

# Design of Piezoelectric Active Structures

## Lecture 1:

### Introduction to Active Materials and Structures

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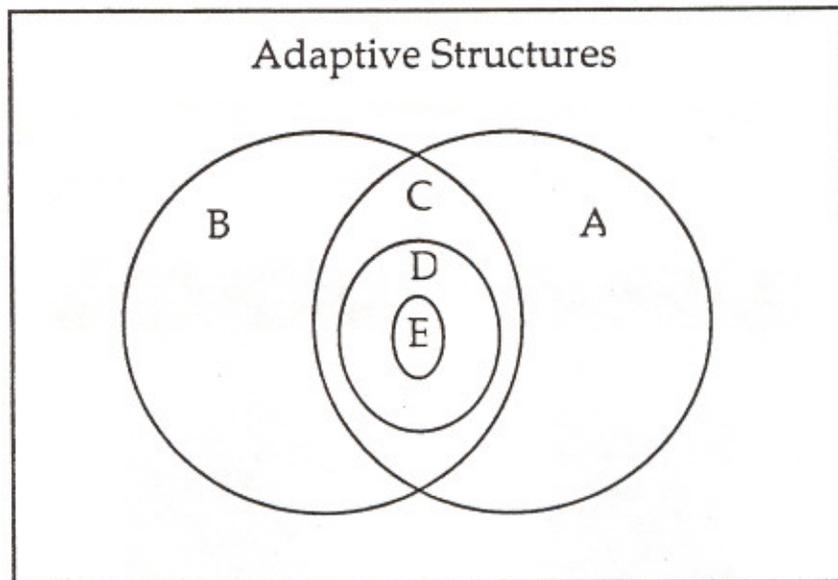
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# Adaptive Structures

- An Adaptive Structure is one whose characteristics can be beneficially changed in response to environmental stimuli.
- Characteristics :
  - shape, stiffness
  - vibration response
  - acoustic reflectivity
  - radar signature, etc.
- Stimuli :
  - external force disturbances
  - pressure fields,
  - thermal loading
  - applied voltages and control signals
- Controllable Response allows new functionality to meet mission requirements such as precision pointing, stealth, etc.
- The goal of the technology is to develop adaptation mechanisms, sensing mechanisms, and processing hardware and algorithms which can enhance the performance of an aerospace structure and vehicle.

# Classifications



- A **Actuated Structures** possess actuation/adaptation mechanisms
- B **Sensory Structures** possess capability to sense environment
- C **Controlled Structures** couple actuation and sensing with processing
- D **Active Structures** have integrated actuators and sensors
- E **Intelligent Structures** have integrated/distributed processing.

# Applications for Active Structures

- Vibration Suppression
  - Precision Pointing of Optical Systems
  - Precision Machining
- Active Noise Control
  - Structural Acoustics
  - Modification of Acoustic Reflection and Transmission
- Optics
  - Static Optical Positioning and Surface Correction
  - Adaptive Optics - Dynamic Wavefront Correction
- Flow-Structure Interactions
  - Static Aeroelastic Control
  - Gust Load Alleviation
  - Flutter Suppression
  - Boundary Layer Control
- Structural Health Monitoring
- Solid State Motors and Articulating Devices

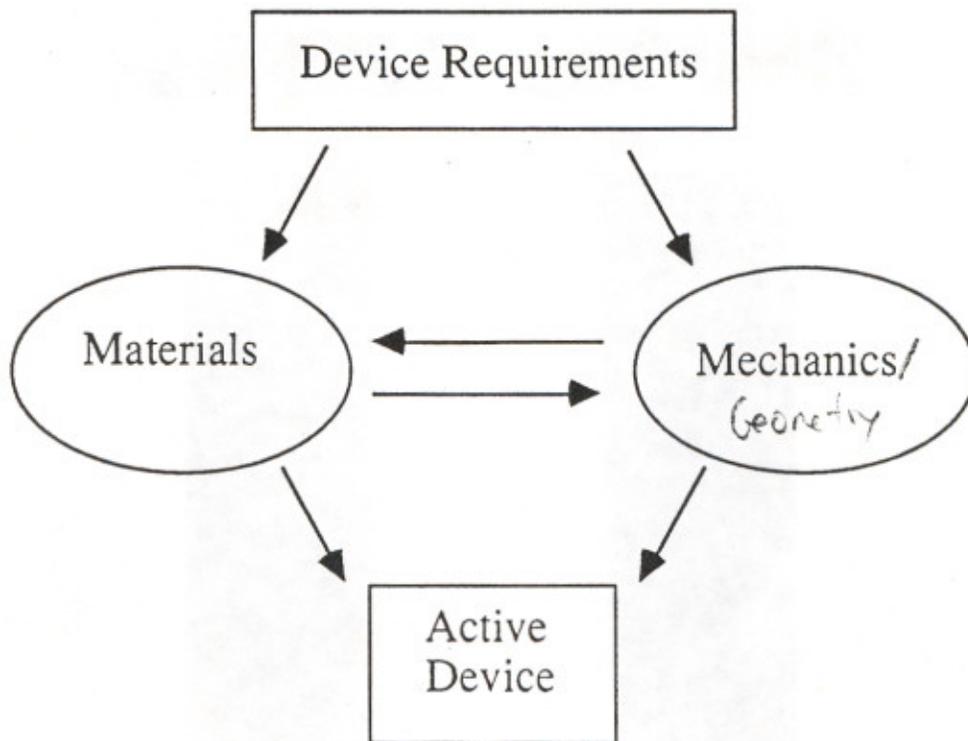
# Survey of Adaptation Mechanisms

- Adaptation properties are usually associated with a given active material which is incorporated into the structure.
- Controllable Size (Induced Strain Actuation)
  - Electrically: Piezoelectric Ceramics  
Piezoelectric Polymers  
Electrostrictive Materials  
Shape Memory Ceramics
  - Thermally: Shape Memory Alloys  
Thermoelastic Materials
  - Magnetically: Magnetostrictive
  - Optically: Photoelastic Materials  
*Chemically*
- Controllable Stiffness
  - Thermally: Shape Memory Alloys  
Viscoelastics
  - Electrically: Electrostrictives
  - Magnetically: Magnetostrictives
- Controllable Viscosity
  - Thermally: Water
  - Electrically: Electrorheological Fluids  
*Magneto-rheological Fluids*
- Electrical Conductivity, Resistivity, Transmission
  - Electrically: Transistors
  - Mechanically: Strain Gauges
  - Optically: Photochromatic Glasses
- Some materials operate as transducers and can therefore be used as sensors. e.g.. Piezoelectrics

• Solid State Actuators - Sensors

# Design of Active Structures/Devices

- Design of active devices requires coordinated selection of mechanical, electrical parameters as well as selection of material and operating environment. - based on requirements.



- The 2 fundamental design problems:
  - 1) The active material is an integral part of the structure, and therefore the actuation or sensing is entirely dependent on host/actuation elastic interaction. - elastic actuators and sensors
  - 2) The active element usually couples electric, magnetic and mechanical fields in the material.

