Peak broadening

Size broadening, Strain broadening

Size/strain broadening

Cullity Chapter 5-1, 5-2, 5-4 Jenkins & Snyder chap 3.9.2; 3.9.3 (p89~p94) Hammond chap 9.3 Cullity Chapter 5-5, 5-6 Krawitz chap 11.6 (p343~p346) Cullity Chapter 14-1. 14-2, 14-3, 14-4, 14-6

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➢ Peak broadening ←

same sample run on two different instruments

- ✓ Small crystallite size
- ✓ Stacking faults, Microstrain, and other Defects in the crystal structure
- ✓ An inhomogeneous composition in a solid solution or alloy

> Different instrument configurations can change the peak width, too.

 \rightarrow Instrument contribution

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Size broadening

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- \triangleright @ θ_B; ABC = λ, DEF = 2λ → diffraction peak
- > ABC = 0.5λ , DEF = $1\lambda \rightarrow$ no diffraction peak
- \succ ABC = 1.1 λ , DEF = 2.2 λ

0.1un

Jenkins & Snyder page 89

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→ PD (path diff.) in 6th plane = $5.5\lambda \rightarrow 1' \& 6'$ out of phase \rightarrow no net diffraction

- > ABC = $1.001\lambda \rightarrow 1' \& 501'$ out of phase; ABC = $1.00001\lambda \rightarrow 1' \& 50001'$ out of phase →→ Sharp diffraction peak @ θ_B
- > When crystal is only 100nm in size, 5000' or 50000' are not present.
- Peak begins to show intensity at a lower θ and ends at a higher θ than $θ_B$ → particle size broadening.
- ➤ Crystallites smaller than 1um can cause broadening. → size can be determined using the peak width (← incomplete destructive interference).

100um

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Crystallite size broadening

size broadening; degree of being "out-of-phase" that can be tolerated

- > In case $\lambda = 1.5$ Å, d= 1.0 Å, $\theta = 49^{\circ}$, $t = \frac{0.9\lambda}{B \cos \theta_B}$
- > 1mm(millimeter) diameter crystal \rightarrow 10⁷ parallel lattice planes, ~10⁻⁷ radian*, ~10⁻⁵ degree \rightarrow too small to observe.
- > 500 Å diameter crystal → 500 parallel lattice planes, ~10⁻³ radian, ~0.2 degree
 → measurable

➤ Non-parallel incident beam, non-monochromatic incident beam → diffraction @ angles not exactly satisfying Bragg's law → line broadening

* B = (0.9 X 1.5 X 10⁻¹⁰)/(10⁻³ X cos 49°) ~ 2 X 10⁻⁷ rad CHAN PARK, MSE, SNU Spring-2022 Crystal Structure Analyses



tolerated vs. crystallite size





Waseda & Matsubara, X-ray diffraction Crystallography, Springer, 2011





Strain broadening

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Strain/Stress

- > Macrostrain/Macrostress \rightarrow shift in peak position
 - ✓ stress is uniformly compressive or tensile over large distances. ← lattice parameter measurement
- > Microstrain/Microstress \rightarrow peak broadening
 - ✓ Distribution of both tensile & compressive stress → distribution of d-values
 - ✓ Can come from dislocations, vacancies, defects, shear planes, thermal expansion/contraction, etc.
 - ← peak profile analysis



Cullity page 176 Jenkins & Snyder, page 91~93

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Broadening

- Darwin width
 - ✓ Incident photon is confined to certain volume.
 - ✓ Result of uncertainty principle ($\Delta p \Delta x = h$) --- Location of the photon in a xtal is restricted to a certain volume.
 - ✓ Δp must be finite. → Δλ must be finite. → finite width of diffraction peak
- Specimen contribution (S)
- > Spectral distribution (radiation source contribution) (W)
- > Instrumental contribution (G)

LaB₆ SRM

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- > (W * G) ; fixed for a particular instrument/target system → instrumental profile g(x)
- > Overall line profile h(x) = (W * G) * S + background = g(x) * S + BKG

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The effect of dislocation contrast on x-ray line broadening: A new approach to line profile analysis

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> explained strain broadening by dislocations.

 $\frac{B\cos\theta}{\lambda} = \frac{0.9}{d} + \Delta K^{D} \qquad y = a + X$ Classical $X = -2\frac{\Delta d}{d}\frac{\sin\theta}{\lambda}$ Modified $X = A(\rho^{*})^{1/2} + A'(Q^{*})^{1/2}$ CHAN PARK, MSE, SNU Spring-2022 Crystal Structure Analyses

Modified Williamson-Hall Plot

$$\frac{B\cos\theta}{\lambda} = \frac{0.9}{d} + A(\rho^*)^{1/2} + A'(Q^*)^{1/2}$$

- $\triangleright \rho^*$: (formal) dislocation density
- \succ O* : (formal) two-particle correlations in the dislocation ensemble
- $\succ A.A'$: parameter determined by dislocations
- > True values of dislocation density, correlation factor

$$\rho^* = \rho(\pi g^2 b^2 \overline{C})/2 \qquad Q^* = Q(\pi g^2 b^2 \overline{C})^2/4$$

- C :average contrast factor of dislocation
- \checkmark b :Burgers vector of dislocation
- ✓ Particular reflection

$$g = \frac{2\sin\theta}{\lambda}$$

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Mosaic spread

Mosaicity is created by slight misorientations of different crystals as they nucleate and grow on the substrate. When the crystals join, they form boundaries.



Mosaic Spread - reciprocal space

- Mosaic spread can be quantified by measuring the broadening of the lattice point in reciprocal space.
- The amount of broadening of the reciprocal lattice point that is perpendicular to the reflecting plane normal can be attributed to mosaic spread.

Mosaic st

The peak broadening parallel to the interface can be attributed to lateral correlation length.

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Ideally imperfect crystal

- Diffracted intensity; perfect xtal << ideally imperfect xtal</p>
- > Decrease in intensity as the crystal becomes more perfect (large mosaic blocks).
- ➤ Ideally imperfect crystal consists of very small mosaic blocks, uniformly disoriented. → no extinction
- Kinematical theory vs. dynamical theory
- > Powder specimens should be ground as fine as possible.
- ➢ Grinding → reduce crystal size, increase # of diffraction cones, decrease mosaic block size, disorient mosaic blocks, strain the crystals non-uniformly.



Primary Extinction

Does not kill the reflection but lower intensity.

How to avoid? – give some stress (increase mosaicity by e.g. LN2 quenching, heat & quenching, etc.).

Lateral correlation

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