

Design of Piezoelectric Active Structures

Lecture 1:

Introduction to Active Materials and Structures

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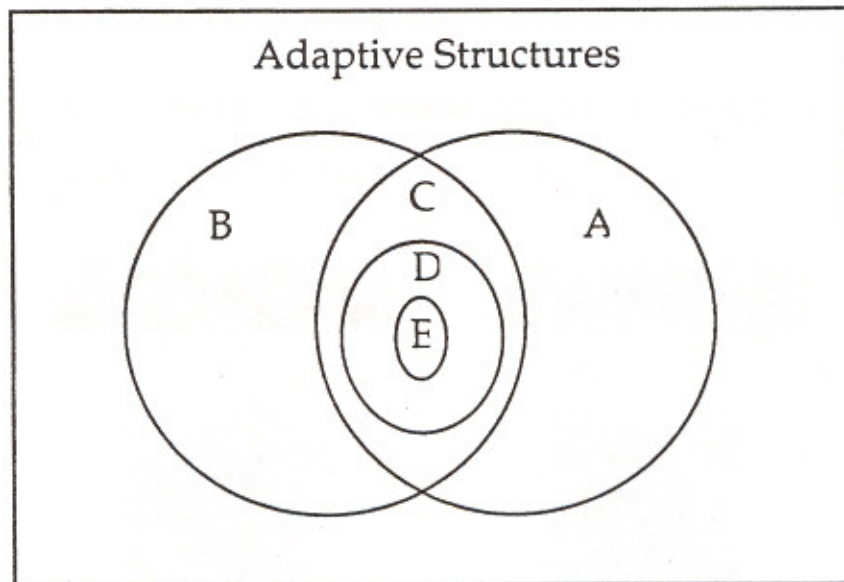
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Adaptive Structures

- An Adaptive Structure is one whose characteristics can be beneficially changed in response to environmental stimuli.
- Characteristics :
 - shape, stiffness
 - vibration response
 - acoustic reflectivity
 - radar signature, etc.
- Stimuli :
 - external force disturbances
 - pressure fields,
 - thermal loading
 - applied voltages and control signals
- Controllable Response allows new functionality to meet mission requirements such as precision pointing, stealth, etc.
- The goal of the technology is to develop adaptation mechanisms, sensing mechanisms, and processing hardware and algorithms which can enhance the performance of an aerospace structure and vehicle.

Classifications



- A **Actuated Structures** possess actuation/adaptation mechanisms
- B **Sensory Structures** possess capability to sense environment
- C **Controlled Structures** couple actuation and sensing with processing
- D **Active Structures** have integrated actuators and sensors
- E **Intelligent Structures** have integrated/distributed processing.

Applications for Active Structures

- Vibration Suppression
 - Precision Pointing of Optical Systems
 - Precision Machining
- Active Noise Control
 - Structural Acoustics
 - Modification of Acoustic Reflection and Transmission
- Optics
 - Static Optical Positioning and Surface Correction
 - Adaptive Optics - Dynamic Wavefront Correction
- Flow-Structure Interactions
 - Static Aeroelastic Control
 - Gust Load Alleviation
 - Flutter Suppression
 - Boundary Layer Control
- Structural Health Monitoring
- Solid State Motors and Articulating Devices

Survey of Adaptation Mechanisms

- Adaptation properties are usually associated with a given active material which is incorporated into the structure.
- Controllable Size (Induced Strain Actuation)

Electrically:	Piezoelectric Ceramics Piezoelectric Polymers Electrostrictive Materials Shape Memory Ceramics
Thermally :	Shape Memory Alloys Thermoelastic Materials
Magnetically:	Magnetostrictive
Optically:	Photoelastic Materials
Chemically	
- Controllable Stiffness

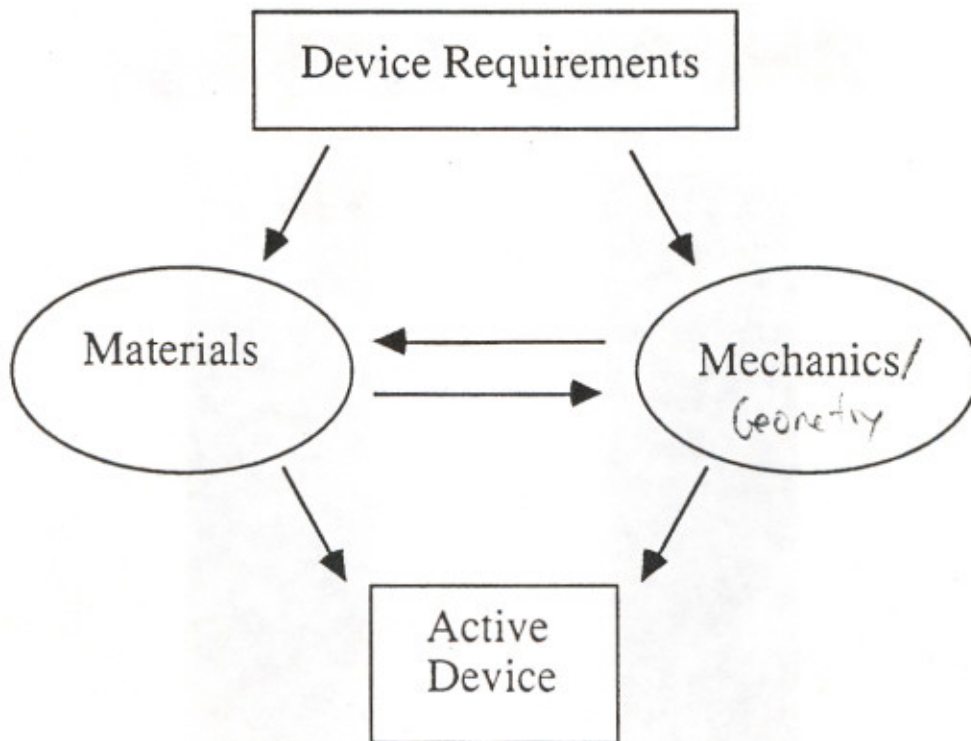
Thermally:	Shape Memory Alloys Viscoelastics
Electrically:	Electrostrictives
Magnetically:	Magnetostrictives
- Controllable Viscosity

Thermally:	Water
Electrically	Electrorheological Fluids
Magnetically	Magnetorheological Fluids
- Electrical Conductivity, Resistivity, Transmission

Electrically:	Transistors
Mechanically:	Strain Gauges
Optically:	Photochromatic Glasses
- Some materials operate as transducers and can therefore be used as sensors. e.g.. Piezoelectrics
- Solid State Actuators - Sensors

Design of Active Structures/Devices

- Design of active devices requires coordinated selection of mechanical, electrical parameters as well as selection of material and operating environment. - based on requirements.



- The 2 fundamental design problems:
 - 1) The active material is an integral part of the structure, and therefore the actuation or sensing is entirely dependent on host/actuation elastic interaction. - elastic actuators and sensors
 - 2) The active element usually couples electric, magnetic and mechanical fields in the material.

