## Ship Stability

## Ch. 10 Hydrostatic Values and Curves

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## Ch. 10 Hydrostatic Values and Curves

1. Hydrostatic Values
2. Trim and Stability Calculation of a $3,700 \mathrm{TEU}$

Container Ship Including Hydrostatic Values
3. More Examples

## Introduction

In general, the document which contains the following list is submitted to ship owner and classification society, and get approval from them 9 months before steel cutting.

- Principle particulars
- General arrangement
- Midship section plan
- Lines plan
- Hydrostatic table
- Bonjean table
- Tank capacity table
- Light weight summary
- Allowable Minimum GM Curve
- Trim \& stability calculation (Intact stability)
- Damage stability calculation
- Freeboard Calculation
- Visibility Check
- Equipment number calculation
$\qquad$



## Hydrostatic Values

$\nabla$ Draft $_{\text {MId }}$, Draft $_{\text {scant }}$ : Draft from base line, moulded / scantling (m)
$\boxtimes$ Volume $_{\text {Mld }}(\nabla)$, Volume ${ }_{\text {Ext }}$ : Displacement volume, moulded / extreme ( $\mathrm{m}^{3}$ )
$\boxtimes$ Displacement $_{\text {Mld }}(\Delta)$, Displacement $_{\text {Ext }}$ : Displacement, moulded / extreme (ton)
■ LCB: Longitudinal center of buoyancy from midship (sign: - Aft / + Forward)
LCF: Longitudinal center of floatation from midship (Sign: - Aft / + Forward)
$\square$ VCB: Vertical center of buoyancy above base line (m)
$\square$ TCB: Transverse center of buoyancy from center line (m)
$\nabla \mathbf{K M}_{\mathrm{T}}$ : Transverse metacenter height above base line (m)
$\mathbf{K M}_{\mathrm{L}}$ : Longitudinal metacenter height above base line (m)
MTC: Moment to change trim one centimeter (ton-m)
TPC: Increase in Displacement ${ }_{\text {MId }}$ (ton) per one centimeter immersion
WSA: Wetted surface area ( $\mathrm{m}^{2}$ )
$\mathrm{C}_{\mathrm{B}}$ : Block coefficient
$\mathrm{C}_{\mathrm{wp}}$ : Water plane area coefficient
$\mathrm{C}_{\mathrm{M}}$ : Midship section area coefficient
$\mathrm{C}_{\mathrm{p}}$ : Prismatic coefficient
Trim: Trim(= after draft - forward draft) (m)

Hydrostatic Curve

sydtob

$$
M_{W P}=M_{y}=\int x d A
$$

$\checkmark$ Displacement volume ${ }^{\text {sencenece }}$

$\therefore \nabla=\int A(x) d x$

Vertical Moment of Displacement Volume ( $M_{\nabla, V}$ ) and Vertical Center of Buoyancy ( $V C B$ or $K B$ )



Transverse Moment of Displacement Volume ( $M_{\nabla, T}$ ) and Transverse Center of Buoyancy (TCB)




Transverse Metacentric Radius ( $B M$ ), Longitudinal Metacentric Radius $\left(B M_{L}\right)$, Moment to change Trim 1 Cm (MTC), and Trim

$$
B M_{0}=\frac{I_{T}}{\nabla}\left(1+\tan ^{2} \phi\right)
$$



## Example of Offsets Table of a 6,300TEU Container Ship



Example of Lines of a 6,300TEU Container Ship

- Fore Body


|  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |



Relationship Between Lines and Offsets Table (2/2)


Example of Hydrostatic Tables of a 6,300TEU Container Ship (1/2)

