Mechanical and Aerospace System Analysis Midterm #2

May. 14. 2009

- 1. Briefly answer following questions.
 - A. Explain the golden rules of OP-amp.
- B. Plot a pole placement graph for an under damped second order system.
 - i. On the graph, describe the values of the pole's real and imaginary value using the damping ratio and the natural frequency.
 - ii. What is the relationship between the angle of the line that intersects the origin and the pole, with the damping ratio?
- C. Derive the %OS of a 2^{nd} order system with C(s)

$$C(s) = \frac{\omega_n^2}{s(s^2 + 2\zeta\omega_n s + \omega_n^2)}$$

- D. Answer the following for a system with poles shown in the graph below.
 - i. What is the settling time(2%) and the peak time of a system with the poles shown in the pole placement graph below?
 - ii. Describe what is needed in order to reduce the settling time to 1/2 of the current value, without changing the % overshoot?



2. A small DC motor is used to spin a disk with an OP-amp as illustrated in the figure. In this application, we do not want the disk to spin up very fast, so a dynamic filter is added to the OP-amp. (the back emf: K_b, the motor torque constant: K_t, Voltage Amp Gain: G)



- A. Derive the transfer function of the OP-amp, $E_0(s)/E_i(s)$
- B. Derive the transfer function of the Motor system $\omega(s)/E_m(s)$
- C. Write the transfer function of the whole system.
- D. What is the settling time of the system?
- E. What is the peak time of the system?
- F. If you want to decrease the peak time, how would you change the components in the OP-amp?
- G. If you want to reduce the overshoot, how would you change the components in the OP-amp?
- 3. The figure shows a double-acting piston and cylinder. The device moves the load mass m and spring with a spring constant k in response to the pressure sources p₁ and p₂. Assume the fluid is incompressible, the resistances are linear and the piston mass is included in m.



- A. What is/are the input(s) to the system?
- B. Derive the equation of motion for the mass m and write the transfer function(s) of the system.
- C. What is the settling time (2%) of the system?
- D. What is the peak time of the system?
- E. In order to change the dynamics of the system, you can turn the knob of the valve R₁. How would you turn the knob in order to reduce the % overshoot?

4. The cylindrical tanks shown in the figure has circular bottom areas A_1 and A_2 . The mass inflow rate $q_i(t)$ from the flow source is a function of time. The resistances are linear and the outlet discharges to atmospheric pressure p_a . (at initial time, $h_1=0$, $h_2=0$)



- A. Derive a model of the liquid level height h_1 and h_2
- B. $R_1 = R_2 = R$ and $A_1 = A$ and $A_2 = 3A$. obtain the transfer function $H_1(s)/Q_i(s)$
- C. Solve for the steady state response h_1 for a unit step input of $q_{mi}(t)$. Hint: Use the transfer function.
- D. What is the rise time of the system?
- E. Can the system oscillate? Explain why or why not.
- F. Obtain the transfer function of $Q_o(s)/Q_i(s)$.
- G. Solve for the steady state response of $q_o(t)$ for a unit step input of $q_{mi}(t)$. Hint: Use the transfer function.