*-material physics*

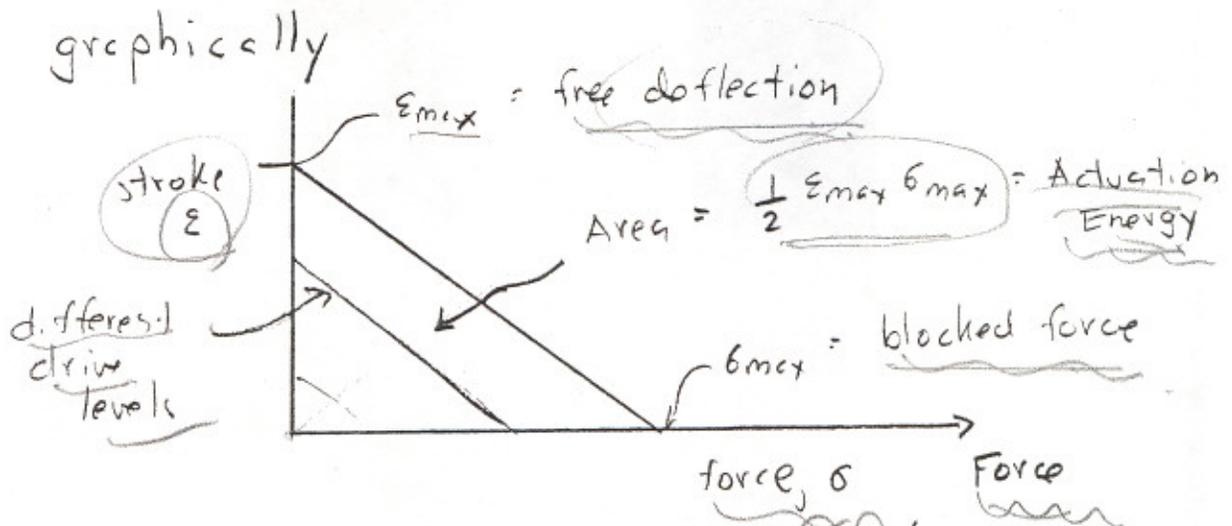
## Active Material Selection Criteria

- Broad range of materials: Piezoelectrics, electrostrictors available as ceramics, piezoelectrics also in polymer form, magnetostrictors and shape memory alloys available as metal alloys.
- Within each type there are many variants. eg. PZT-4 (Navy Type I), PZT-5A (Navy Type II), PZT-5H (Type VI) etc.
- Large variation in:
  - modulus, anisotropy,
  - mechanical strength, fracture toughness
  - dielectric strength,
  - maximum actuation strain,
  - maximum inducible stress,
  - sensitivity to input fields,
  - temperature ranges for operation,
  - property stability over time
  - frequency response, hysteresis
  - linearity,
  - availability, cost.
- Need coherent modeling and design capability to establish relative material performance for a given application.

# Actuation Figures of Merit

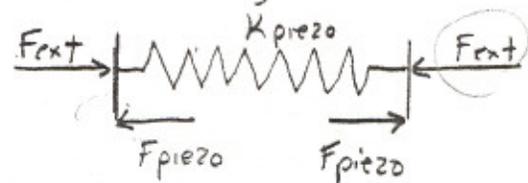
- Stroke Actuation (induced strain)  
 Max stroke ( free strain) at highest field allowable  
Strain/field if field is limited
- Force Actuation (induced stress)  
 Max Force (clamped stress) at highest field allowable  
Stress/field if field is limited
- Same types with applied charge rather than electric field.
- More complicated in distributed problems since it is no longer uniaxial.

graphically



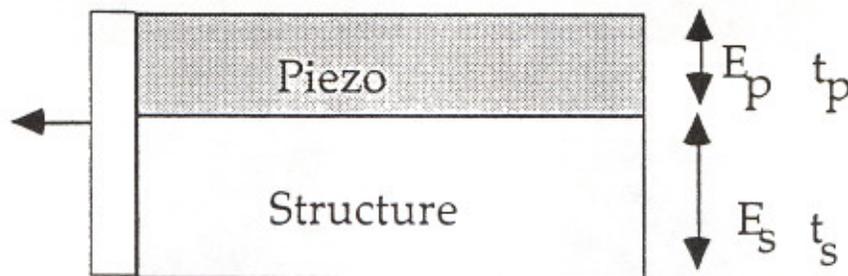
• Actuation Energy Density =  $\frac{1}{2} \epsilon \sigma / \rho$

• Simple 1-D model



## Elastic Actuation - I

- Must really consider the coupled active material/substructure system
- Simple Bar Example:



- Possible figure of merit for coupled system: maximum strain induced in a bar with surface bonded actuation strain material.

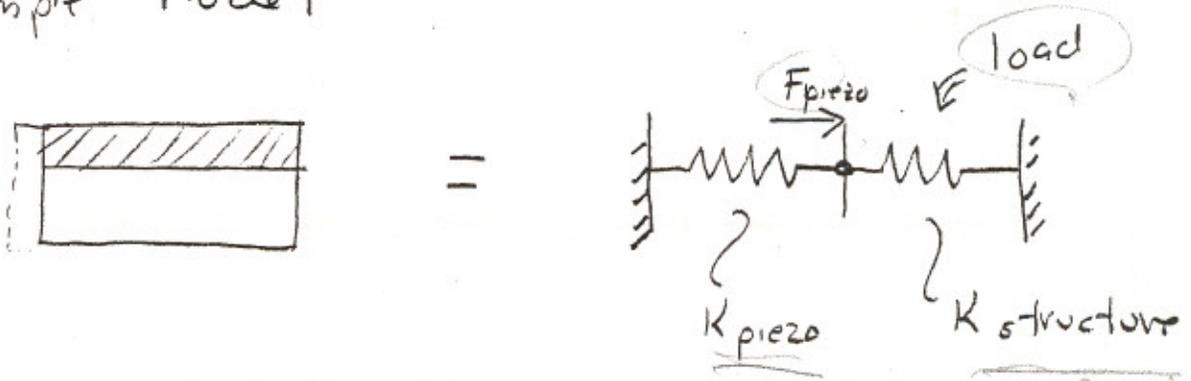
$$\varepsilon_{tot} = \varepsilon_{p_{max}} \left( \frac{1}{1 + \Psi} \right)$$