- material physics

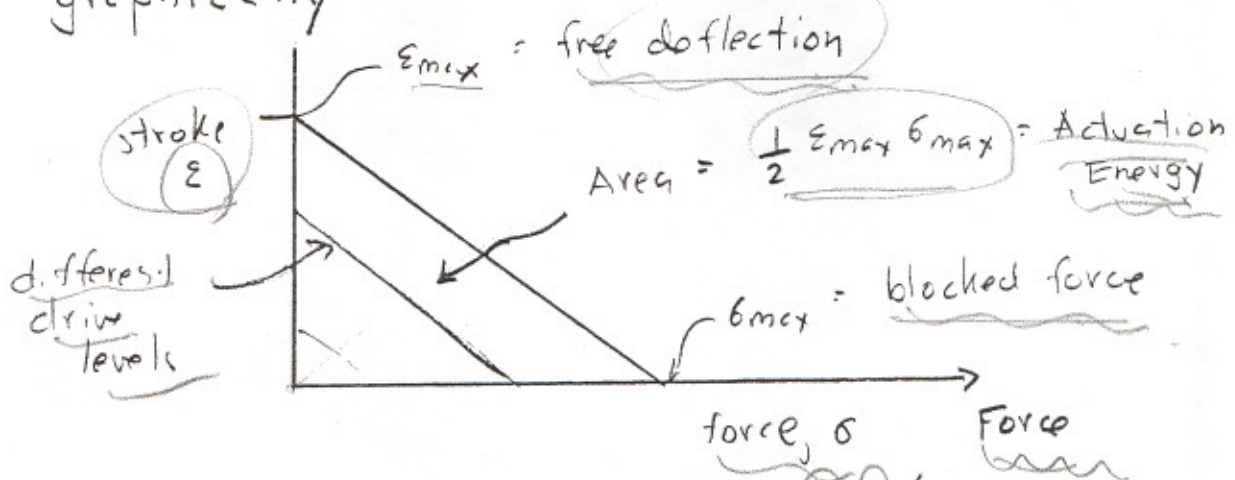
Active Material Selection Criteria

- Broad range of materials: Piezoelectrics, electrostrictors available as ceramics, piezoelectrics also in polymer form, magnetostrictors and shape memory alloys available as metal alloys.
- Within each type there are many variants. eg. PZT-4 (Navy Type I), PZT-5A (Navy Type II), PZT-5H (Type VI) etc.
- Large variation in:
 - modulus, anisotropy,
 - mechanical strength, fracture toughness
 - dielectric strength,
 - maximum actuation strain,
 - maximum inducible stress,
 - sensitivity to input fields,
 - temperature ranges for operation,
 - property stability over time
 - frequency response, hysteresis
 - linearity,
 - availability, cost.
- Need coherent modeling and design capability to establish relative material performance for a given application.

Actuation Figures of Merit

- Stroke Actuation (induced strain)
Max stroke (free strain) at highest field allowable
Strain/field if field is limited
- Force Actuation (induced stress)
Max Force (clamped stress) at highest field allowable
Stress/field if field is limited
- Same types with applied charge rather than electric field.
- More complicated in distributed problems since it is no longer uniaxial.

graphically



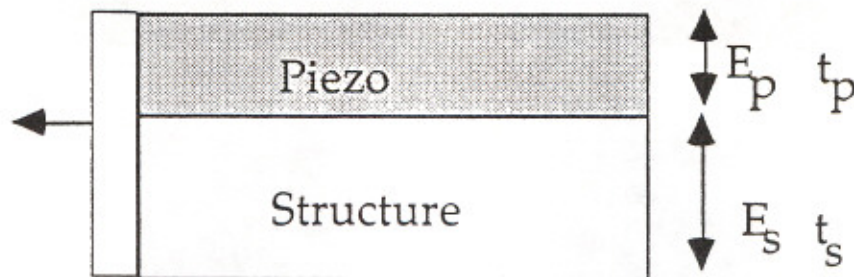
• Actuation Energy Density = $\frac{1}{2} \epsilon \sigma / \rho$

• Simple 1-D model



Elastic Actuation - I

- Must really consider the coupled active material/substructure system
- Simple Bar Example:



- Possible figure of merit for coupled system: maximum strain induced in a bar with surface bonded actuation strain material.

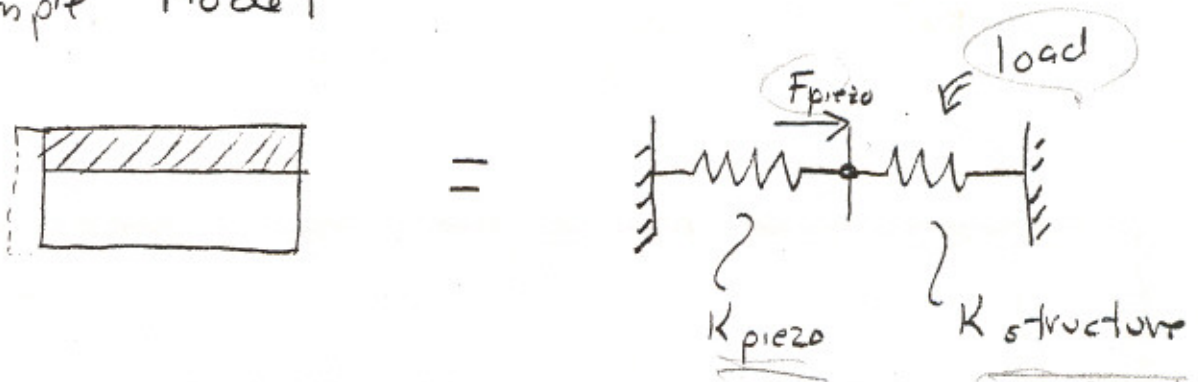
$$\varepsilon_{tot} = \varepsilon_{p_{max}} \left(\frac{1}{1 + \Psi} \right)$$

