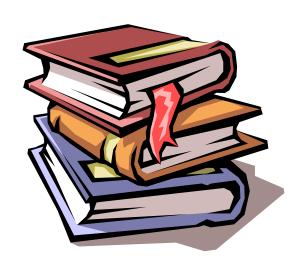
# **Cryogenic Engineering**

2015 Fall Semester Min Soo, Kim



Chapter 8.
Vacuum Technology



### 8.2 Flow regimes in vacuum systems

#### Flow in low pressure

At low pressure, the gas molecules are so far apart that the gas cannot be treated as a continuous medium, and we obtain another flow regime

#### free molecular flow

The dimensionless parameter used to determine the dividing line between continuum and free-molecular flow is the *Knudsen number*,  $K_{Kn} = \lambda/D$ 

- 1. Continuum flow,  $K_{Kn} < 0.01$
- 2. Mixed flow,  $0.01 < K_{Kn} < 0.30$
- 3. Free-molecular flow,  $0.30 < K_{Kn}$
- $\lambda$ : mean free path of the gas molecules
- D: characteristic dimension of the flow channel



# 8.2 Flow regimes in vacuum systems

#### Degree of vacuum

- 1. Rough vacuum, 25 torr < P
- 2. Medium vacuum,  $10^{-3}$  torr < P < 25 torr
- 3. High vacuum,  $10^{-6}$  torr < P <  $10^{-3}$  torr
- 4. Medium vacuum,  $10^{-9}$  torr  $< P < 10^{-6}$  torr
- 5. Medium vacuum,  $P < 10^{-9}$  torr

$$1 torr = 133.322 Pa = \frac{1}{760} atm$$



For laminar continuum flow in a circular tube, Poisseuille's equation

$$\Delta p = 128\mu L\dot{m}/\pi D^4 \rho g_c$$
where  $L =$  tube length
$$D =$$
 tube diameter
$$\bar{\rho} =$$
 mean fluid density
$$\mu =$$
 fluid viscosity

Substituting 
$$\bar{\rho} = \frac{\bar{p}M}{R_{\nu}T}$$
, where  $\bar{p} = (p_1 + p_2)/2$ 

$$\Delta p = 128\mu L R_u T \dot{m} / \pi D^4 g_c \bar{p} M$$



According to kinetic theory of gases (Kennard 1938), the mass flow rate for mixed flow in a circular tube

$$\dot{m} = \frac{\pi D^4 g_c \bar{p} \Delta p}{128 \mu L R_u T} \left[ 1 + \frac{8\mu}{\bar{p} D} \left( \frac{\pi R_u T}{2g_c M} \right)^{1/2} \right]$$

For free-molecular flow in long tubes

$$\dot{m} = \left(\frac{\pi g_c M}{18R_u T}\right)^{1/2} \left(\frac{D^3 \Delta p}{L}\right)$$



The throughput is commonly used in vacuum work

$$Q = p\dot{V} = \dot{m}R_uT/M$$

A conductance C for a vacuum element

$$C = Q/\Delta p = m/\Delta \rho$$



The conductance for a long tube may be written as follows.

1. Laminar continuum flow

$$C = \pi D^4 g_c \bar{p} / 128 \mu L$$

2. Mixed flow

$$C = (\pi D^4 g_c \bar{p} / 128\mu L) [1 + (8\mu/\bar{p}D) \left(\frac{\pi R_u T}{2g_c M}\right)^{1/2}]$$