| $\begin{gathered} \text { DRAFT } \\ (\mathrm{M}) \end{gathered}$ | $\underset{\operatorname{MLD}\left(M^{3}\right)}{\operatorname{DISP}}$ | $\begin{gathered} \text { DISP } \\ \text { EXT(Ton) } \end{gathered}$ | $\begin{aligned} & V C B \\ & (\mathrm{M}) \end{aligned}$ | $\underset{(\mathrm{M})}{L C B}$ | $\underset{(\mathrm{M})}{\mathrm{LCF}}$ | $\begin{aligned} & K M \\ & (\mathrm{M}) \end{aligned}$ | $\underset{(\mathrm{M})}{K M_{2}}$ | $\begin{gathered} \text { MTC } \\ (\mathrm{T}-\mathrm{M}) \end{gathered}$ | $T P C$ (Ton) | $\underset{\left(\mathrm{M}^{2}\right)}{\text { WSA }}$ | $C_{B}$ | $C_{\text {w }}$ | $C_{P}$ | $C_{M}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4.000 | 22054.0 | 22720.3 | 2.171 | -2.732 | -1.546 | 31.537 | 926.651 | 795.5 | 68.5 | 7474.0 | 0.5248 | 0.6332 | 0.5769 | 0.9097 |
| 4.050 | 22389.1 | 23064.3 | 2.199 | -2.714 | -1.535 | 31,314 | 916.847 | 798.9 | 68.7 | 7507.8 | 0.5261 | 0.6349 | 0.5777 | 0.9107 |
| 4.100 | 22726.2 | 23410.3 | 2.226 | -2.697 | -1.523 | 31.098 | 907.266 | 802.4 | 68.9 | 7541.5 | 0.5275 | 0.6367 | 0.5786 | 0.9118 |
| 4.150 | 23053.3 | 23756.4 | 2.253 | -2.680 | $-1.511$ | 30.889 | 897.964 | 805.9 | 69.1 | 7575.3 | 0.5288 | 0.6384 | 0.5794 | 0.9128 |
| 4.200 | 23400.4 | 24102.4 | 2.281 | -2.663 | -1.500 | 30.686 | 888.93 | 809.3 | 69.3 | 7609.1 | 0.5302 | 0.6402 | 0.5802 | 0.9138 |
| 4.250 | 23737.5 | 24448.5 | 2.308 | -2.646 | -1.488 | 30.490 | 880.152 | 812.8 | 69.5 | 7642.9 | 0.5314 | 0.6420 | 0.5810 | 0.9147 |
| 4.300 | 24077.3 | 24797.2 | 2.336 | -2.630 | -1.476 | 30.300 | 871.537 | 816.3 | 69.7 | 7676.7 | 0.5327 | 0.6437 | 0.5818 | 0.9157 |
| 4.350 | 24419.0 | 25148.0 | 2.363 | -2.614 | -1.465 | 30.115 | 863.102 | 819.8 | 69.9 | 7710.5 | 0.5341 | 0.6454 | 0.5826 | 0.9166 |
| 4.400 | 24760.7 | 25498.8 | 2.391 | -2.598 | -1.453 | 29.936 | 854.9 | 823.3 | 70.1 | 7744.3 | 0.5354 | 0.6472 | 0.5835 | 0.9176 |
| 4.450 | 25102.4 | 25849.6 | 2.418 | -2.582 | -1.441 | 29.762 | 846.921 | 826.7 | 70.3 | 7778.1 | 0.5366 | 0.6489 | 0.5843 | 0.9185 |
| ... |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 7.500 | 47233.9 | 48564.4 | 4.087 | $-2.084$ | -2.217 | 21.918 | 560.803 | 1023.9 | 78.2 | 9736.7 | 0.5979 | 0.7224 | 0.6283 | 0.9517 |
| 7.550 | 47615.8 | 48956.4 | 4.115 | $-2,086$ | $-2.257$ | 21.852 | 558.143 | 1027.2 | 78.3 | 9768.7 | 0.5988 | 0.7235 | 0.6290 | 0.9520 |
| 7.600 | 47999.0 | 49349.6 | 4.142 | -2.088 | -2.302 | 21.785 | 555.428 | 1030.3 | 78.4 | 9800.7 | 0.5996 | 0.7246 | 0.6296 | 0.9523 |
| 7.650 | 48382.1 | 49742.8 | 4.170 | -2.090 | -2.348 | 21.722 | 552.756 | 1033.4 | 78.6 | 9832.7 | 0.6004 | 0.7256 | 0.6303 | 0.9527 |
| 7.700 | 48765.2 | 50136.0 | 4.197 | -2.092 | -2.393 | 21.659 | 550.126 | 1036.6 | 78.7 | 9864.6 | 0.6013 | 0.7267 | 0.6309 | 0.9530 |
| 7.750 | 49148.4 | 50529.3 | 4.224 | -2.094 | -2.438 | 21.598 | 547.537 | 1039.7 | 78.8 | 9896.6 | 0.6021 | 0.7277 | 0.6316 | 0.9533 |
| 7.800 | 49533.1 | 50924.1 | 4.252 | $-2.097$ | $-2.483$ | 21.538 | 544.992 | 1042.9 | 78.9 | 9928.6 | 0.6029 | 0.7288 | 0.6322 | 0.9536 |
| 7.850 | 49919.1 | 51320.2 | 4.279 | -2.100 | -2.527 | 21.481 | 542.488 | 1046.1 | 79.0 | 9960.7 | 0.6037 | 0.7298 | 0.6329 | 0.9539 |
| 7.900 | 50305.0 | 51716.3 | 4.307 | $-2.104$ | $-2.571$ | 21.424 | 540.023 | 1049.2 | 79.1 | 9992.8 | 0.6045 | 0.7309 | 0.6335 | 0.9542 |
| 7.950 | 50690.9 | 52112.3 | 4.334 | $-2.107$ | -2.615 | 21.369 | 537.595 | 1052.4 | 79.2 | 10024.8 | 0.6053 | 0.7319 | 0.6342 | 0.9544 |
| ... |  |  |  |  |  |  |  |  |  |  |  |  |  |  |