$$\Psi = \frac{E_s t_s}{E_p t_p} = \frac{K_s}{K_p}$$

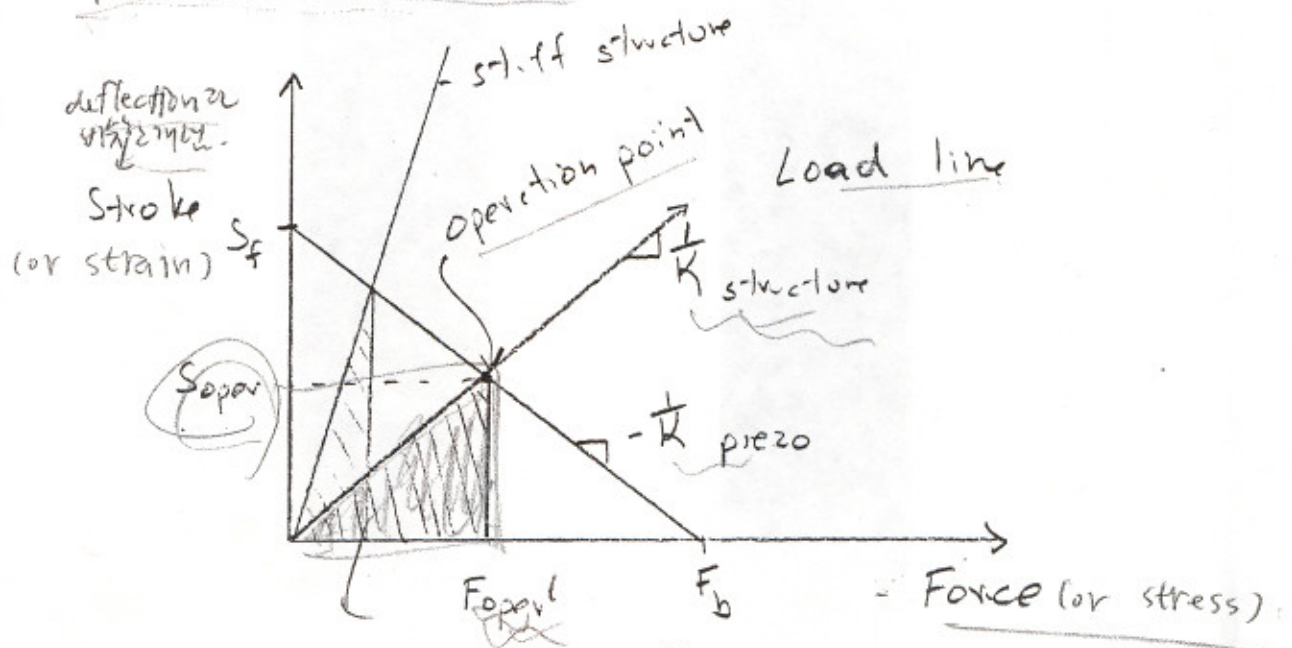
- Actuation strain and material stress depend on *relative* values of active material and structure.

Elastic Actuation - II

• Simple Model



• Graphical Representation

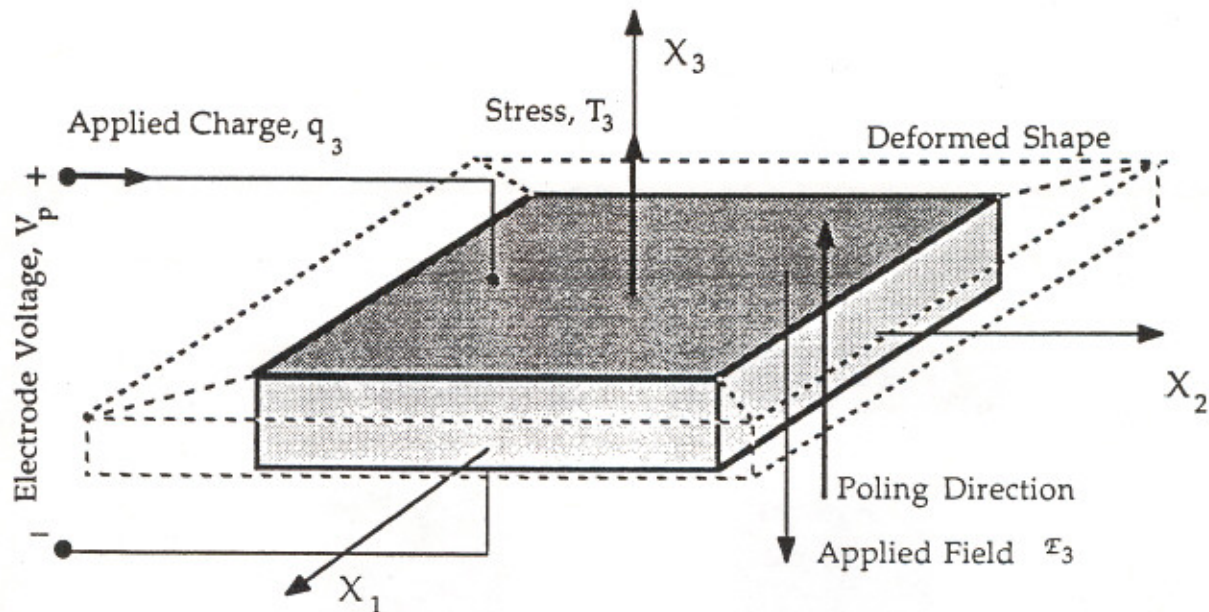


area: energy transferred to the system.
linear

• Max work delivered to load is $\frac{1}{4} \frac{F_0 S_F}{2}$

when $K_{structure} = K_{piezo}$
(impedance matching) ✓

What is Piezoelectricity?



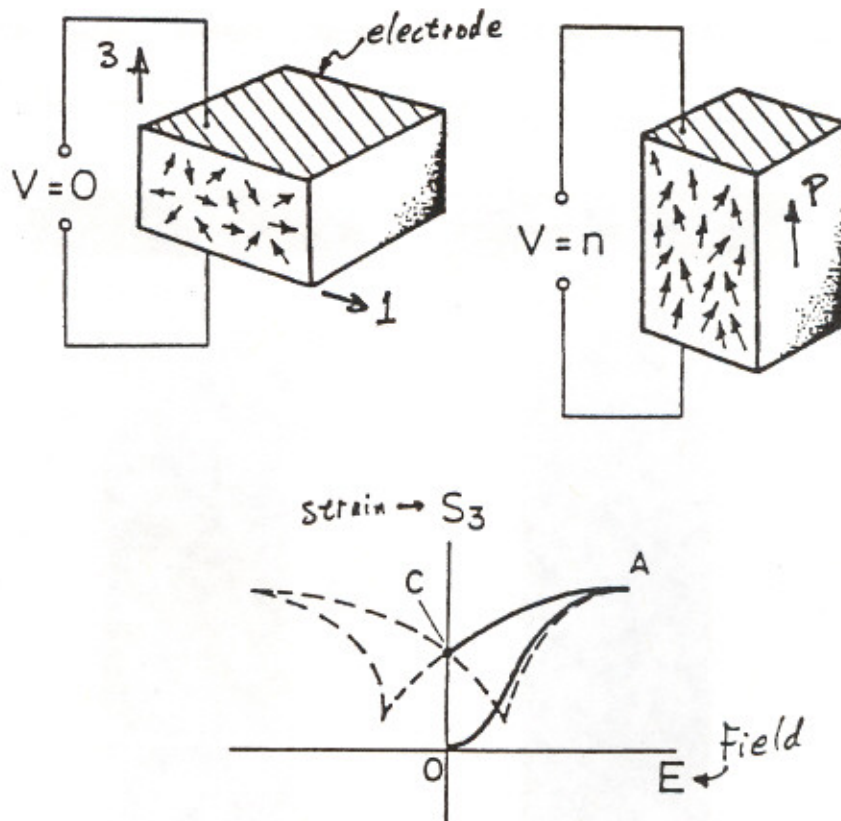
- Piezoelectric causes deformation when voltage is applied (or vice-versa).
- Piezoelectric actuation strain enters equations in a manner analogous to thermal strain but is field dependent.
- High bandwidth, well into structural acoustic range.