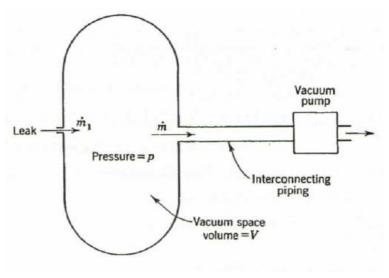
3. Free molecular flow

$$C = (\pi g_c R_u T / 18M)^{\frac{1}{2}} (D^3 / L)$$



# 8.4 Calculation of pump-down time for a vacuum system

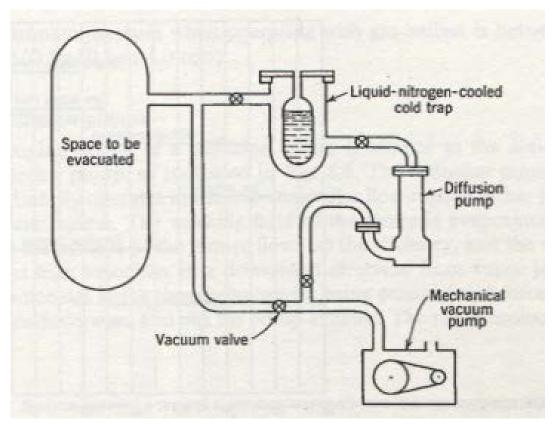
One of the important factors in the design of a vacuum system is the determination of the pump-down time, or the time required to reduce the pressure of the system from ambient pressure to the desired operating pressure.



Vacuum system for pump-down equation development



### 8.5 Components of vacuum systems



<Basic elements of a typical vacuum system>

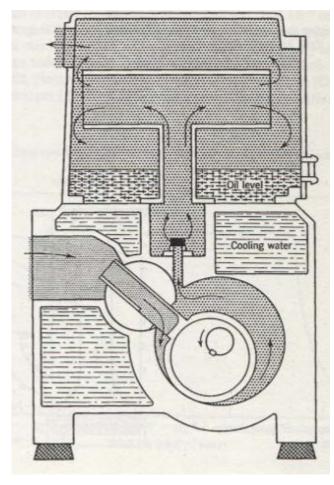


# 8.5 Components of vacuum systems

- Mechanical vacuum pump is used as a forepump or roughing pump to reduce the system pressure to approx. 1.0Pa
- Diffusion pump operates if the pressure reduces about 1.0Pa valve in the bypass line is closed
- Cold trap or baffle are provided near the inlet of the diffusion pump preventing backstreaming of oil vapor, to freeze out condensable gases



### 8.6 Mechanical vacuum pumps



<Section view of a typical rotary-piston mechanical vacuum pump>

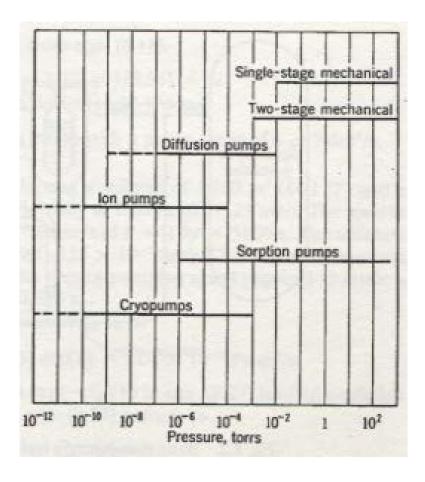


# 8.6 Mechanical vacuum pumps

- Basic principle same as the rotary pump for higher pressures!
- Eccentric rotor(piston) rotates within the cylindrical jacket.
- Gas enters the space between the two cylinders is compressed to a higher pressure as the piston rotates.
- Gas is discharged through a check valve that prevents backflow of the air into the pump space.
- Oil separator is provided to remove the oil from the gas and return the oil to the pump.
- Gas Ballast To prevent moisture condensation within the pump volume.
  - Admit sufficient atmospheric air into the pump space.