$$\Psi = \frac{E_s t_s}{E_p t_p} = \frac{K_s}{K_p}$$

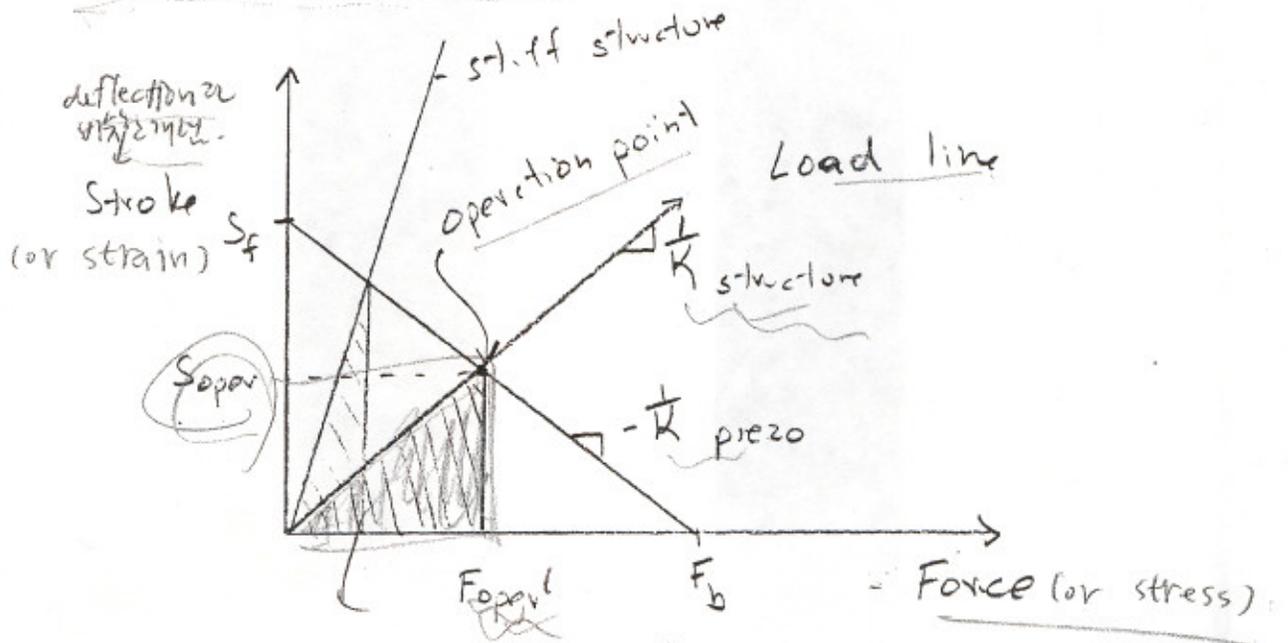
- Actuation strain and material stress depend on *relative* values of active material and structure.

# Elastic Actuation - II

## Simple Model



## Graphical Representation

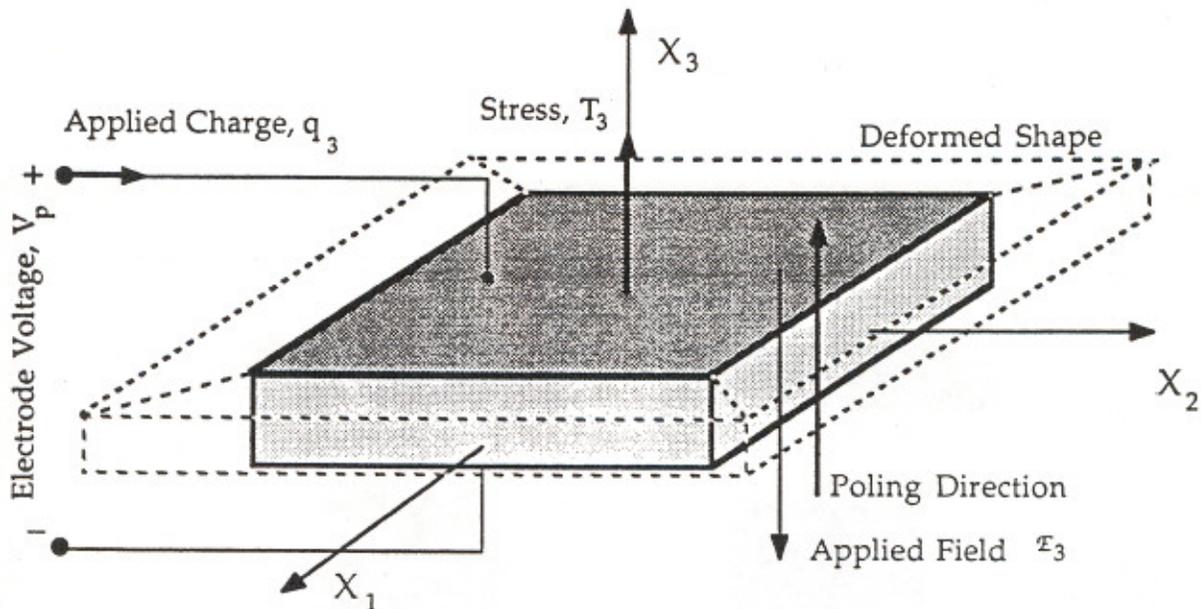


area: energy transferred to the system.  
linear

Max work delivered to load is  $\frac{1}{4} \frac{F_b S_f}{2}$

when  $K_{structure} = K_{piezo}$   
(impedance matching)

# What is Piezoelectricity?



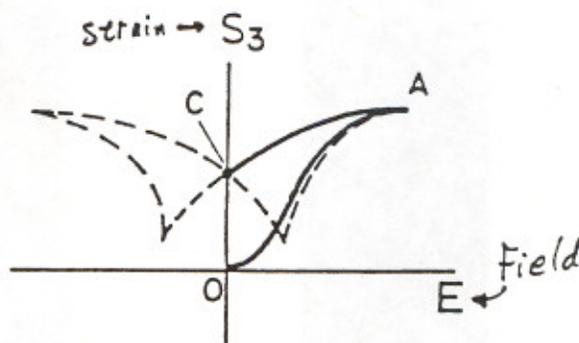
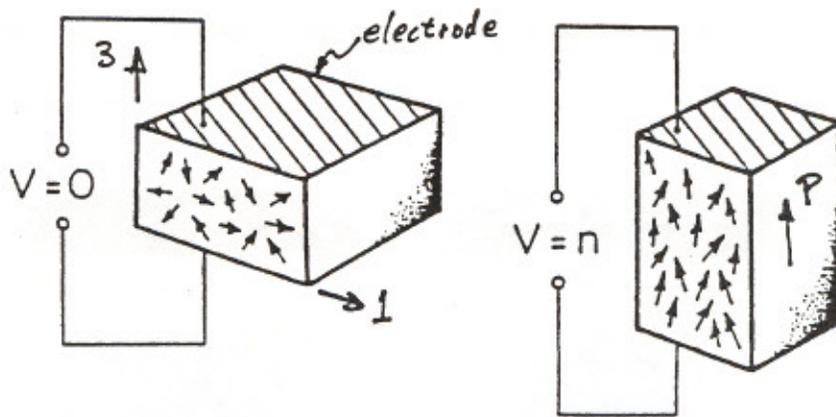
- Piezoelectric causes deformation when voltage is applied (or vice-versa).
- Piezoelectric actuation strain enters equations in a manner analogous to thermal strain but is field dependent.
- High bandwidth, well into structural acoustic range.

## Piezoelectric Materials in Structures

- Piezoelectric materials have been modelled in surface bonded and embedded configurations in beams, plates, and tubes.
- Intelligent structures have been manufactured with piezoelectric materials embedded in glass/epoxy and graphite /epoxy laminates.
- Piezoelectric materials have been used in passive damping applications as a replacement for viscoelastic materials.
- Piezoelectric materials have been used as actuators in active structural control applications such as structural vibration, aeroelastic, and acoustic control.