Piezoelectric Materials in Structures

- Piezoelectric materials have been modelled in surface bonded and embedded configurations in beams, plates, and tubes.
- Intelligent structures have been manufactured with piezoelectric materials embedded in glass/epoxy and graphite /epoxy laminates.
- Piezoelectric materials have been used in passive damping applications as a replacement for viscoelastic materials.
- Piezoelectric materials have been used as actuators in active structural control applications such as structural vibration, aeroelastic, and acoustic control.

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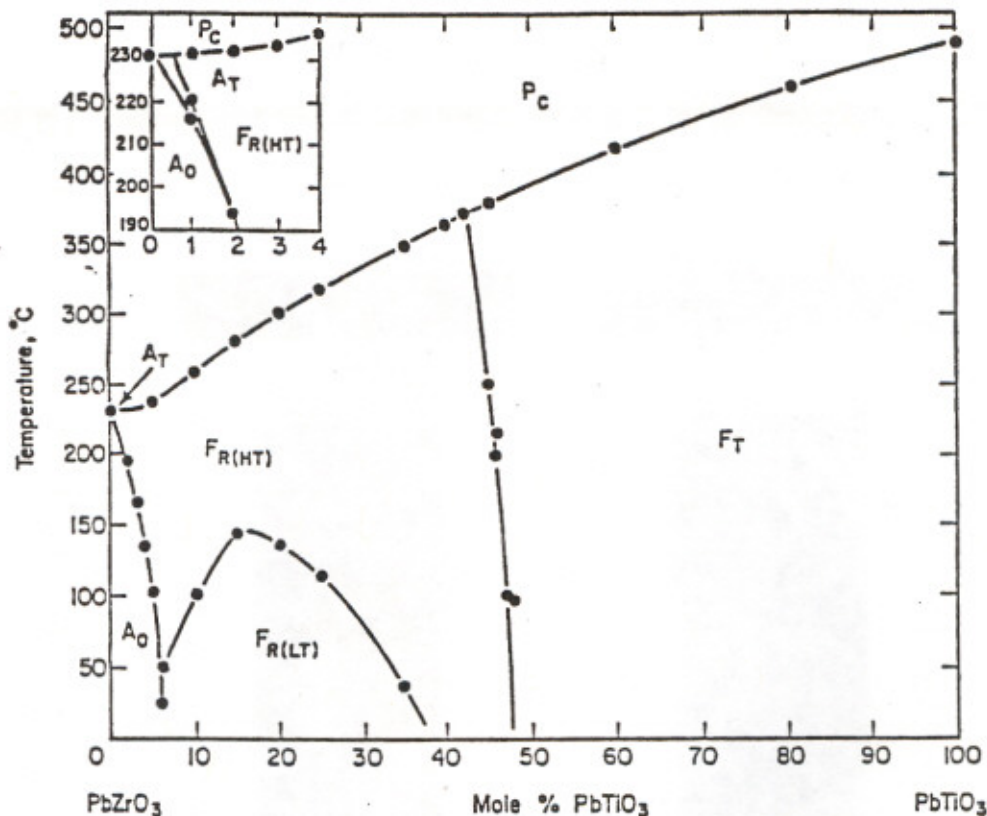
Piezoelectric Action



- Poling, or application of a large coercive field on the order of 50 Volts/mil, aligns crystalline subdomains in the ceramic.
- Poling causes the ceramic to grow in the field direction and to shrink laterally, roughly according to Poisson's ratio.
- Subsequent application of field in the poling direction also causes the ceramic to grow in that direction.
- Application of reverse field causes the ceramic to shrink until a negative coercive field level is reached. Poling action then switches and the ceramic grows again. Hence the "butterfly" curve.

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PZT Phase Boundaries



- PZT is a solid solution of lead zirconate (PbZrO₃) and lead titanate (PbTiO₃). The ratio of these two molecules and addition of other trace compounds determines the phase transition boundaries, and hence the properties.
- PZT and Barium Titanate are Perovskite ceramics. PZT has somewhat better piezoelectric and dielectric properties.
- These Perovskites have very high dielectric constants (capacitance) relative to free space of $D' \sim 1700$. This is due to offsets in the charged ions in the crystal lattice. The previous highest known material had $D' \sim 30$.
- The electric offsets in the crystal lattice also cause very high mechanical strains when subjected to a field, and conversely.

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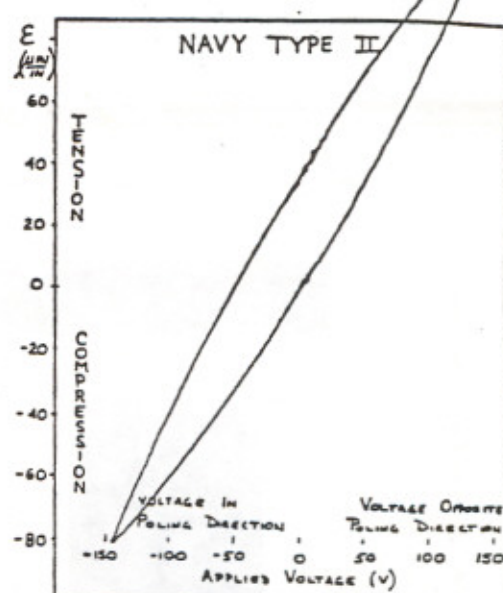
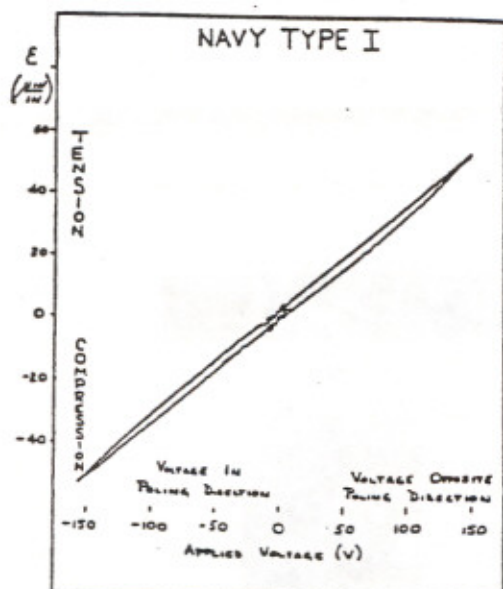
PZT Actuators

- Principle: Bond or embed piezoelectric wafer on surface.
Apply voltage V across electrodes generating field $\Phi = V / t$.
Actuate in lateral mode (note $d_{33} \sim 2.5 \times d_{31}$)
Max Free Strain: $\epsilon_{\max} = \Phi_{\max} d_{31} \sim 120 \mu\text{-strains}$ (Type II)
Max Blocked Stress: $\sigma_{\max} = E \Phi_{\max} d_{31} \sim 1,100 \text{ psi}$
Max Line Force for 7.5 mil wafer: $N_{\max} = \sigma_{\max} t \sim 8 \text{ lb/inch}$
(requires 150 Volts DC)
- Attaching PZT to structure drops strain levels by stiffness ratio: $E_p t_p / (E_p t_p + E_s t_s)$
- To Push on a Stiff Structure You Need a Hard Ceramic!