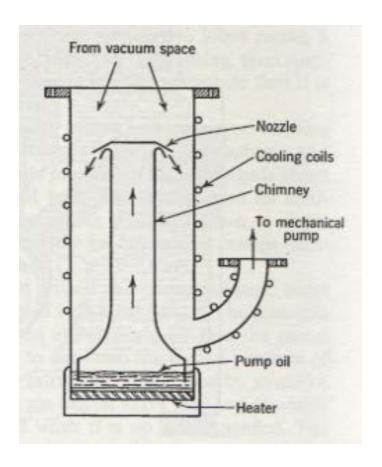


### 8.6 Mechanical vacuum pumps



<Operating range for various vacuum pumps>



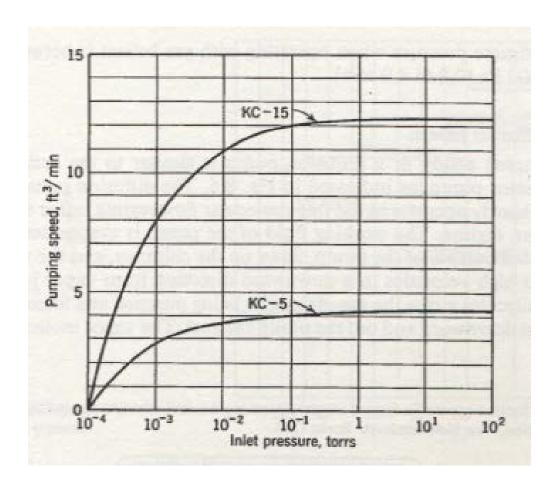


<Schematic of a single-stage diffusion pump>



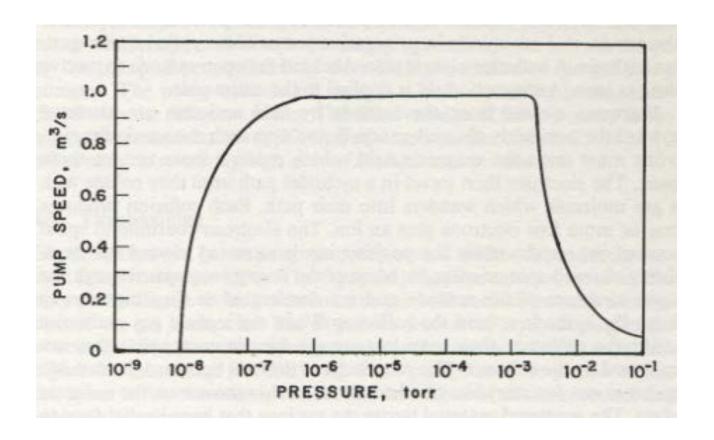
- Diffusion pumps similar to the action of a steam ejector pump.
- Ordinarily operates in the free-molecular flow regime rather than the continuum regime.
- Working fluid is evaporated in the boiler at the bottom, flows up the chimney,
   vapor is ejected at high velocities in a downward direction from vapor jets.
- Vapor molecules strikes gas molecules force the gas molecules downward and out the pump exhaust.
- Vapor molecules are condensed and returned to the boiler.
- Gas molecules removed by a mechanical backing pump.





<Pumping speed curves for mechanical vacuum pumps>





<Pumping-speed curve for a diffusion pump having a nominal diameter of 100mm(4in)>



Ideal case, a diffusion pump should remove gas molecules as fast as they diffuse into the pump inlet

→ maximum pumping speed is the same as the conductance of an aperture!

$$S_p^0 = (\frac{\pi g_c R_u T}{32M})^{1/2} D^2$$



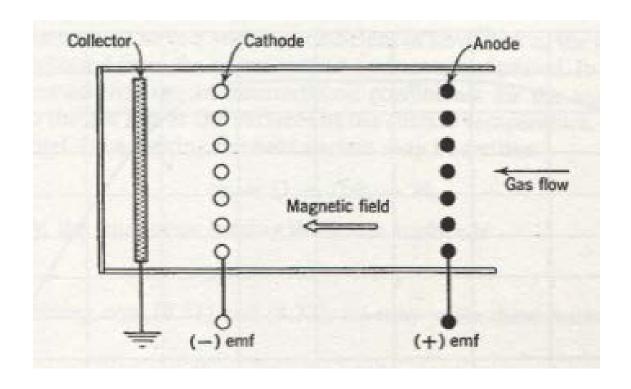
The ratio of the actual pump speed to the theoretical pump speed is called the Ho coefficient

$$S_p = H_0 S_p^0$$

Typical Ho coefficients for commercial vacuum pumps range between 0.40~0.55.



#### 8.8 Ion pumps



<Schematic of an ion pump>



#### 8.8 Ion pumps

#### Ion pump structure:

- Combination of ionization and chemisorption
- A large positive electricpotential Anode, a large negative electricpotential Chathode
- Magnetic field is applied to the entire unit

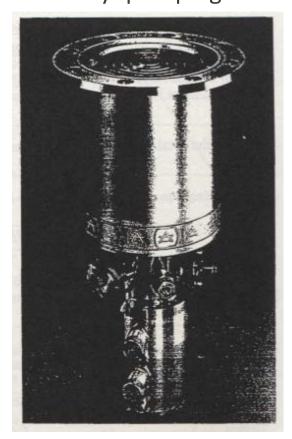


### 8.8 Ion pumps

- Electrons from cathode attracted to the anode
- Due to the magnetic field, electrons moves cycloidal path
- Collision supplies more free electrons
- Positive ion attracted to the Cathode
- Remainder of the ions bombard the cathode and tear out
- Sputtered material buries the gas ions
- The gas ions are driven to the collector
- The Ion pump has relatively high pumping efficiency!



