5. Joint blocks

- Joint blocks: rock blocks determined entirely by joint planes without free surfaces
- Generally do not draw any significant concern in rock mechanics literature because they are hidden within rock mass.
- Affect the size and shape of blasted rock materials (Fig.5.2, 5.3).
- Affected by orientation, spacing and extent of each joint set.
- Difference with free plane-bearing blocks: more chances to have parallel joints as boundary planes.
- Intuitively derived principles in block occurrence
- Blocks made by less joints are more likely to occur (Fig. 5.5). Ex) 1100 vs. 1120 (2D)
- Blocks with parallel joints are more likely than those with non-parallel joins.

$$
\text { Ex) } 3322>3323>1120(2 D)
$$

## 1) Joint blocks in 2D

- Joint blocks with no repeated joints (Fig.5.7, 5.8)
- No. of all JPs: $2^{\text {n }}$
- No. of non-empty JPs: $2 \mathrm{n}(\mathrm{n} \geq 1)$
- No. of empty JPs (finite JB): $2^{n}-2 n$
- Joint blocks with one repeated joint set (Fig.5.9)
- No. of all JPs: $2^{n-1}$
- No. of non-empty JPs: 2
- No. of empty JPs (finite JB): $2^{\mathrm{n}-1}-2$
when the repeated joint is selected randomly: $\mathrm{n}\left(2^{\mathrm{n}-1}-2\right)$


## 1) Joint blocks in 2D

- Joint blocks with two or more repeated joint sets (Fig.5.11)
- No. of all JPs: $2^{\mathrm{n}-\mathrm{m}}$
- No. of non-empty JPs: 0
- No. of empty JPs (finite JB): $2^{\mathrm{n}-\mathrm{m}}$
when the repeated joint is selected randomly: ${ }_{\mathrm{n}} \mathrm{C}_{\mathrm{m}} 2^{\mathrm{n}-\mathrm{m}}=\mathrm{n}!/[(\mathrm{n}-\mathrm{m})!\mathrm{m}!] 2^{\mathrm{n}-\mathrm{m}}$


## 2) Joint blocks in 3D

- Joint blocks with no repeated joints (Fig.5.16)
$\mathrm{n} \quad$ No. of non-empty JPs

$$
\begin{array}{lc}
1 & 2 \\
\geq 2 & 2(\mathrm{n}-1) \text { JPs are added } \\
\mathrm{n} & 2+\sum_{i=2}^{n} 2(i-1) \\
& =2-2(n-1)+(2+n)(n-1) \\
& =n^{2}-n+2
\end{array}
$$

- Joint blocks with one repeated joint set (Fig.5.17)
- No. of all JPs: $2^{\mathrm{n}-1}$
- No. of non-empty JPs: 2(n-1)
- No. of empty JPs (finite JB): $2^{\mathrm{n}-1}-2(\mathrm{n}-1)$
when the repeated joint is selected randomly: $n\left(2^{n-1}-2(n-1)\right)$


## 2) Joint blocks in 3D

- Joint blocks with two repeated joint sets (Fig.5.18)
- No. of all JPs: $2^{\mathrm{n}-2}$
- No. of non-empty JPs: 2
- No. of empty JPs (finite JB): $2^{\mathrm{n}-2}-2$
when the repeated joint is selected randomly: ${ }_{\mathrm{n}} \mathrm{C}_{2}\left(2^{\mathrm{n}-2}-2\right)=\mathrm{n}(\mathrm{n}-1)\left(2^{\mathrm{n}-2}-2\right) / 2$
- Joint blocks with three or more repeated joint sets (Fig.5.19, 20)
- No. of all JPs: $2^{\mathrm{n}-\mathrm{m}}$
- No. of non-empty JPs: 0
- No. of empty JPs (finite JB): $2^{\text {n-m }}$
when the repeated joint is selected randomly: $\mathrm{C}_{\mathrm{m}} 2^{\mathrm{n}-\mathrm{m}}$


## 3) Stereographic projection solution for joint blocks

- Finite joint blocks with no repeated joint sets

TABLE 5.3

| Set | Dip, $\alpha$ <br> $(\mathrm{deg})$ | Dip Direction, $\beta$ <br> (deg) |
| :---: | :---: | :---: |
| 1 | 75 | 80 |
| 2 | 65 | 330 |
| 3 | 40 | 30 |
| 4 | 10 | 270 |