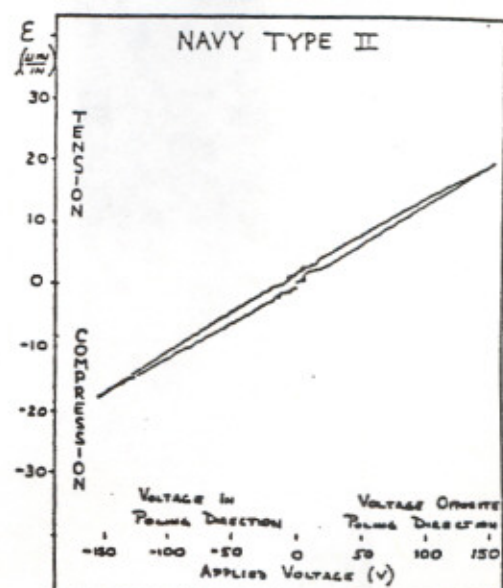
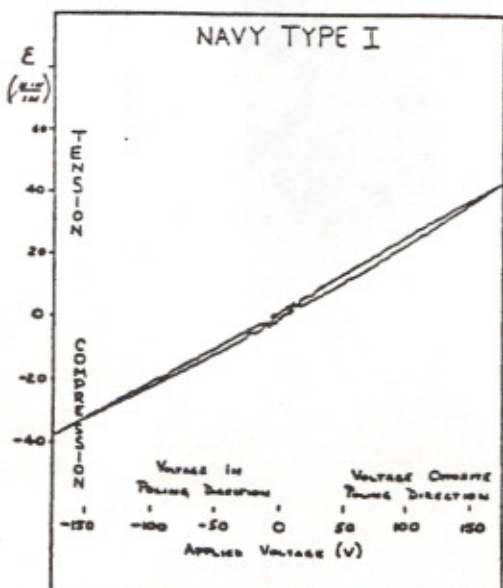
Quantity	Description	Units	Material			
			Type I	Type II	PZWT	PVF ₂
d_{31}	Lateral Strain Coeff.	m/V or C/N	1.23e-10	1.66e-10	2.8e-10	0.23e-10
ϵ_{AC}	Max AC Field	V/m	1.6e6	.71e6	1.6e6	30.e6
ϵ_R	Max Reverse Field	V/m	1.6e6	.71e6	.39e6	7.9e6
$d_{31} V_R$	Max Reverse Strain	m/m	2.0e-4	1.2e-4	1.1e-4	1.8e-4
E	Young's Modulus	N/m ² (Pa)	9.9e10	6.9e10	4.8e10	2e9
Ed_{31}	Stress per Field	(N/m ²)/(V/m)	12.2	11.5	13.4	.046
$Ed_{31}\epsilon_R$	Max Reverse Stress	N/m ²	19.5e6	8.2e6	5.2e6	0.36e6
D	Permittivity	Farad/m	1.3e-8	1.5e-8	2.9e-8	1.06e-10
Ed_{31}/D	Stress per Charge	(N/m ²)/(C/m ²)	9.4e8	7.7e8	4.6e8	4.3e8

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PZT Actuation Comparison



Free PZTs



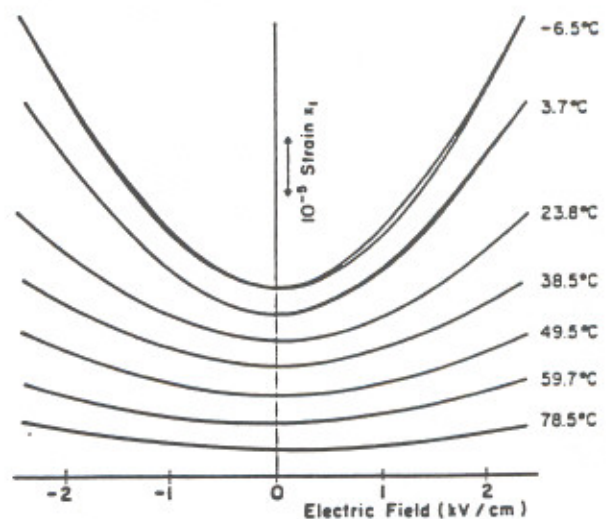
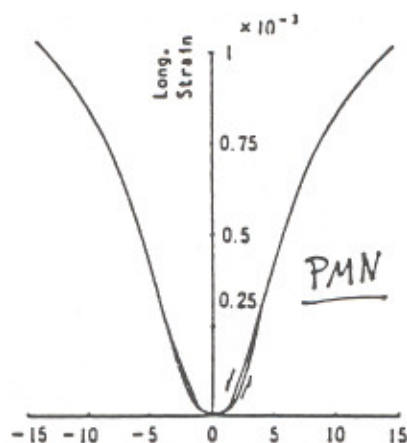
PZTs Embedded in Graphite/Epoxy

Type I has lower intrinsic hysteresis & better stiffness match to graphite.
Type II has higher free strain. Embedding decreases hysteresis.

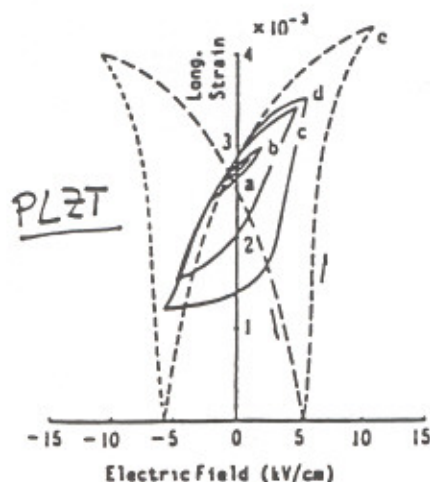
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Electrostrictive Ceramics

- Lead Magnesium Niobate (PMN) is a Perovskite crystal.
- Application of field (+/-) causes the crystal to grow longitudinally and shrink laterally.
- Strain Effect is Quadratic in Voltage and Decreases with Temperature.
- Vibration damping requires a bias voltage.
- Low hysteresis makes PMN suitable for open loop optical shape control.