| $\underset{(\mathrm{M})}{\text { DRAFT }}$ | $\underset{\operatorname{MLD}\left(\mathrm{M}^{3}\right)}{\operatorname{DISP}}$ | $\begin{gathered} \text { DISP } \\ \text { EXT(Ton) } \end{gathered}$ |  |  |  | $\begin{aligned} & K M \\ & \text { (M) } \end{aligned}$ |  |  | $\begin{gathered} \text { TPC } \\ \text { (Ton) } \end{gathered}$ |  | $C^{\prime \prime}$ | $C_{w}$ | $C_{F}$ | $C_{M}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11.750 | 81677.2 | 83912.8 | 6.431 | . 98 | -8.607 | 18.91 | 430.346 | 1347.2 | 88.1 | 5.4 | . 593 | . 8134 | 0.6803 | 92 |
| 11.800 | 82107.4 | 8354.3 | 6.459 | -3.326 | -8.710 | 18.912 | 430.028 | 1353.1 | 88.2 | 12631.3 | 0.6600 | 0.8148 | 0.6809 | 0.9693 |
| 11.850 | 8253 | 84797.3 | 6. | -35 | -8. | 18.905 | 429.787 | 1359.4 | 88.4 | 67.6 | . 606 | 8162 | 0.6815 | . 695 |
| 11.900 | 82970.8 | 85240.4 | 6.515 | -3.384 | -8.923 | 18.90 | 429.5 | 1365 | 88.5 | 12703.9 | 0.6613 | 0.8176 | 0.6820 | 0.9696 |
| 11.950 | 83402.4 | 683 | 6.543 | 退 | -9.0. | 18.89 | 429.31 | 1371. | 88.7 | 740.2 | 0.620 | 819 | 0.6826 | 7 |
| 12.000 | 83634.1 | 86126.4 | 6.571 | -3.442 | -9.136 | 18.88 | 429.08 | 1378.1 | 88.8 | 12776.5 | 0.6626 | 0.8204 | 0.6832 | . 698 |
| 12,050 | 84267.9 | 86571.6 | 6.599 | -3.471 | -9.233 | 18.87 | 428,885 | 1384.5 | 89.0 | 12812.5 | 0.6633 | 0.8218 | 0.6838 | 700 |
| 12.100 | 84703.3 | 87018.4 | 6.627 | -3.501 | -9.32 | 18.86 | 428.71 | 1391. | 89.1 | 12848.3 | 0.663 | 0.8231 | 0.6844 | 0.9701 |
| 12.150 | 85138.6 | 8465.1 | 6.6 | -3.531 | -9.413 | 18.85 | 428.55 | 1397. | 89.3 | 12884.0 | 0.6646 | 0.8245 | 0.6850 | . 9702 |
| 12.200 | 85573.9 | 87911.9 | 6.683 | -3.561 | $-9.50$ | 18.840 | 428.38 | 1404 | 89.4 | 12919.8 | 0.665 | 0.8258 | 0.6856 | 0.9703 |
| 12.250 | 86 | 88358.7 | 6.711 | -3.59 | -9.593 | 18.82 | 428.22 | 1410 | 89.5 | 12955 | 0.665 | 0.8271 | 0.686 | 0.9705 |
| ... |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 14.250 | 104062.4 | 10688 | 7.843 | -4.937 | -12.78 | 18. | 423. | 1683.1 | 95.4 | 391 | 6924 | . 8808 | 0.7105 | 6 |
| 14.300 | 104528.0 | 107363.1 | 7.872 | -4.973 | -12.837 | 18.604 | 423.328 | 1689.2 | 95.5 | 14426.2 | 0.6931 | 0.8819 | 0.7111 | 0.9747 |
| 14.350 | 104995.0 | 107842.2 | 7.9 | . 008 | -12.880 | 18.68 | 423.0 | 1695 | 95.6 | 1461.0 | 0.693 | 0.8831 | 0.7117 | 0748 |
| 14.400 | 105451.9 | 108321.3 | 7.929 | -5.042 | -12.940 | 18.68 | 422.78 | 1701. | 95.7 | 14495.8 | 0.694 | 0.8843 | 0.7123 | 0.9749 |
| 14.450 | 105928.8 | 108800 | 7.9 | -5. | -12.992 | 18.682 | 422.5 | 1708 | 95.9 | 14530 | 0.695 | . 88 | 0.71 | 0.9750 |
| 14.500 | 106395 | 109279 | 7.986 | -5.112 | -13.043 | 18,68 | 422.2 | 1714.5 | 96.0 | 14565. | 0.6957 | 0.8866 | 0.7135 | 0.9751 |
| 14.550 | 106864.4 | 109760.5 | 8.015 | 147 | -13.090 | 18.68 | 422.0 | 1720 | 96.1 | 14600.3 | 0.6964 | 0.8878 | 0.714 | . 9751 |
| 14.600 | 107334.5 | 110242.8 | 8.043 | -5.182 | -13.133 | 18.681 | 421.779 | 1727.4 | 96.2 | 14635.1 | 0.6971 | 0.8889 | 0.7148 | 0.9752 |
| 14.650 | 107804.5 | 110725.1 | 8.072 | -5.217 | -13.176 | 18.681 | 421.55 | 1733.9 | 96.4 | 14970.0 | 0.6977 | 0.8901 | 0.7154 | 0.9753 |
| 14.700 | 108274.5 | 111207 | 8.101 | -5.251 | -13.219 | 18.681 | 421.32 | 1740.3 | 96.5 | 14704.9 | 0.6984 | 0.8912 | 0.7160 | 97 |