# Active Damping Workshop

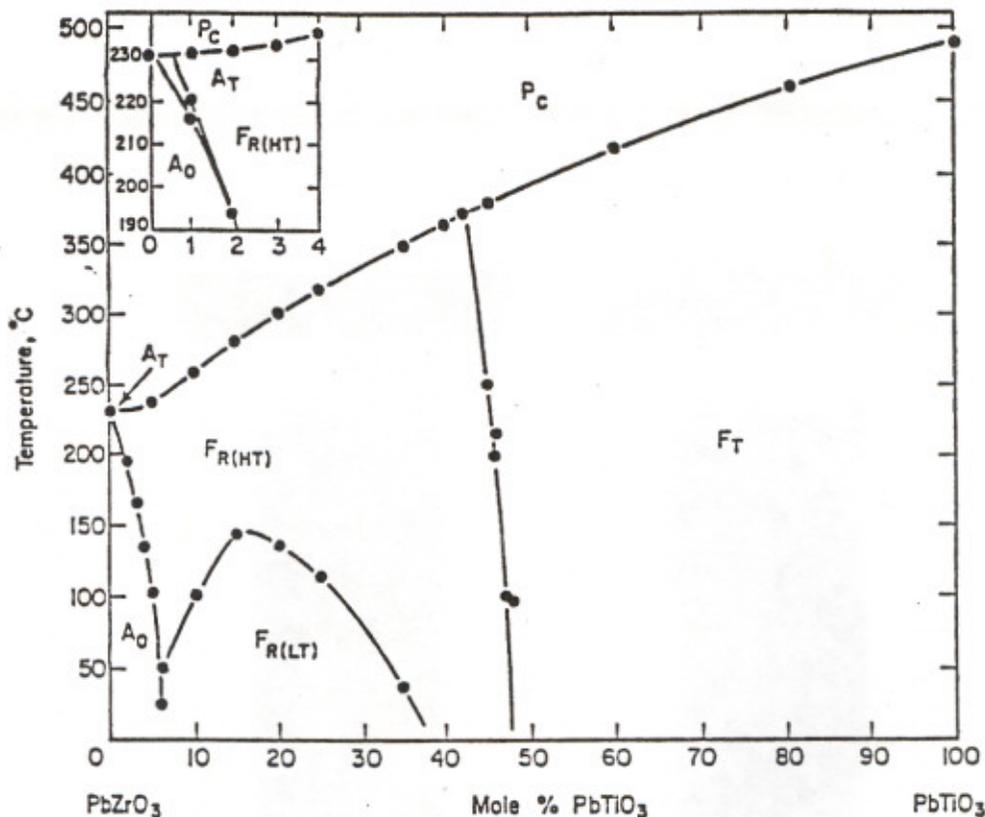
## Piezoelectric Action



- Poling, or application of a large coercive field on the order of 50 Volts/mil, aligns crystalline subdomains in the ceramic.
- Poling causes the ceramic to grow in the field direction and to shrink laterally, roughly according to Poisson's ratio.
- Subsequent application of field in the poling direction also causes the ceramic to grow in that direction.
- Application of reverse field causes the ceramic to shrink until a negative coercive field level is reached. Poling action then switches and the ceramic grows again. Hence the "butterfly" curve.

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## PZT Phase Boundaries



- PZT is a solid solution of lead zirconate (PbZrO<sub>3</sub>) and lead titanate (PbTiO<sub>3</sub>). The ratio of these two molecules and addition of other trace compounds determines the phase transition boundaries, and hence the properties.
- PZT and Barium Titanate are Perovskite ceramics. PZT has somewhat better piezoelectric and dielectric properties.
- These Perovskites have very high dielectric constants (capacitance) relative to free space of  $D' \sim 1700$ . This is due to offsets in the charged ions in the crystal lattice. The previous highest known material had  $D' \sim 30$ .
- The electric offsets in the crystal lattice also cause very high mechanical strains when subjected to a field, and conversely.

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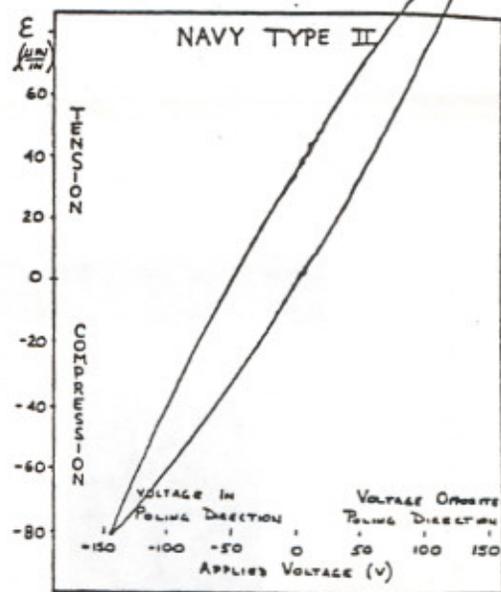
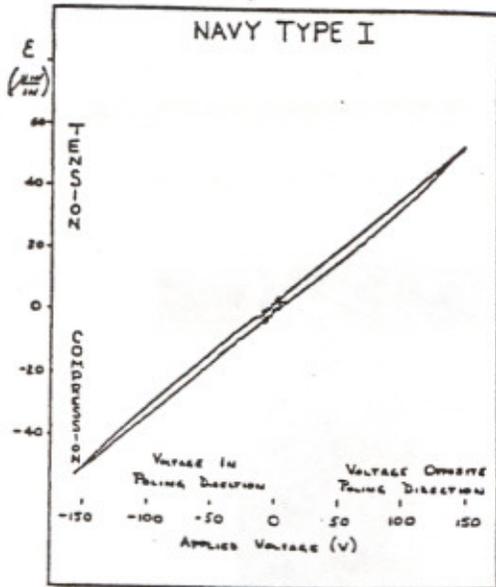
## PZT Actuators

- Principle: Bond or embed piezoelectric wafer on surface. Apply voltage  $V$  across electrodes generating field  $\Phi = V / t$ . Actuate in lateral mode (note  $d_{33} \sim 2.5 \times d_{31}$ )  
 Max Free Strain:  $\epsilon_{\max} = \Phi_{\max} d_{31} \sim 120 \mu\text{-strains}$  (Type II)  
 Max Blocked Stress:  $\sigma_{\max} = E \Phi_{\max} d_{31} \sim 1,100 \text{ psi}$   
 Max Line Force for 7.5 mil wafer:  $N_{\max} = \sigma_{\max} t \sim 8 \text{ lb/inch}$  (requires 150 Volts DC)
- Attaching PZT to structure drops strain levels by stiffness ratio:  $E_p t_p / (E_p t_p + E_s t_s)$
- To Push on a Stiff Structure You Need a Hard Ceramic!