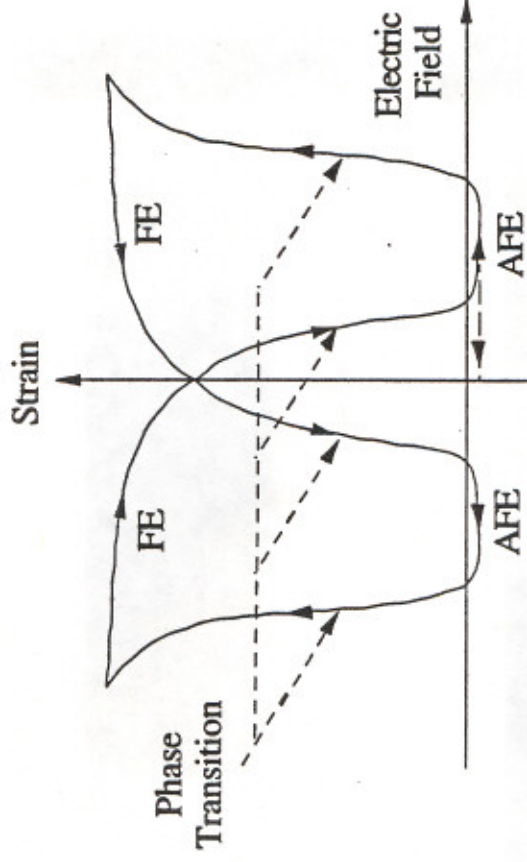


PMN vs. Temperature



Shape Memory Ceramics

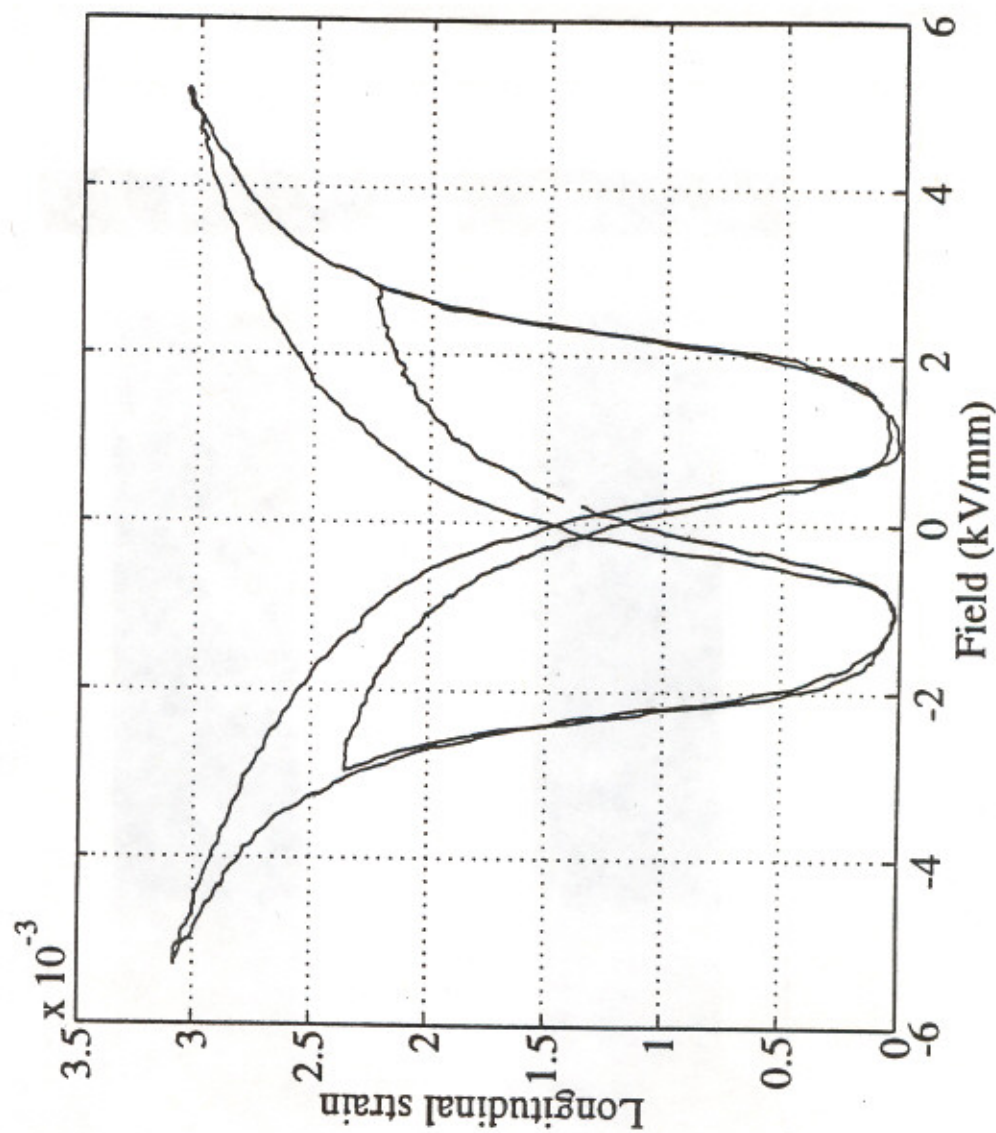
- Concept: Electric field induces phase transition between Ferroelectric (FE) and anti-ferroelectric (AFE) phases:



- Large isotropic strains (0.5%) accompany transition between phases
Material exhibits shape memory and requires electric field or stress to return to original state
- High switching rates permit high bandwidth applications: Adaptive Mirrors and Optics (JPL), Antennas

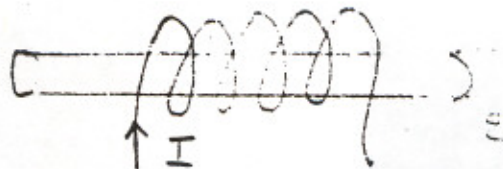
High Field Experimental Data for PLZST (A3)

$\text{Pb}_{0.97}\text{La}_{0.02}(\text{Zr}_{0.66}\text{Ti}_{0.105}\text{Sn}_{0.235})\text{O}_3$



