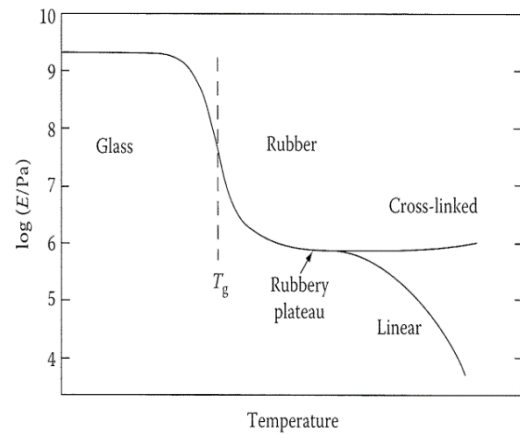


*Total of 97 points. Answer the following questions in a concise manner.*

1. [3 + 2 + 2 + 4 + 3 points] **A plate with the dimension of 100 x 100 x 5 mm<sup>3</sup> formed from a polymeric material with the Young's modulus of 2.0 GPa is subjected to a biaxial load of 25 kN along the two directions on the largest plane. Answer the following questions.**
  - (a) Express the stress state in a [3 x 3] matrix form. Don't forget the unit.
  - (b) To calculate the final dimension of the plate you need to assume that the polymer is isotropic. What other assumption do you need (about the behavior of the polymer)? Why?
  - (c) What additional information do you need to predict the final dimension of the plate? What would be the reasonable value for that?
  - (d) Estimate the final thickness of the plate using the value you gave in (c).
  - (e) Does the result of (d) justify the assumption you made in (b)? Explain.
2. [3 x 3 points] **There are two mechanical models for linear viscoelasticity; Maxwell and Voigt models. They are composed of one spring element with the modulus  $E$  and one dashpot element with the viscosity  $\eta$ .**
  - (a) Show the constitutive equation for a creep test of a Maxwell model with the given stress of  $\sigma_0$ .
  - (b) Show the constitutive equation for a stress relaxation test of a Voigt model with the given strain of  $\epsilon_0$ .
  - (c) One of the problems of the models results from the fact that they have single \_\_\_\_\_ or \_\_\_\_\_, which is unrealistic. Fill the both blanks.
3. [4 x 3 points] **For the construction of 'master curve' on modulus vs time plot using the time-temperature superposition principle, answer the following questions.**
  - (a) Vertical shift (in modulus) can be ignored. Why?
  - (b) For horizontal shift (in time), does the results at a temperature higher than the reference temperature shift to a shorter or longer time frame? Why?
  - (c) When the reference temperature is set to the \_\_\_\_\_ temperature, the amount of horizontal shift is given by the \_\_\_\_\_ equation. Fill the both blanks. For the second one, no need to spell out.
  - (d) What is the two constants in the equation of (c) called? Why are they called so?
4. [5 + 3 x 3 points] **For a polymer that follows pressure-dependent Tresca yield criterion and critical-strain craze criterion, answer the following questions.**
  - (a) It is observed that this polymer undergoes shear yielding at a stress of 60 MPa in uniaxial tension and at 70 MPa in uniaxial compression at the strain rate of 10 mm/min. It is also observed that the polymer undergoes crazing at a stress of 50 MPa in uniaxial tension and at 40 MPa in biaxial tension. Show the yield and craze locus on  $\sigma_1$ - $\sigma_2$  coordinate.
  - (b) Is this polymer ductile or brittle upon biaxial compression? Explain your answer using your drawing of (a).
  - (c) Show how the drawing changes when the strain rate increases to 100 mm/min.
  - (d) Show by drawing that a ductile-brittle transition can occur with the increase in testing temperature.

5. [4 x 3 points] Referring to the figure on the right, answer the following questions.



- As the average molar mass of an amorphous polymer increases, would the width (in temperature) of rubbery plateau increase, decrease, or remain the same? Why?
- As the average molar mass of an amorphous polymer increases, would the level (in modulus) of rubbery plateau increase, decrease, or remain the same? Why?
- As the crystallinity of a semi-crystalline polymer increases, would the level (in modulus) of rubbery plateau increase, decrease, or remain the same? Why?
- As the average molar mass between the crosslinks of a rubber increases, would the level (in modulus) of rubbery plateau increase, decrease, or remain the same? Why?

6. [9 x 2 points] Fill the blanks in the description of the fracture stress [ $\sigma_f$ ] of polymers.

- The theoretical fracture stress of a material is one-tenth of its (a1)\_\_\_\_\_. However, the measured  $\sigma_f$  is much smaller than this due to the existence of flaw or crack, which results in (a2)\_\_\_\_\_ and (a3)\_\_\_\_\_.
- In front of a crack, exceedingly high stress resulted from (a2) is cut off by (b1)\_\_\_\_\_ of the polymer, and the material undergoes (b2)\_\_\_\_\_. This is the reason why  $\sigma_f$  measured is much larger than that estimated based on the (b3)\_\_\_\_\_ that are created by crack propagation.
- Since both of the low  $\sigma_f$  of (a) and the high  $\sigma_f$  of (b) are due to the existence of crack, it is called (c)\_\_\_\_\_, following the name of the scientist who suggested the both.
- (a3) in front of a crack tip is due to the (d1)\_\_\_\_\_ stress state, which make the (b2) occur at a higher (b1). (a3) can explain the ductile-brittle transitions with the change in (d2)[temperature, strain-rate, surface crack, specimen thickness] (Choose two).

7. [6 x 3 points] Answer the following questions in one sentence. No drawing or equation.

- Why is a rubber called 'entropy spring'?
- Why is a polymer melt 'pseudo-plastic', while some colloids or suspensions 'dilatant'?
- Why is a PRP not as efficient in reinforcing [enhancing modulus] as an FRP with the same matrix and reinforcement materials?
- Why is the dielectric constant of a polymer related to its solubility parameter?
- How is the thermal stability different from the heat resistance?
- Why is the flame resistance of a polymer related to its thermal stability?