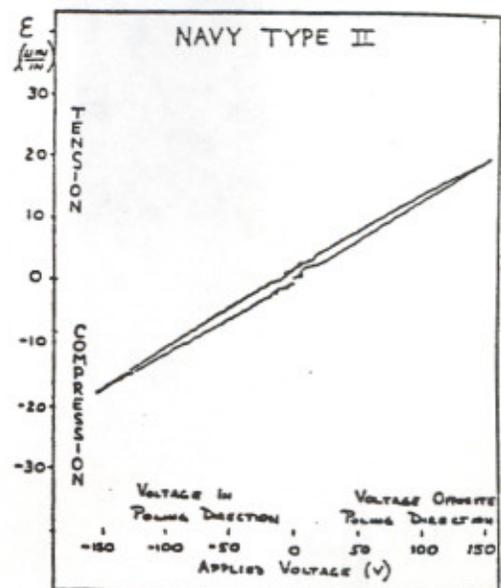
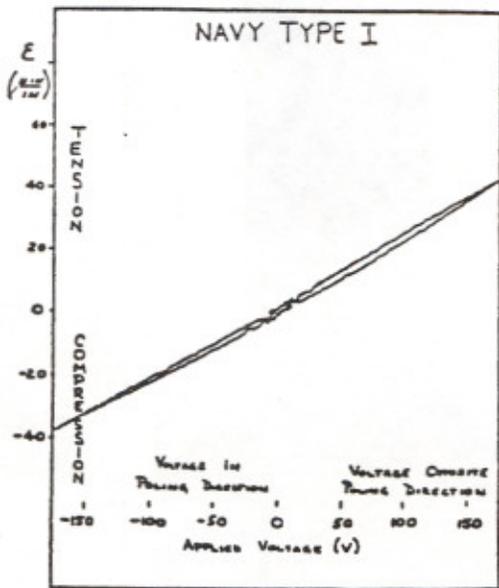
| Quantity            | Description           | Units                                   | Material |          |         |                  |
|---------------------|-----------------------|---|----------|----------|---------|------------------|
|                     |                       |   | Type I   | Type II  | PZWT    | PVF <sub>2</sub> |
| $d_{31}$            | Lateral Strain Coeff. | m/V or C/N                              | 1.23e-10 | 1.66e-10 | 2.8e-10 | 0.23e-10         |
| $\epsilon_{AC}$     | Max AC Field          | V/m                                     | 1.6e6    | .71e6    | 1.6e6   | 30.e6            |
| $\epsilon_R$        | Max Reverse Field     | V/m                                     | 1.6e6    | .71e6    | .39e6   | 7.9e6            |
| $d_{31} V_R$        | Max Reverse Strain    | m/m                                     | 2.0e-4   | 1.2e-4   | 1.1e-4  | 1.8e-4           |
| $E$                 | Young's Modulus       | N/m <sup>2</sup> (Pa)                   | 9.9e10   | 6.9e10   | 4.8e10  | 2e9              |
| $Ed_{31}$           | Stress per Field      | (N/m <sup>2</sup> )/(V/m)               | 12.2     | 11.5     | 13.4    | .046             |
| $Ed_{31}\epsilon_R$ | Max Reverse Stress    | N/m <sup>2</sup>                        | 19.5e6   | 8.2e6    | 5.2e6   | 0.36e6           |
| $D$                 | Permittivity          | Farad/m                                 | 1.3e-8   | 1.5e-8   | 2.9e-8  | 1.06e-10         |
| $Ed_{31}/D$         | Stress per Charge     | (N/m <sup>2</sup> )/(C/m <sup>2</sup> ) | 9.4e8    | 7.7e8    | 4.6e8   | 4.3e8            |

# Active Damping Workshop

## PZT Actuation Comparison



Free PZTs



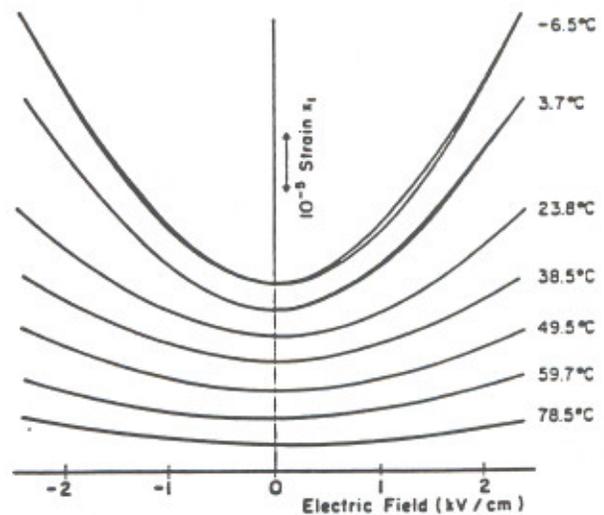
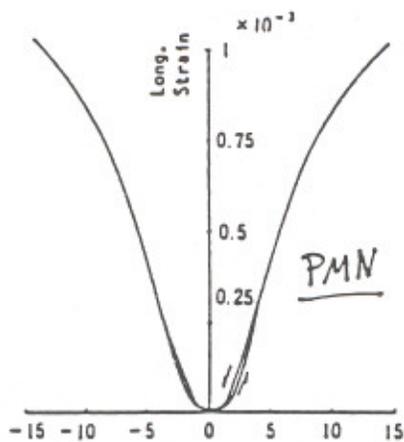
PZTs Embedded in Graphite/Epoxy

Type I has lower intrinsic hysteresis & better stiffness match to graphite.  
Type II has higher free strain. Embedding decreases hysteresis.

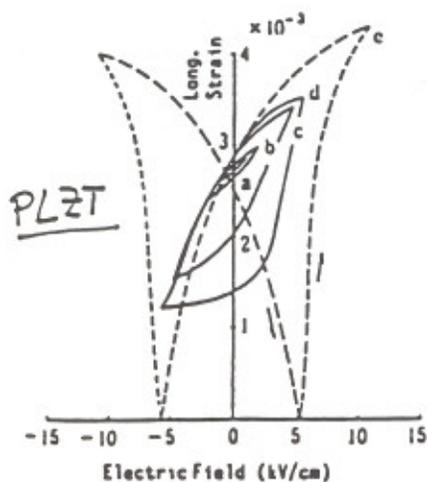
# Active Damping Workshop

## Electrostrictive Ceramics

- Lead Magnesium Niobate (PMN) is a Perovskite crystal.
- Application of field (+/-) causes the crystal to grow longitudinally and shrink laterally.
- Strain Effect is Quadratic in Voltage and Decreases with Temperature.
- Vibration damping requires a bias voltage.
- Low hysteresis makes PMN suitable for open loop optical shape control.