0111

## 3) Stereographic projection solution for joint blocks

- Finite joint blocks with one repeated joint set

(a)


## 3) Stereographic projection solution for joint blocks

- Finite joint blocks with two repeated joint sets



## 3) Stereographic projection solution for joint blocks

- Finite joint blocks with three or more repeated joint sets

TABLE 5.6 Empty Joint Pyramids with Three Repeated Joint Sets for the Joint System of Table 5.3


## 4) Computation of emptiness of joint pyramids using vectors

| TABLE 5.7 |  |  |  |
| :---: | :---: | :---: | :---: |
| Joint Set | $X$ | $\boldsymbol{Y}$ | $\boldsymbol{Z}$ |
| 1 | 0.9512 | 0.1677 | 0.2588 |
| 2 | -0.4531 | 0.7848 | 0.4226 |
| 3 | 0.3213 | 0.5566 | 0.7660 |
| 4 | -0.1736 | 0 | 0.9848 |

$$
\begin{aligned}
& 0.9512 X+0.1677 Y+0.2588 Z \geq 0 \\
& 0.4531 X-0.7848 Y-0.4226 Z \geq 0 \\
& 0.3213 X+0.5566 Y+0.7660 Z \geq 0 \\
& -0.1736 X+\quad 0.9848 Z \geq 0
\end{aligned}
$$

- With no repeated joint sets: 0100 (p.148)

1) Calculate normal vectors of joints.
2) Define JP equations according to JP code.
3) Calculate direction vectors of joint intersections:

$$
\pm \vec{I}_{12}, \pm \vec{I}_{13}, \pm \vec{I}_{14}, \pm \vec{I}_{23}, \pm \vec{I}_{24}, \pm \vec{I}_{34}
$$

4) Check whether any intersection vector satisfies the JP equations.
5) If the JP equations are not satisfied for any intersection vectors the JP block is finite.

## 4) Computation of emptiness of joint pyramids using vectors

- With one repeated joint set: 1310
- Follow the same procedure as in the case of no repeated joints. c.f. JP of the repeated joint should be expressed by an equality.

$$
\begin{array}{ll}
-0.9512 X-0.1677 Y-0.2588 Z \geq 0 & \text { Intersection vectc } \\
-0.4531 X+0.7848 Y+0.4226 Z=0 & \vec{I}_{12}, \pm \vec{I}_{23}, \pm \vec{I}_{24} \\
-0.3213 X-0.5566 Y-0.7660 Z \geq 0 \\
-0.1736 X+0.9848 Z \geq 0 &
\end{array}
$$

- With two repeated joint sets: 3031
- Follow the same procedure as in the case of one repeated joint.

$$
\begin{aligned}
& 0.9512 X+0.1677 Y+0.2588 Z=0 \\
& -0.4531 X+0.7848 Y+0.4226 Z \geq 0 \quad \text { Intersection vectors to check: } \pm \vec{I}_{13} \\
& 0.3213 X+0.5566 Y+0.7660 Z=0 \\
& +0.1736 X \quad-\quad 0.9848 Z \geq 0
\end{aligned}
$$

## 5) Application of block theory: an example

- Joint spacing (true \& apparent spacing)
$h=d \sin \delta, \quad \cos \delta=\left|\hat{n}_{1} \cdot \hat{n}_{2}\right|$

- Constructing a trace map in any section plane

Joint trace: $\vec{I}_{12}=\hat{n}_{1} \times \hat{n}_{2}$
' 1 ' denotes joint and '2' denotes rock exposure.

- The ratio of finite to infinite blocks as a rock mass index


## 5) Application of block theory: an example

- Constructing a trace map in any section plane



## 5) Application of block theory: an example



This means that dip vector of rock exposure is located inside of the great circle of Jt 1.

## 5) Application of block theory: an example

- The ratio of finite to infinite blocks as a rock mass index

Complete polygons: 37
Finite joint blocks: 11
Infinite joint blocks: 26
Semi-continuous rock mass - relatively higher powder factor than the case of discontinuous rock mass is required.

## Home Work

- Make a computer code that shows block types (tapered, finite \& infinite) of rock blocks formed by combination of 4 joints and 1 free plane when the orientation (dip/dip direction) of each joint/free plane is given.