Example of Hydrostatic Curves of a 6,300TEU Container Ship


Example of Programming for Calculation of the Hydrostatics - Example of Hydrostatic Tables of a 320K VLCC (1/2)


Example of Programming for Calculation of the Hydrostatics

- Example of Hydrostatic Tables of a 320K VLCC (2/2)


Example of Programming for Calculation of the Hydrostatics - Example of Hydrostatic Curves of a 320K VLCC


## 2. Trim and Stability Calculation of a 3,700TEU Container Ship Including Hydrostatic Values



Midship Section in G/A



| Name | Specific Gravity | Filling Ratio* |
| :---: | :---: | :---: |
| Heavy Fuel Oil | 0.990 | $98 \%$ |

$1,214.6 \times 0.99=1,202.4$
$1,118.6 \times 0.99=1,107.4$




$$
L C G_{D W T}=\frac{\sum L C G_{i} \times \rho_{i} V_{i}}{D W T}
$$

$=$
$\qquad$

Lightweight Summary


Hydrostatic Tables


Loading Conditions: Lightship Condition (1/6)

- Lightship condition: Condition that loaded nothing (no cargo, imaginary condition)


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sydab

| ORAUGHT F.P | = | 1.526 |  | K.M. T | = | 21.296 M |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| QRAUGHT MIDSHIP | = | 3.806 | M | KG (SOLID) | = | 13.200 M |
| DRAUGHT A.P | = | 6.086 | M | GM (SOLID) | = | 8.096 M |
| TRIM BY STERN | = | 4.560 | M | FREE SUAF . CORA (GGo) | = | 000 M |
| PROPELLEA I/D | = | 74.0 | \% | GoM (FLUID) | = | 8.096 M |
| DISPLACEMENT | $=$ | 15998.1 | T | KGo ACTUAL (FLUID) | $=$ | 13.200 M |
| DRAUGHT AT LCF | = | 3.871 |  | (1) TRIM (DIS*A)/(MTC*100) | $=$ | 4. 560 M |
| L.CB FROM A.P | = | 118.416 |  | FREE SURF. MOM | $=$ | 0 T-M |
| LCG FROM A.P | = | 103.228 |  | M. T. C | = | 532.8 T-M |
| TRIM LEVER : A | = | 15.188 | M | LCF FROM A.P | = | 119.110 M |