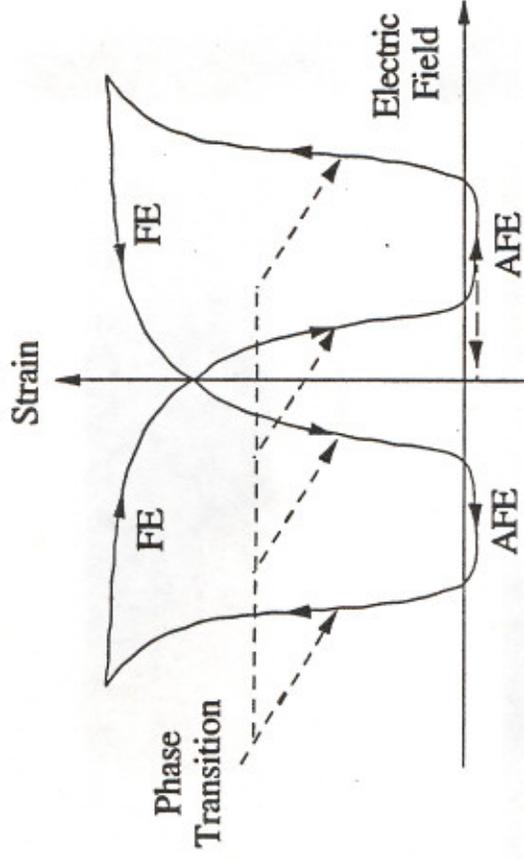


PMN vs. Temperature



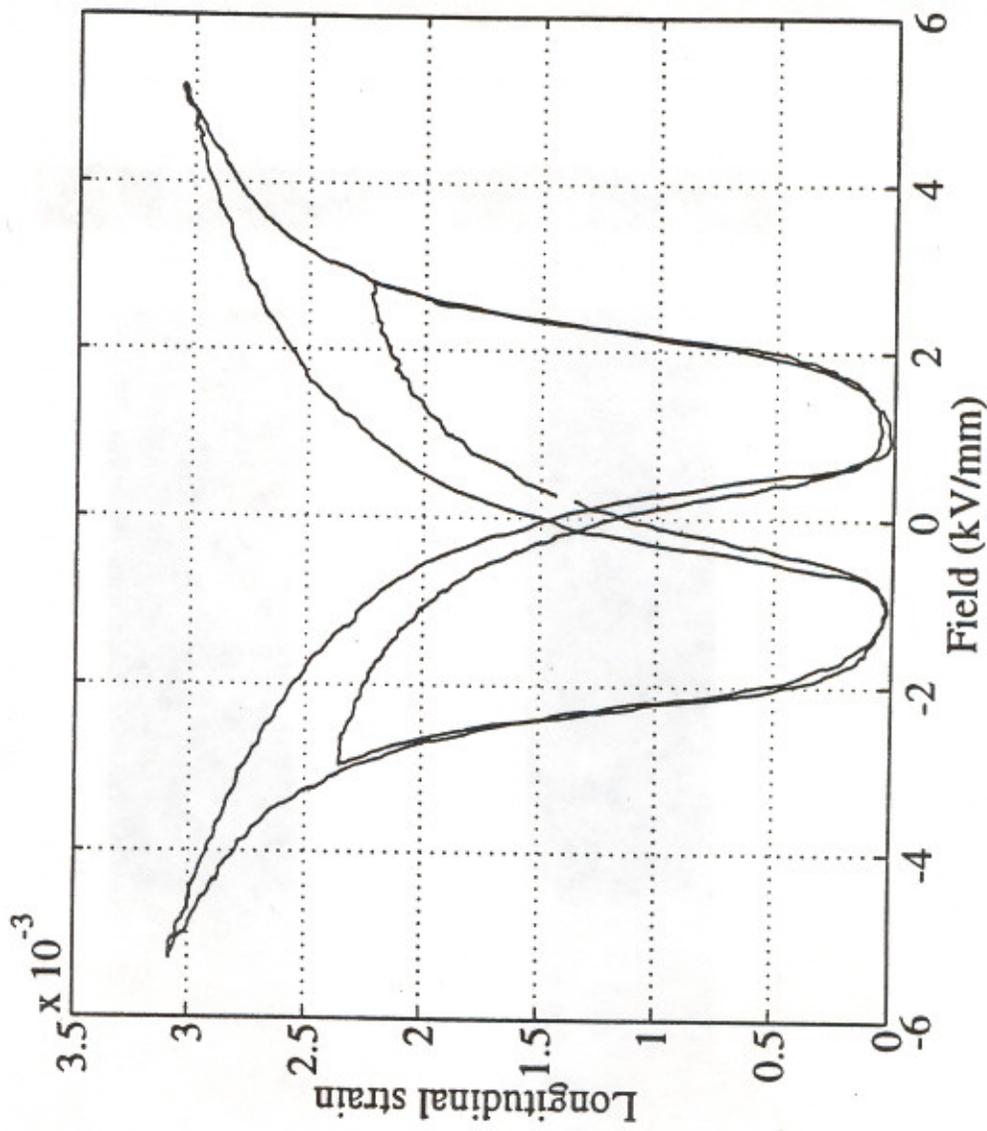
## Shape Memory Ceramics

- Concept: Electric field induces phase transition between Ferroelectric (FE) and anti-ferroelectric (AFE) phases:



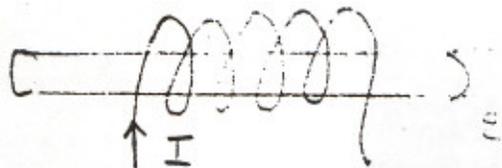
- Large isotropic strains (0.5%) accompany transition between phases  
Material exhibits shape memory and requires electric field or stress to return to original state
- High switching rates permit high bandwidth applications: Adaptive Mirrors and Optics (JPL), Antennas

# High Field Experimental Data for PLZST (A3)



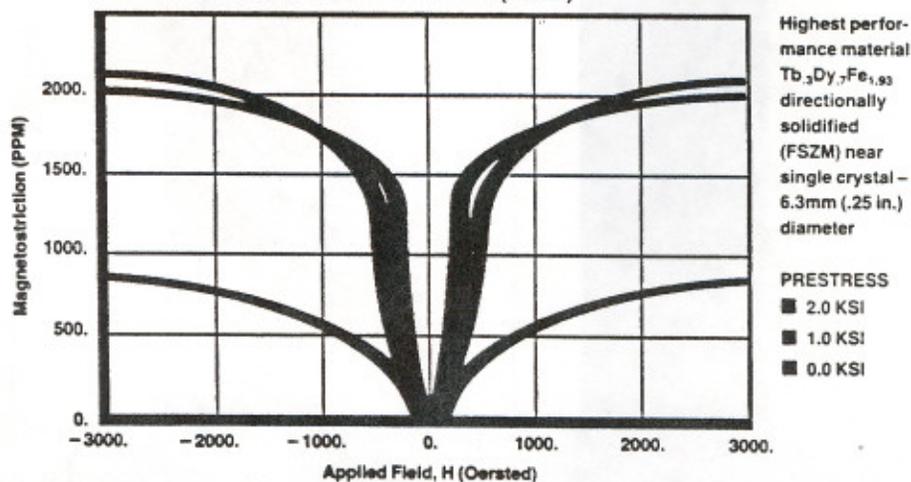
# Magnetostrictive Materials

- Discovered by James Joule, 1840 in Nickel
- Terfenol-D is an alloy of Iron, Terbium, and Dysprosium developed in late 70's by the Navel Ordinance Lab.
- Typical Configuration:



$$H = nI = \text{coercive field (A / m)}$$

- Coercive Field - Strain Curve

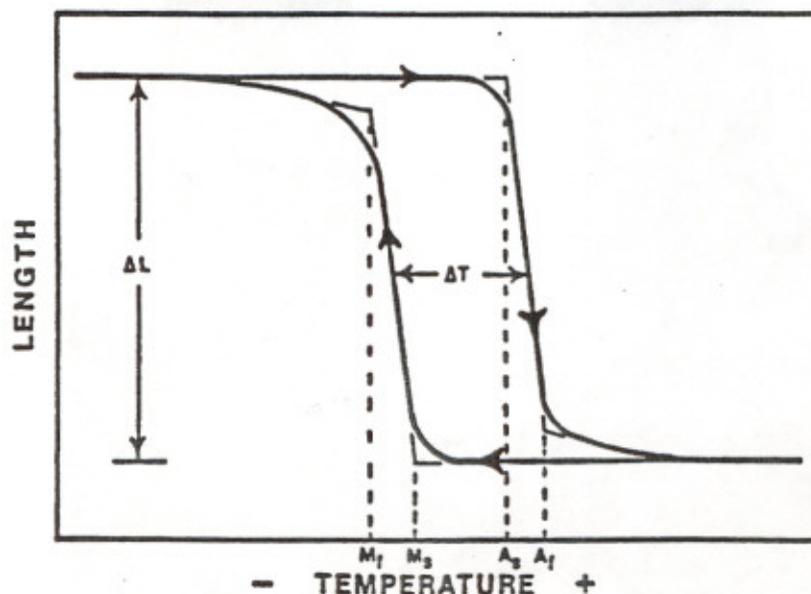


Material is typically biased magnetically  $h = 500-1000$  Oersteads ( $=1000/4\pi$  A/m) to produce linear properties

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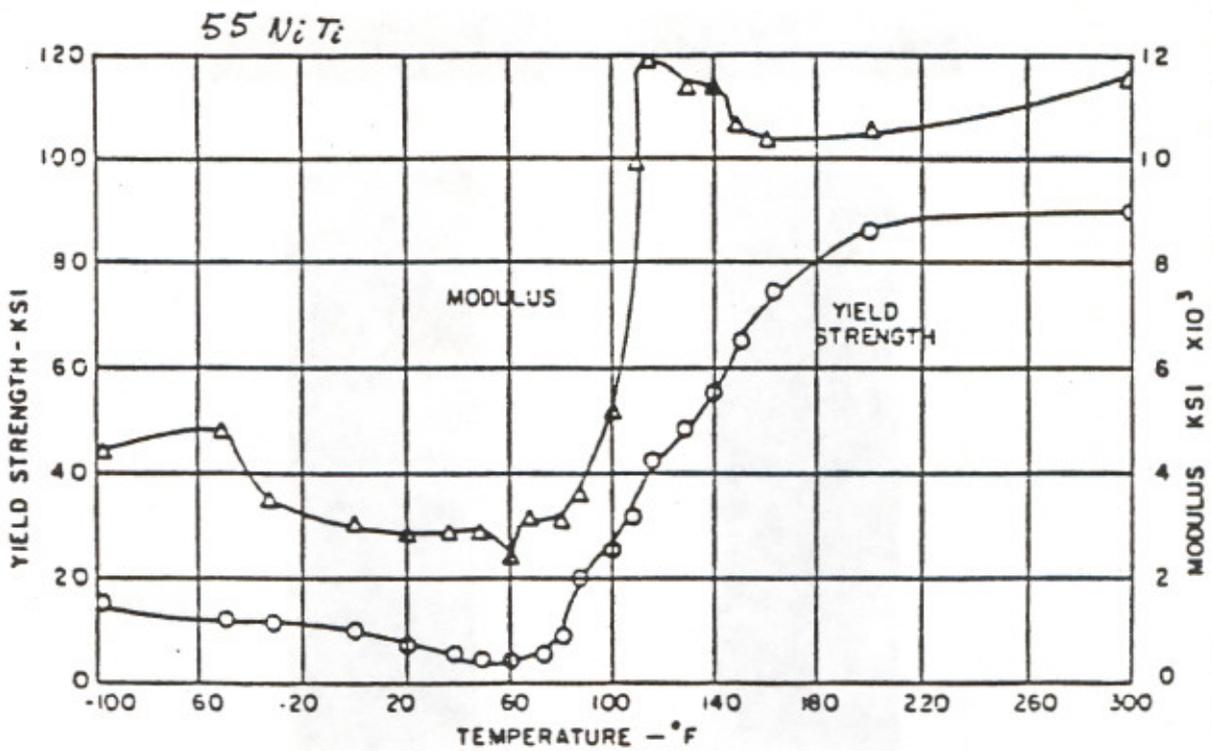
## Shape Memory Metals

- Nitinol is the most widely used SMM. It is a Nickel-Titanium alloy developed at the Naval Ordnance Laboratory.
- The high temperature phase is Austenitic.
- The low temperature phase is Martensitic.
- Transition Temperature (TTR) can be adjusted by varying alloy. TTR is stress dependent.
- Nitinol working stress = 25,000 psi  
working strain = 3.5%.
- To pull one must heat SMM wire with electric current  
To push one must cool by convection, conduction and/or radiation.
- Vibration damping frequency is limited by maximum cooling rate and hysteresis. Control demonstrated to 3 Hz.
- Difficult to control temperature accurately.
- CTE mismatch makes attachment to structure difficult.



# Active Damping Workshop

## Nitinol Properties Vs. Temperature



# Comparison of Commercially Available and Potential Actuation Materials

|                                 | PZT-5H        | PVDF       | PMN              | TERF-DZ          | NITINOL            | PLZST                |
|---------------------------------|---------------|------------|------------------|------------------|--------------------|----------------------|
| Actuation Mechanism             | piezo-ceramic | piezo film | electro-strictor | magneto-strictor | shape memory alloy | shape memory ceramic |
| $\epsilon_{max}$ (strain)       | 0.13%         | 0.07%      | 0.1%             | 0.2%             | 2%-8%              | 0.3%-0.9%            |
| E (Msi)                         | 16 (D)        | 0.3        | 17               | 7                | 4 (m), 13 (a)      | 12 (FE)              |
| $\sigma_{max}$ (kpsi)           | 20.8          | 0.21       | 17               | 14               | 26 - 104           | 36-108               |
| Density (kg/m <sup>3</sup> )    | 7500          | 1780       | 7800             | 9250             | 7100               | 7500                 |
| Actuation Energy Density (J/kg) | 13.5          | 0.285      | 7.51             | 10.4             | 252-4032           | 49.6-446             |
| Hysteresis                      | 10%           | >10%       | <1%              | 2%               | High               | High                 |
| Temp Range                      | -20C to 200C  | Low        | 0C to 40C        | High             | -                  | 0C to 40C            |
| Bandwidth                       | 100kHz        | 100kHz     | 100kHz           | <10kHz           | <5Hz               | <100Hz               |

(m) = martensite (a) = austenit (FE) ferroelectric (D) = open circuit  
 Actuation Energy Density =  $1/2 \epsilon_{max} \sigma_{max} / \rho$

## Sensing Figures of Merit

- Consider sensing of mechanical fields (stress or strain). Sensing duals are:

|             |         |         |
|-------------|---------|---------|
| Electrical: | Voltage | Charge  |
| Magnetic:   | Current | Voltage |
- Volt per stress or strain
- Charge per stress or strain
- In the sensing case you usually look at the normalized figures of merit since you rarely exceed material capability - exception is high stress of piezoceramic.