Condensation of a gas on a cryogenically cooled surface to produce a vacuum is called "Cryopumping"

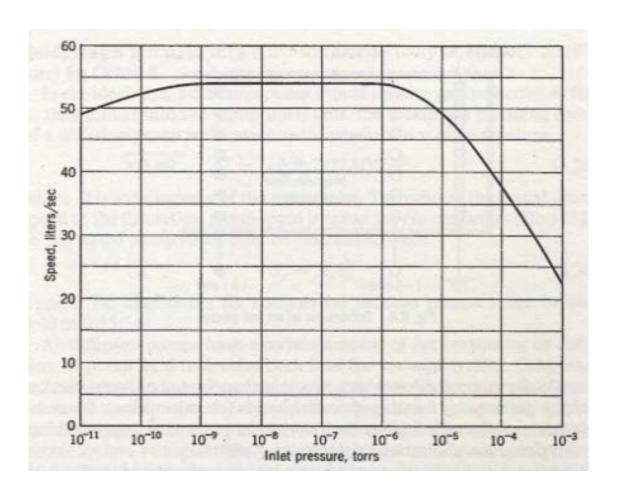


<Air products Model AP-8S cryopump>



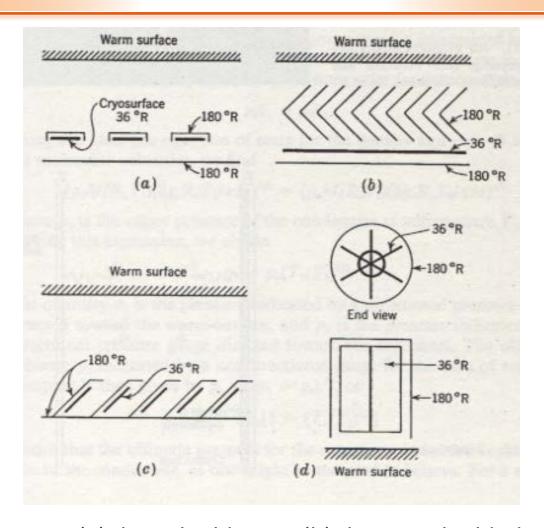
- The cryopumping phenomenon
- : Phase change from gas to solid at the cold surface + adsorption of the gas molecules.
- Extremely large pumping speeds
- Pump is placed within the space to be evacuated
- : The resistance of the interconnecting piping is eliminated.



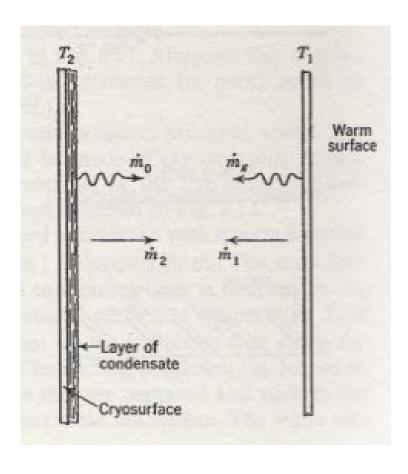


<Pumping-speed curve for an ion pump>





<Cryopump arrays – (a)Plate-shield array;(b)Chevron-shielded array;(c)Santler
array;(d)Cryopump for high-velocity wind-turnnel cryopumping>



<Parallel-plate cryopump system>



General expression for the pumping speed of the parallel-plate cryopump:

$$\frac{S_p}{A} = \frac{\left(\frac{2g_c R_u T_1}{\pi M}\right)^{\frac{1}{2}} \left(1 - \frac{p_u}{p}\right) f}{1 + \left(\frac{p_u}{p}\right) \left[\left(\frac{T_1}{T_2}\right)^{\frac{1}{2}} - 1\right] + G}$$

$$G = (1 - f)\left(\frac{T_1}{T_2}\right)^{1/2} \left\{ 1 - \left(\frac{p_u}{p}\right) \left[1 - \left(\frac{T_2}{T_1}\right)^{\frac{1}{2}}\right] \right\}$$