(1) In hydrostatic tables

| DRAFT <br> (M) | $\begin{aligned} & \text { DISP } \\ & \text { MLD(M3) } \end{aligned}$ | $\begin{gathered} \text { OISP } \\ \operatorname{EXT}(T) \end{gathered}$ | VCB <br> (M) | $\begin{aligned} & \text { LCB } \\ & (M) \end{aligned}$ | $\begin{aligned} & \text { L.CF } \\ & (M) \end{aligned}$ | KMT <br> (M) | $\begin{aligned} & \text { KML } \\ & (M) \end{aligned}$ | $\begin{aligned} & \text { MTC } \\ & (T-M) \end{aligned}$ | $\begin{gathered} \text { TPC } \\ \text { (TON) } \end{gathered}$ | WSA (M2) | C B | C W | $C P$ | CM |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3.75 | 14919.7 | 15400.8 | 2.025 | 18.39 | 9.002 | 21.691 | 838.95 | 525.6 | 49.7 | 5602.1 | . 5072 | . 6127 | . 5421 | . 9356 |
| 380 | 151608 | 15648.4 | 2051 | 18 | 19018 | 21.524 | 830.12 | 528.6 | 19.9 | 56317 | 5086 | 6145 | 5431 | 9364 |
| 3.85 | 15401.8 | 15896.1 | 2.076 | 118.412 | 119.093 | 21.362 | 822.15 | 531.6 | 50.0 | 5661.4 | . 5099 | 6163 | . 5441 | . 9372 |
| 3.90 | 15644.8 | 16145.8 | 2.103 | 118.422 | 119.132 | 21.201 | 813.71 | 534.3 | 50.1 | 5690.8 | . 5113 | 6180 | . 5451 | . 9380 |
| 3.95 | 15891.1 | 16398.8 | 2.133 | 718.434 | Y. 159 | 21.031 | 804.83 | 536.7 | 50.3 | 5719.8 | . 5121 | . 6196 | . 5462 | . 9388 |

By linear interpolation, draft at $\mathrm{LCF}=3.871[\mathrm{~m}], V C B(=K B)=2.087[m]$,


| ORAUGHT F.P | = | 1.526 M | K.M. T | $=$ | 21.296 M |
| :---: | :---: | :---: | :---: | :---: | :---: |
| DRAUGHT MIDSHIP | = | 3.806 M | KG (SOLID) | = | 13. 200 M |
| DRAUGHT A.P | = | 6.086 M | GM (SOLID) | $=$ | 8.096 M |
| TRIM BY STERN | = | 4.550 M | FREE SUAF. CORA (GGo) | = | 000 M |
| PROPELLEA I/D | = | $74.0 \%$ | Gom (FLUID) | $=$ | 8.096 M |
| DISPLACEMENT | = | 15998.1 T | KGo ACTUAL (FLUID) | = | 13.200 M |
| draught at lcF | = | 3.871 M | TRIM (DIS*A) / (MTC* 100 ) | $=$ | 4.560 M |
| LCB FROM A.P | $=$ | 118.416 M | FREE SURF. MOM | $\cdots$ | $0 \mathrm{~T}-\mathrm{M}$ |
| LCG FROM A.P | $=$ | 103.228 M | M. T. C | = | 532.8 T-M |
| TRIM LEVER : A | = | 15.188 M | LCF FROM A.P | = | 119.110 M |

(2)
(3) Trim $[\mathrm{m}]=\frac{\Delta \times \text { Trim Lever }}{M T C \times 100}=\frac{15,998.1 \times 15.188}{532.8 \times 100}=4.560[\mathrm{~m}]$



Loading Conditions: Ballast Departure Condition (1/6)

- Ballast departure condition: Condition that loaded ballast water and consumable cargo

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| QRAUGHT F.P | = | 5.553 |  | K.M. T | = | 15.728 | M |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| QRAUGHT MIDSHIP | = | 6.998 | M | KG (SOLID) | $=$ | 9.584 | M |
| ORAUGHT A.P | = | 8.443 | M | GM (SOLID) | = | 6.144 | M |
| TRIM BY STERN | $=$ | 2.890 |  | FREE SURF. CORR (GGo) | = | 177 | M |
| PROPELLER I/D | $=$ | 105.1 |  | Gom (FLUTO) | = | 5.967 | M |
| DISPLACEMENT | = | 32980.1 |  | KGo ACTUAL (FLUID) | $=$ | 9.761 | M |
| DRAUGHT AT LCF | = | 7.044 |  |  | $=$ |  |  |
| LCB FROM A.P |  | 118.910 |  | 1) FREF SUAF MOM | $=$ | 5847 | T-M |
| LCG FPRM A.P | = | 113.116 |  | M.T.C. | $=$ | 661.3 | T-M |
| TRIM LEVER: A | $=$ | 5.794 |  | LCF FHOMM A | = | 118.107 |  |