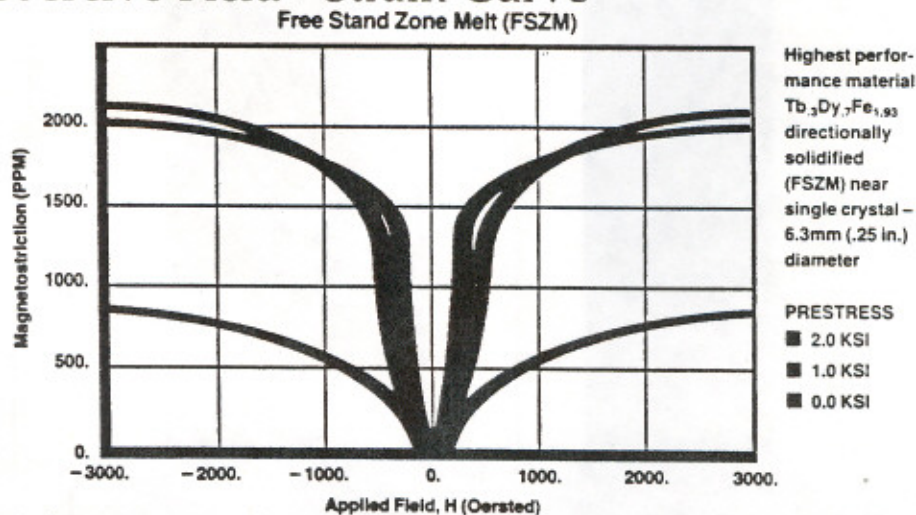
Magnetostrictive Materials

- Discovered by James Joule, 1840 in Nickel
- Terfenol-D is an alloy of Iron, Terbium, and Dysprosium developed in late 70's by the Navel Ordinance Lab.
- Typical Configuration:



$$H = nI = \text{coercive field (A / m)}$$

- Coercive Field - Strain Curve

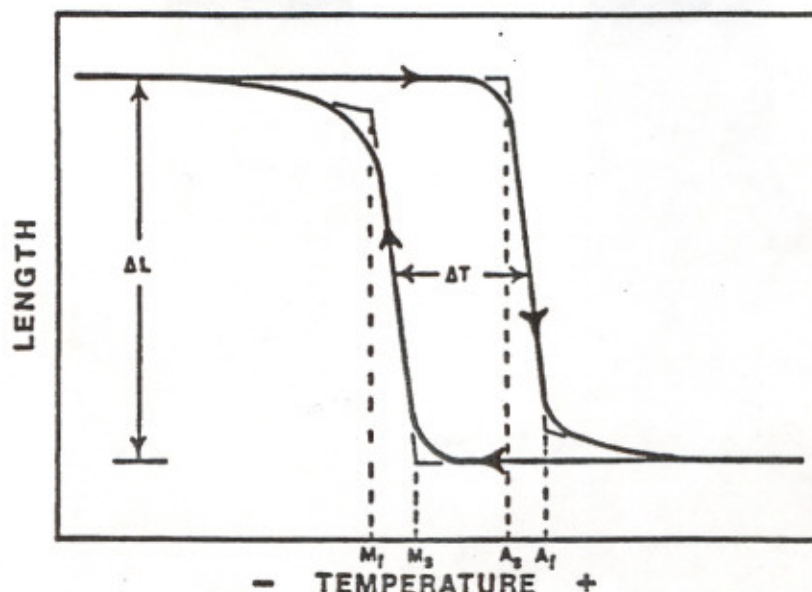


Material is typically biased magnetically $h = 500-1000$ Oersteads ($=1000/4\pi$ A/m) to produce linear properties

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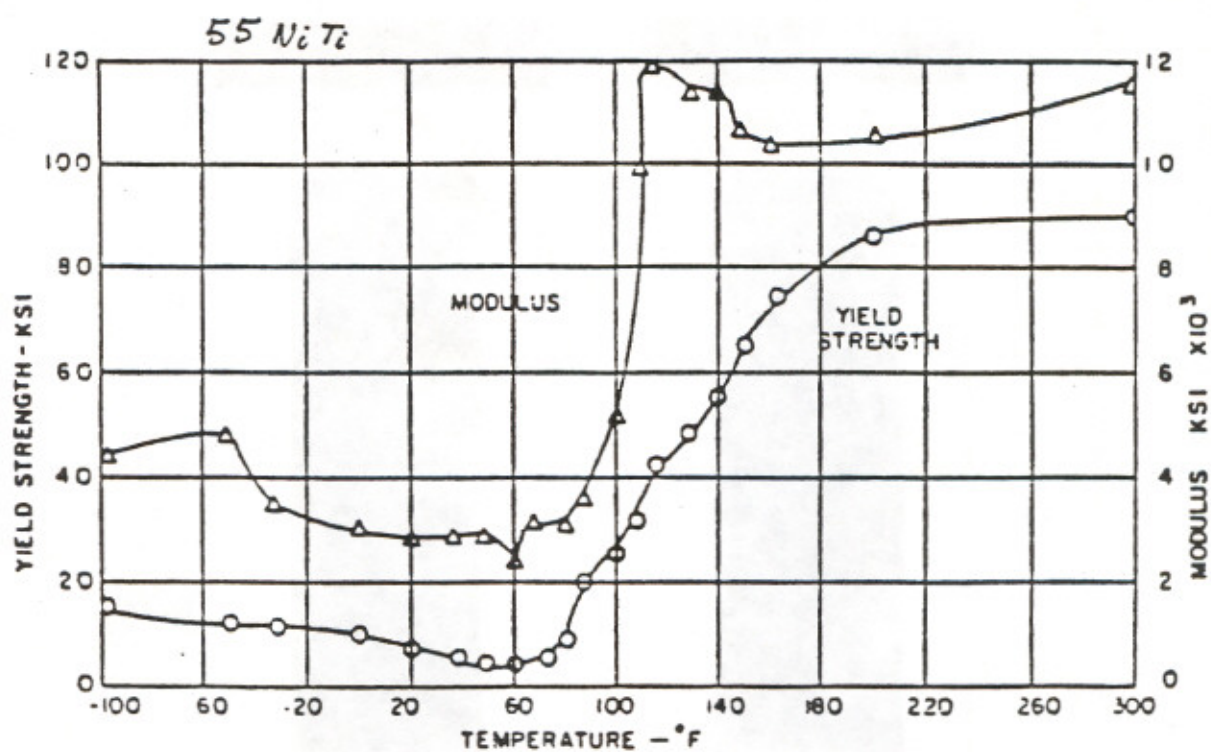
Shape Memory Metals

- Nitinol is the most widely used SMM. It is a Nickel-Titanium alloy developed at the Naval Ordnance Laboratory.
- The high temperature phase is Austenitic.
- The low temperature phase is Martensitic.
- Transition Temperature (TTR) can be adjusted by varying alloy. TTR is stress dependent.
- Nitinol working stress = 25,000 psi
working strain = 3.5%.
- To pull one must heat SMM wire with electric current
To push one must cool by convection, conduction and/or radiation.
- Vibration damping frequency is limited by maximum cooling rate and hysteresis. Control demonstrated to 3 Hz.
- Difficult to control temperature accurately.
- CTE mismatch makes attachment to structure difficult.