# Active Damping Workshop

## PZT Sensor Example

Material Properties for Navy Type II PZT & PVF<sub>2</sub> Film

| Quantity  | Description                | Units                                | Material |              |
|-----------|----------------------------|--------------------------------------|----------|--------------|
|           |                            |                                      | Ceramic  | Film         |
| $d_{31}$  | Lateral Strain Coefficient | m/V or Coul/N                        | 1.8e-10  | 23e-12       |
| $d_{33}$  | Axial Strain Coefficient   | "                                    | 3.6e-10  | 33e-12       |
| $d_{15}$  | Shear Strain Coefficient   | "                                    | 5.4e-10  | n.a.         |
| $E$       | Young's Modulus            | N/m <sup>2</sup> or Pascal           | 6.30e10  | 2e9          |
| $G$       | Shear Modulus              | "                                    | 2.34e10  | n.a.         |
| $\nu$     | Poisson's Ratio            | -                                    | 0.35     | n.a.         |
| $Ed_{31}$ | Actuation & Sensing        | N/m/V or Coul/m <sup>2</sup>         | 11.34    | .046         |
| $D_0$     | Free Space Permittivity    | Farad/m or N/V <sup>2</sup>          | 8.85e-12 | =            |
| $D'$      | Relative Permittivity      | -                                    | 1700     | 12           |
| $D$       | Absolute Permittivity      | "                                    | 1.5e-8   | 1.06e-10     |
| $\rho$    | Resistivity                | $\Omega$ -m or V <sup>2</sup> -sec/N | 1e10     | 1e13         |
| $\alpha$  | CTE                        | $\mu$ -strain/ $^{\circ}$ K          | 5        | $\sim$ 30-40 |
| $p$       | Pyroelectric Coefficient   | Coul/(m <sup>2</sup> $^{\circ}$ K)   | 4e-4     | 2.5e-5       |
| $k$       | Boltzmann's Constant       | Joules/ $^{\circ}$ K                 | 1.38e-23 | =            |

- Lateral Mode PZT Sensor: 1" x 1" x .0075"  
 $Q = 7.1e-9$  Coulomb /  $\mu$ -strain  
 $C = .05$   $\mu$ -Farads :  $V = Q/C = .14$  Volts /  $\mu$ -strain
- Lateral Mode PVF<sub>2</sub> Sensor: 1" x 1" x .002"  
 $Q = 2.9e-11$  Coulomb /  $\mu$ -strain  
 $C = .0013$   $\mu$ -Farads :  $V = Q/C = .022$  Volts /  $\mu$ -strain
- PZT sensors have 200X higher charge sensitivity, and thus give less noise for a charge amplifier. They are universally employed in accelerometers.
- PVF<sub>2</sub> Sensors have reasonable voltage sensitivity. They are easy to apply and inexpensive.

## *Active Damping Workshop*

### **Strain Gages**

- Principle: A metal strip is attached to a surface. Strain causes a cross-sectional area change in the conductor, changing its resistivity. The gage is placed in a bridge with balanced nominal resistances such that zero strain gives zero differential voltage. Voltage changes for a constant current source produce an indication of resistance and hence strain.

- Sensitivity is defined by Gage Factor:

$$GF = \frac{(\Delta R/R)}{(\Delta L/L)}$$

- For most metal foil strain gages  $GF \sim 2 - 4$ .

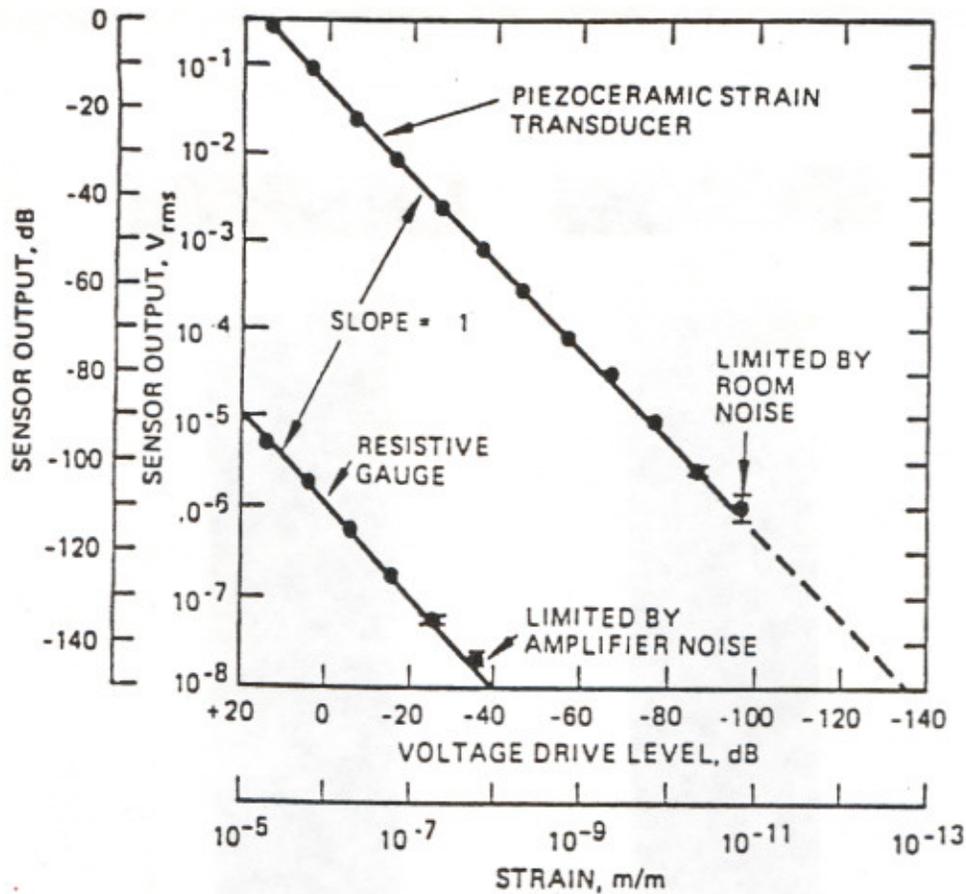
Thus sensitivity is  $\sim 2 \mu\text{-Volts} / \mu\text{-strain}$ .

A factor of 100,000 lower sensitivity than a PZT sensor.

- Shape memory metal gage factor is around 100X higher. However, GF is extremely temperature sensitive.

# Active Damping Workshop

## PZT Sensor vs. Strain Gage



- This experiment was published by Bob Forward of Hughes Research Labs in 1980.
- Forward used PZTs in an attempt to measure gravitational waves.
- The limit of measurable strain in a PZT is  $1e-13$  strains.
- Op amp noise is the limiting factor.

## Summary

- There are numerous applications for integral sensors and actuators in active structures and devices.
- To determine the systems behaviour must consider 2 couplings: material/structure and mechanical/electrical.