha \cos \beta}{\cos \alpha + \cos \delta})^2 + (y_0 - \frac{R \sin \alpha \sin \beta}{\cos \alpha + \cos \delta})^2 = \frac{\cos \delta - \cos \alpha}{\cos \alpha + \cos \delta} R^2 + \frac{R^2 \sin^2 \alpha}{(\cos \alpha + \cos \delta)^2}$

$= \frac{R^2 (1 - \cos^2 \alpha)}{(\cos \alpha + \cos \delta)^2} = \left( \frac{R \sin \alpha}{\cos \alpha + \cos \delta} \right)^2$

$\therefore (x_0, y_0) = \left( \frac{R \sin \alpha \cos \beta}{\cos \alpha + \cos \delta}, \frac{R \sin \alpha \sin \beta}{\cos \alpha + \cos \delta} \right)$

radius =  $\frac{R \sin \alpha}{\cos \alpha + \cos \delta}$

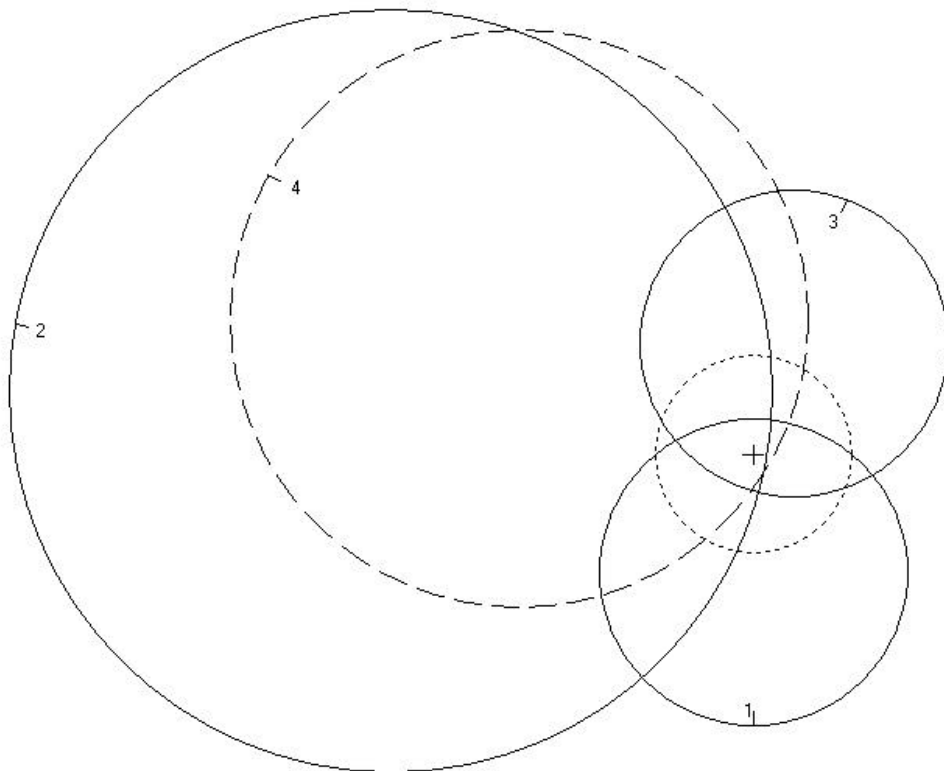
5. There are 4 joint sets around a tunnel of which axis is parallel to north-south. Find joint pyramid codes of removable blocks on a tunnel roof (horizontal plane) and tapered blocks from the following great circles projected by lower-focal-point stereographic projection. (20)



Removable blocks: 1011, 1111, 1110(?), 0111(?)

Tapered blocks: 1001, 0110

6. There are 3 joint sets around a planar rock exposure whose orientation is expressed as a dash-lined great circle in a lower-focal point stereographic projection as below. We installed a rectangular survey window whose width and height are 10 m and 8 m, respectively, on the exposure so that two boundary lines of the window are parallel to horizontal surface. 1) Draw the joint traces of each joint set in the rectangular window when the apparent spacing of each joint on the exposure is about 2 m. 2) Find out several joint pyramid codes of rock blocks observed in the window ignoring the joints possibly intersecting the blocks behind the exposure. Assume that the joints belonging to joint set 1 is large enough that their traces are entirely crossing the window while other joint traces belonging to set 2 and 3 are of 3 ~ 5 m in length in the window. (Key point: to find out the orientation of joint traces from the intersection of great circles) (20)



Rock block behavior analysis