(1) In hydrostatic tables

| DRAFT (N) | $\begin{aligned} & \text { OISP } \\ & \text { MLD(M3) } \end{aligned}$ | $\begin{gathered} \text { OISP } \\ \operatorname{EXT}(T) \end{gathered}$ | $\begin{aligned} & \text { VCB } \\ & (M) \end{aligned}$ | $\begin{aligned} & \mathrm{LCB} \\ & (M) \end{aligned}$ | $\begin{aligned} & \mathrm{LCF} \\ & (\mathrm{M}) \end{aligned}$ | KMT <br> (M) | KML <br> (M) | $\begin{aligned} & \text { MTC } \\ & (T-M) \end{aligned}$ | $\begin{gathered} \text { TPC } \\ \text { (TON) } \end{gathered}$ | WSA (M2) | C B | C W | C P | C M |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 7.00 | 31782.0 | 32730.5 | 3.802 | 118.912 | 18.753 | 15.763 | 498.01 | 659.6 | 56.4 | 7422.2 | . 5770 | . 6945 | . 5976 | 9655 |
| 7.05 | 32056.1 | 33012.2 | 3.829 | 118.910 | 18.701 | 15.724 | 495.22 | 661.5 | 56.5 | 7450.0 | . 5779 | 6956 | . 5983 | 9658 |
| 7.10 | उ<332.2 | $3 \times 250.0$ | 3.858 | 178.907 | 178.639 | 15.686 | 492.45 | 663.4 | 56.5 | 7478.0 | 5787 | 6966 | . 5991 | 9660 |
| 7.15 | 32608.3 | 33579.8 | 3.886 | 118.903 | 118.577 | 15.649 | 489.74 | 665.3 | 56.6 | 7506.0 | 5796 | . 6977 | . 5998 | 9662 |
| 7.20 | 32884.4 | 33863.6 | 3.914 | 118.900 | 118.516 | 15.613 | 487.07 | 667.2 | 56.7 | 7534.1 | 5804 | . 6987 | 6005 | 9665 |

$$
V C B(=K B)=3.826[\mathrm{~m}],
$$


(2)
(3) Trim $[m]=\frac{\Delta \times \text { Trim Lever }}{M T C \times 100}=\frac{32,980.1 \times 5.794}{661.3 \times 100}=2.890[\mathrm{~m}]$

| DRAUGHT F.P <br> DRAUGHT MIDSHIP <br> ORAUGHT A.P <br> TRIM BY STERN <br> PROPELLER I/D <br> DISPLACEMENT | $=$ $=$ $=$ $=$ $=$ $=$ | 5.553 M 6.998 M 8.443 M 2.890 M 105.1 m 32980.1 T | K.M. T KG (SOLID) GM (SOLID) FREE SURF. CORR. (GGO) GOM (FLUIO) KGO ACTUAL (FLUID) | $=$ $=$ $=$ $=$ $=$ | 15.728 M <br> 9.584 M <br> 6.144 M <br> .177 M <br> 5.967 M  <br> 9.761 M  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| DRAUGHT AT LCF <br> LCB FROM A.P <br> LCG FROM A.P <br> TRIM LEVER : A | $=$ $=$ $=$ $=$ | $\begin{array}{r} 7.044 \mathrm{M} \\ 118.910 \mathrm{M} \\ 113.116 \mathrm{M} \\ 5.794 \mathrm{M} \end{array}$ | ```TRIM (DIS*A)/(MTC*100) FREE SURF. MOM. M.T.C. LCF FROM A.P``` | $=$ $=$ $=$ $=$ | $\begin{array}{r} 2.890 \mathrm{M} \\ 5847 \mathrm{~T}-\mathrm{M} \\ 661.3 \mathrm{~T}-\mathrm{M} \\ 118.707 \mathrm{M} \end{array}$ |



[Example] Calculation of an Angle of Heel (1/2)
A box-shaped barge ( $L \times B \times D: 100 m \times 20 m \times 12 m$ ) is floating in freshwater on an even keel at draft of 6 m . Vertical center of mass of the barge is 4 m from baseline. When an external moment about $x$ axis of 3,816 ton-m is applied on the ship, calculate an angle of heel.