For the special case of unity sticking coefficient, f=1, the parameter G=0

$$(\frac{S_p}{A})_{f=1} = \left(\frac{2g_c R_u T_1}{\pi M}\right)^{\frac{1}{2}} \frac{\left(1 - \frac{p_u}{p}\right)}{1 + \left(\frac{p_u}{p}\right) \left[\left(\frac{T_1}{T_2}\right)^{\frac{1}{2}} - 1\right]}$$



Determining the sticking coefficient f,

$$f = 0.453 + 0.256 \log_{10} M \ (for M \le 137 \ g/mol)$$
  
 $f = 1 \ (for M > 137 \ g/mol)$ 



Gas Being Pumped	Cryosurface Temperature (K)	Warm-Surface Temperature (K)	Sticking Coefficient f	Reference
Ammonia	77.3	300	0.45	Brown and Wang 1965
Argon	20	77.3	0.79	Dawson et al. 1964
CO <sub>2</sub>	77.3	300	0.62	Brown and Wang 1965
CO <sub>2</sub>	20	195	0.90	Dawson et al. 1964
CO <sub>2</sub>	77.3	195	0.80	Dawson et al. 1964
CO <sub>2</sub>	20.2	300	0.65	Dawson et al. 1964
CO <sub>2</sub>	77.3	300	0.63	Dawson et al. 1964
CO <sub>2</sub>	21.0	400	0.44	Dawson et al. 1964
CO <sub>2</sub>	77.3	400	0.49	Dawson et al. 1964
Nitrogen	20		0.55	Moore 1962
Nitrogen	20	85	0.73	Hurlbut and Mansfield 1963
Nitrogen	20	77.3	0.87	Dawson et al. 1964
Water	77.3	300	0.92	Brown and Wang 1965

<Measured values of the sticking coefficient f >



In cryopumping-array calculations, the parameter  $capture\ coefficient\ C_c$  is utilized.

$$\frac{S_p}{A} = \frac{C_c}{2 - C_c} \left( \frac{2g_c R_u T_1}{\pi M} \right)^{\frac{1}{2}} (1 - \frac{p_u}{p})$$

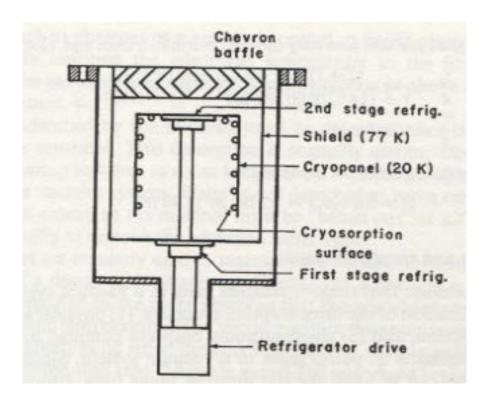


Table 8.5. Capture coefficients  $C_c$  for various cryopump configurations when pumping air (or nitrogen)

Cryopump Configuration	Capture Coefficient C <sub>e</sub>	Reference
Arrangement (a), Fig. 8.9	0.25	A. D. Little 1960
Arrangement (b), Fig. 8.9	0.27	A. D. Little 1960
Arrangement (c), Fig. 8.9	0.45	A. D. Little 1960
Arrangement (d), Fig. 8.9	0.79	Barnes and Hood 1962
NRC Modular Cryopump	0.26	Hoenig 1964
Air Products AP-8S	0.31	Bentley 1980

<Capture coefficients  $C_c$  for various cryopump configurations when pumping air(or nitrogen)>





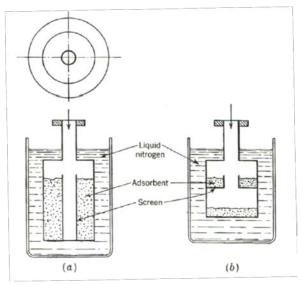
<Schematic of a cryosorption pump>



### 8.10 Getters and sorption pumps

Getters are materials that remove residual gases in a vacuum system by one or a combination of the three sorption processes:

(1) Physical adsorption (2) absorption (3) chemisorption



Typical sorption pumps



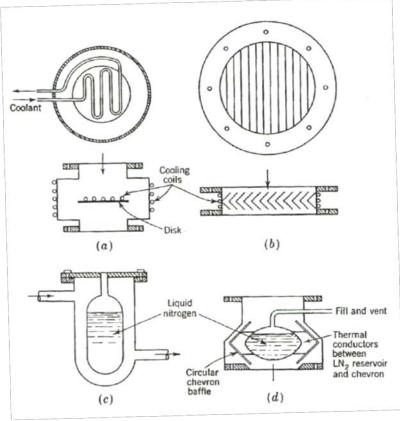
# 8.11 Baffles and cold traps

**Baffles** are cooled surfaces placed near the inlet of a vacuum pump to prevent back streaming of the pump fluid into the vacuum space.

A **cold trap** is similar to a baffle, but the cold trap in always refrigerated by a cryogenic fluid or dry ice to condense and capture both oil-vapor molecules and any other condensable gases.



#### 8.11 Baffles and cold traps

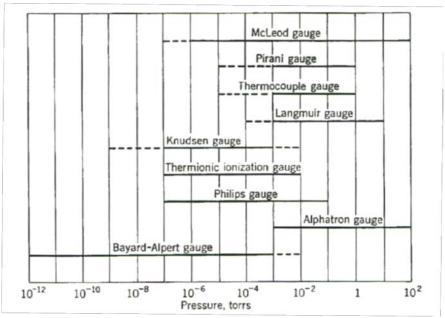


Baffles and cold traps. (a) Disc baffle; (b) chevron baffle; (c) simple cold trap; (d) combination baffle and cold trap



#### 8.12 Vacuum gauges

Because pressures measured by vacuum gauges are several orders of magnitude smaller than atmospheric pressure, most of the ordinary pressure gauges cannot be easily used n vacuum work.



Operating range for various vacuum gauges

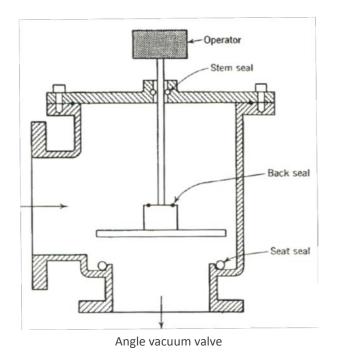


Valves used in vacuum systems require:

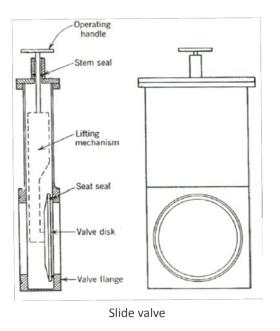
- (1) Freedom from leakage under high vacuum
- (2) Maximum conductance
- (3) Absence of outgassing



Angle valves have a relatively high conductance because the closing disc can be withdrawn completely from the flow passage.

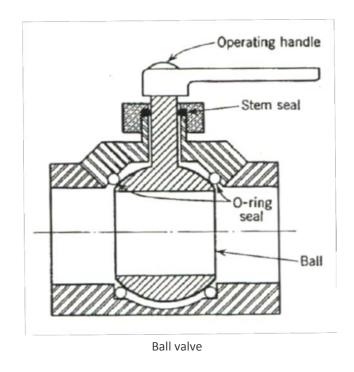


Slide valves have an in-line design and high conductance because the closing protion of the valve may be withdrawn completely from the flow passage.

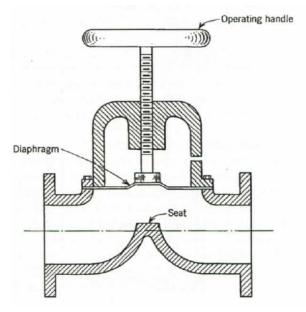




Ball valves are a form of stopcock. The valve consists of a sphere with a hole drilled through it.



The diaphragm valve is a vacuum valve of somewhat lower conductance and lower performance than the valves previously mentioned.



Diaphragm valve