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Nitinol Properties Vs. Temperature



Comparison of Commercially Available and Potential Actuation Materials

	PZT-5H	PVDF	PMN	TERF-DZ	NITINOL	PLZST
Actuation Mechanism	piezo-ceramic	piezo film	electro-strictor	magneto-strictor	shape memory alloy	shape memory ceramic
ϵ_{\max} (strain)	0.13%	0.07%	0.1%	0.2%	2%-8%	0.3%-0.9%
E (Msi)	16 (D)	0.3	17	7	4 (m), 13 (a)	12 (FE)
σ_{\max} (kpsi)	20.8	0.21	17	14	26 - 104	36-108
Density (kg/m ³)	7500	1780	7800	9250	7100	7500
Actuation Energy Density (J/kg)	13.5	0.285	7.51	10.4	252-4032	49.6-446
Hysteresis	10%	>10%	<1%	2%	High	High
Temp Range	-20C to 200C	Low	0C to 40C	High	-	0C to 40C
Bandwidth	100kHz	100kHz	100kHz	<10kHz	<5Hz	<100Hz

(m) = martensite (a) = austenite (FE) ferroelectric (D) = open circuit
 Actuation Energy Density = $1/2 \epsilon_{\max} \sigma_{\max} / \rho$

Sensing Figures of Merit

- Consider sensing of mechanical fields (stress or strain). Sensing duals are:

Electrical:	Voltage	Charge
Magnetic:	Current	Voltage
- Volt per stress or strain
- Charge per stress or strain
- In the sensing case you usually look at the normalized figures of merit since you rarely exceed material capability - exception is high stress of piezoceramic.

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PZT Sensor Example

Material Properties for Navy Type II PZT & PVF₂ Film

Quantity	Description	Units	Material	
			Ceramic	Film
d_{31}	Lateral Strain Coefficient	m/V or Coul/N	1.8e-10	23e-12
d_{33}	Axial Strain Coefficient	"	3.6e-10	33e-12
d_{15}	Shear Strain Coefficient	"	5.4e-10	n.a.
E	Young's Modulus	N/m ² or Pascal	6.30e10	2e9
G	Shear Modulus	"	2.34e10	n.a.
ν	Poisson's Ratio	-	0.35	n.a.
Ed_{31}	Actuation & Sensing	N/m/V or Coul/m ²	11.34	.046
D_0	Free Space Permittivity	Farad/m or N/V ²	8.85e-12	=
D'	Relative Permittivity	-	1700	12
D	Absolute Permittivity	"	1.5e-8	1.06e-10
ρ	Resistivity	Ω -m or V ² -sec/N	1e10	1e13
α	CTE	μ -strain/ $^{\circ}$ K	5	\sim 30-40
p	Pyroelectric Coefficient	Coul/(m ² $^{\circ}$ K)	4e-4	2.5e-5
k	Boltzmann's Constant	Joules/ $^{\circ}$ K	1.38e-23	=

- Lateral Mode PZT Sensor: 1" x 1" x .0075"
 $Q = 7.1e-9$ Coulomb / μ -strain
 $C = .05$ μ -Farads : $V = Q/C = .14$ Volts / μ -strain
- Lateral Mode PVF₂ Sensor: 1" x 1" x .002"
 $Q = 2.9e-11$ Coulomb / μ -strain
 $C = .0013$ μ -Farads : $V = Q/C = .022$ Volts / μ -strain
- PZT sensors have 200X higher charge sensitivity, and thus give less noise for a charge amplifier. They are universally employed in accelerometers.
- PVF₂ Sensors have reasonable voltage sensitivity. They are easy to apply and inexpensive.

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Strain Gages

- Principle: A metal strip is attached to a surface. Strain causes a cross-sectional area change in the conductor, changing its resistivity. The gage is placed in a bridge with balanced nominal resistances such that zero strain gives zero differential voltage. Voltage changes for a constant current source produce an indication of resistance and hence strain.

- Sensitivity is defined by Gage Factor:

$$GF = \frac{(\Delta R/R)}{(\Delta L/L)}$$

- For most metal foil strain gages $GF \sim 2 - 4$.

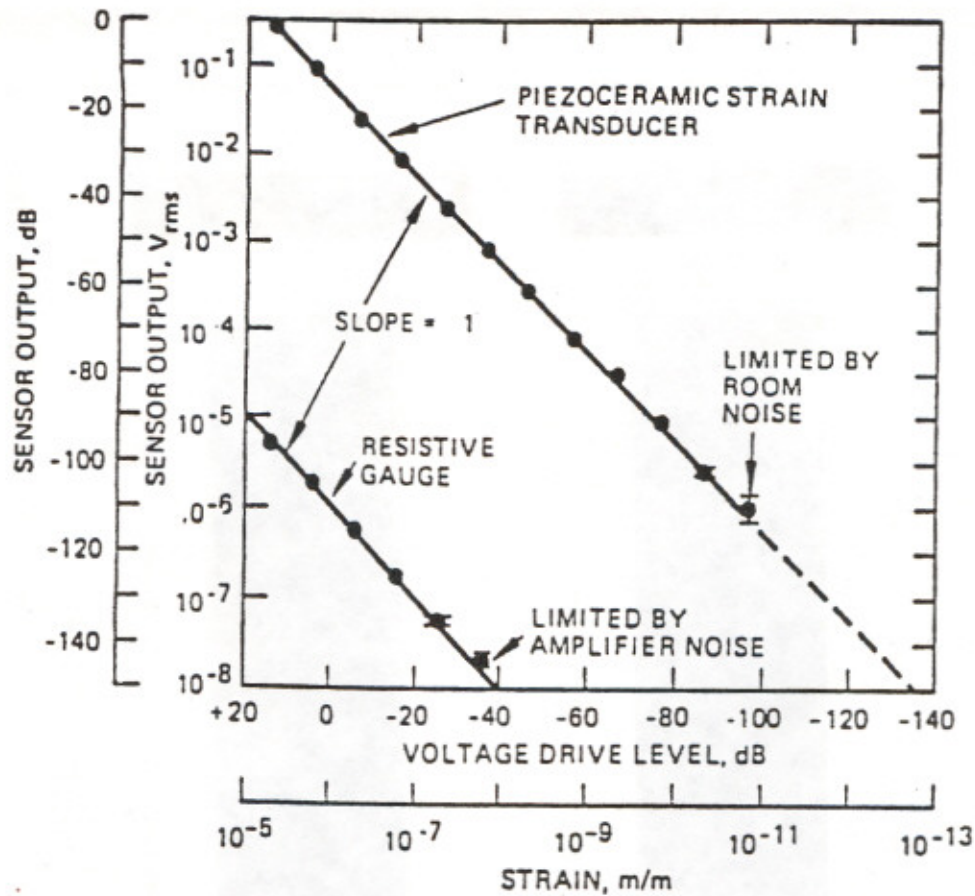
Thus sensitivity is $\sim 2 \mu\text{-Volts} / \mu\text{-strain}$.

A factor of 100,000 lower sensitivity than a PZT sensor.

- Shape memory metal gage factor is around 100X higher. However, GF is extremely temperature sensitive.

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PZT Sensor vs. Strain Gage



- This experiment was published by Bob Forward of Hughes Research Labs in 1980.
- Forward used PZTs in an attempt to measure gravitational waves.
- The limit of measurable strain in a PZT is $1e-13$ strains.
- Op amp noise is the limiting factor.

Summary

- There are numerous applications for integral sensors and actuators in active structures and devices.
- To determine the systems behaviour must consider 2 couplings: material/structure and mechanical/electrical.