## [Example] Calculation of an Angle of Heel (2/2)


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Given
L: $100 \mathrm{~m}, \mathrm{~B}: 20 \mathrm{~m}, \mathrm{D}: 10 \mathrm{~m}, \mathrm{~T}: 5 \mathrm{~m}, \mathrm{KG}: 7 \mathrm{~m}$
Cargo Load: 1,000ton
(At 20 m in front of the center of the ship and 4 m
above the baseline)
Find: The draft at the aft perpendicular of the ship


(1) Calculation of the change of the draft (T)
$\delta \Delta=T P C \cdot \delta T$
(2)-2) Calculation of $G M_{L 1}$
$K B_{1}=2.744 \mathrm{~m}$ -
$\square$
(3) Calculation of the draft at the aft perpendicular of the ship

$$
T_{A f, F \text { Fore }}=T_{1} \pm \frac{\operatorname{trim}}{2}
$$

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## [Example] Calculation of Trim for a Barge Ship When the Cargo is Moved

A barge ship is 20 m length, 12 m breadth, 4 m depth, and is floating at 2 m draft in the fresh water. When a 10ton cargo which is loaded on the center of the deck is moved to 4 m in the direction of the forward perpendicular and 2 m in the direction of the starboard, determine the draft at the forward perpendicular (FP), after perpendicular (AP), portside, and starboard of the ship. KG of the ship is given as 2 m .

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1. Change of draft caused by trim

$$
\operatorname{Trim}[\mathrm{m}]=\frac{\sum \text { Trim Moment }}{M T C \cdot 100}
$$

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# - Trim moment caused by moving the cargo in the direction of the forward perpendicular <br> Trim Moment $=10 \cdot 4 \cdot \cos \theta \approx 40$ ton $\cdot m$ 

$\square$

$$
\delta y_{G}^{\prime}=\frac{w \cdot l_{T}}{\Delta}=0.04 \mathrm{~m}
$$

$\square=$
If the inclination angles are small, the difference of the
approximate solution and exact solution will be small.
The linearized terms in the solving procedure

- Trim moment $w \cdot l \cdot \cos \theta \cong w \cdot l$
$-I_{L} I_{T}$
- AWP
- TPC, MTC
$-\mathrm{KB}_{1}$
$-\mathrm{LCB}_{1}$



## [Example] Calculation of Trim of a Ship (2/7)

Given:
L: $180 \mathrm{~m}, \mathrm{~B}: 30 \mathrm{~m}, \mathrm{D}: 10 \mathrm{~m}, \mathrm{~T}: 8 \mathrm{~m}$
Density of the ship material $\rho_{m}=1.0 \mathrm{ton} / \mathrm{m}^{3}$.
The ship is floating in fresh water.
Find:
(1) Displacement ( A )
(2) $\mathrm{LCF}, \mathrm{LCB}, \mathrm{LCG}, \mathrm{KG}$
(3) When the all cargo hold are full with the load
whose density is $0.6 \mathrm{ton} / \mathrm{m}^{3}$ homogeneously,
DWT and LWT?
(4) How do we calculate the change of the trim
when the cargo is loaded or unloaded?
$\mathbf{F}=\mathbf{A x}$
(2) LCF, LCB, LCG, KG
(3) When the all cargo hold are full with the load DWT and LWT?
(4) How do we calculate the change of the trim when the cargo is loaded or unloaded?

Given:
L: $180 \mathrm{~m}, \mathrm{~B}: 30 \mathrm{~m}, \mathrm{D}: 10 \mathrm{~m}, \mathrm{~T}: 8 \mathrm{~m}$
L: $180 \mathrm{~m}, \mathrm{~B}: 30 \mathrm{~m}, \mathrm{D}: 10 \mathrm{~m}, \mathrm{~T}: 8 \mathrm{~m}$
Density of the ship material: $\rho_{m}=1.0$ ton $/ \mathrm{m}^{3}$
The ship is floating in fresh water.
Find:
(1) Displacement ( $\Delta$ )
(2) LCF, LCB, LCG, KG
(3) When the all cargo hold are full with the
load whose density is 0.6 ton $/ \mathrm{m}^{3}$
homogeneously.
What is the DWT and LWT?
(4) How do we calculate the change of the trim when the cargo is loaded or unloaded?

|  |  |
| :--- | :--- |
| $\square$ |  |
| $\square$ |  |
| $\square$ |  |



## (3) When the all cargo hold are full with the load whose density is 0.6 ton $/ \mathrm{m}^{3}$ homogeneously. What is the DWT and LWT?

$$
D W T=A_{W P_{-} \text {Hold }} \cdot D \cdot \rho_{\text {cargo }}
$$

$\square$

## [Example] Calculation of Barge Ship's Trim and Heel Angles (1/18)

A barge ship of 28 m length, 18 m breadth, 9 m height, 1 m shell plate thickness, density of shell plate $\rho_{m}=1.0$ ton $/ \mathrm{m}^{3}$ is shown below.
(1) Calculate ship's lightweight and draft
 in fresh water under the condition of "light ship" loading condition. And if the 10 m barge ship is floating in sea water, what is the draft?
(2) The barge ship floats in fresh water and it carries the loads as shown in the table.

| Item | Unit Mass | \# of Cargoes | Loading position $(\mathrm{m})$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $x$ | $y$ | $z$ |
|  |  | 3 | 0 | 0 | 1 |
| Freight 1 | 100 ton | 2 | -5 | 0 | 1 |
| Freight 2 | 150 ton | 2 |  |  |  |

Calculate the ship's (a) deadweight (DWT) (b) TPC © MTC © Trim © Fore and after drafts (f) LCB © LCG.
(3) From the result of the question (2), if the freight 2 is unloaded from the barge ship, calculate LCB and LCG.
(4) From the result of the question (3), if the freight 1 moves 5 m along the positive y direction. calculate the barge ship's heel angle.
[Example] Calculation of Barge Ship's Trim and Heel Angles (2/18)
Given:
L: $30 \mathrm{~m}, \mathrm{~B}$ : $20 \mathrm{~m}, \mathrm{D}$ : 10 m , Shell plate thickness:
1m
Density of the shell plate: $\rho_{m}=1.0$ ton $/ \mathrm{m}^{3}$

$\Delta_{L W T}=A_{w P} \cdot T_{f w} \cdot \rho_{f w}$
(2) When the freight 1 and 2 are loaded in fresh water (a) Deadweight (DWT) (b) TPC © MTC (d) Trim (e) Fore and after drafts $\oplus$ LCB (9) LCG

# (1) LWT, Draft in fresh water ( $\mathrm{T}_{\mathrm{fw}}$ ), Draft in sea water $\left(\mathrm{T}_{\mathrm{sw}}\right)$ 

$\Delta_{L w T}=\overline{A_{w p}} \cdot T_{f w} \cdot \rho_{f w}$
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(b) TPC is calculated as follows:

$$
T P C=\frac{A_{W P} \cdot \rho_{f w}}{100}=\frac{20 \cdot 30 \cdot 1.0}{100}=6 \mathrm{ton} / \mathrm{cm}
$$



$$
\begin{aligned}
G M_{L} & =K B+B M_{L}-K G \\
& =1.72+21.8-2.09=21.43 \mathrm{~m}
\end{aligned}
$$

(d) Loading of the freight 2 leads to

Trim Moment $=-5 \cdot(150 \cdot 2)=-1,500$ ton $\cdot m$

$-1$
$=$
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(3) Freight 2 is unloaded from (2), calculate LCB, LCG.

If the freight 2 is unloaded from the condition (2), the ship's trim becomes zero. Hence $\mathrm{LCB}=\mathrm{LCG}=0$. At this time, the displacement $\Delta$ is 1,764 ton, draft is $1,764 /(30 \cdot 20)=2.94 \mathrm{~m}$.

## [Example] Calculation of Barge Ship's Trim and Heel Angles (15/18)

lacement $\Delta$ is 1,764 ton, draft is $1,764 /(30 \cdot 20)=2.9$


Restoring moment is obtained using the following equation. $G Z=G M \cdot \sin \phi=(K B+B M-K G) \cdot \sin \phi$

Because the barge ship's shape is box-shape

[Example] Practical Calculation of a Ship's Fore and Aft Drafts (1/9)

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[Example] Practical Calculation of a Ship's Fore and Aft Drafts (2/9)


# Trim $[\mathrm{m}]=\frac{\sum \text { Trim Moment }}{M T C \cdot 100}$ 

## i) Full loading condition

Ship's total weight at full loading condition: $\Delta=168,962$ ton

# $M T C=\frac{\Delta \cdot \overline{G M_{L}}}{100 \cdot L_{B P}}$ 

$1 \times$

Change in trim: $\delta t=8.937 \mathrm{~m}$
$\qquad$

(1) Calculation of parallel rise (draft change)

- Tones per 1 cm immersion (TPC)



