



**457.562 Special Issue on
River Mechanics
(Sediment Transport)
.11 Bed forms**



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1. Progression of bed forms

- Various bedforms are associated with various flow regimes. In the case of a sand-bed stream with a characteristic size less than about 0.5mm a clear progression is evident as flow velocity increases.
- The bed is assumed to be initially flat. At very low imposed velocity U , the bed remains flat because no sediment is moved.
 - As the velocity exceeds the critical value, ripples are first formed.
 - At higher values, dunes form and coexist with ripples.
 - For even higher velocities, well-developed dunes form in the absence of ripples.



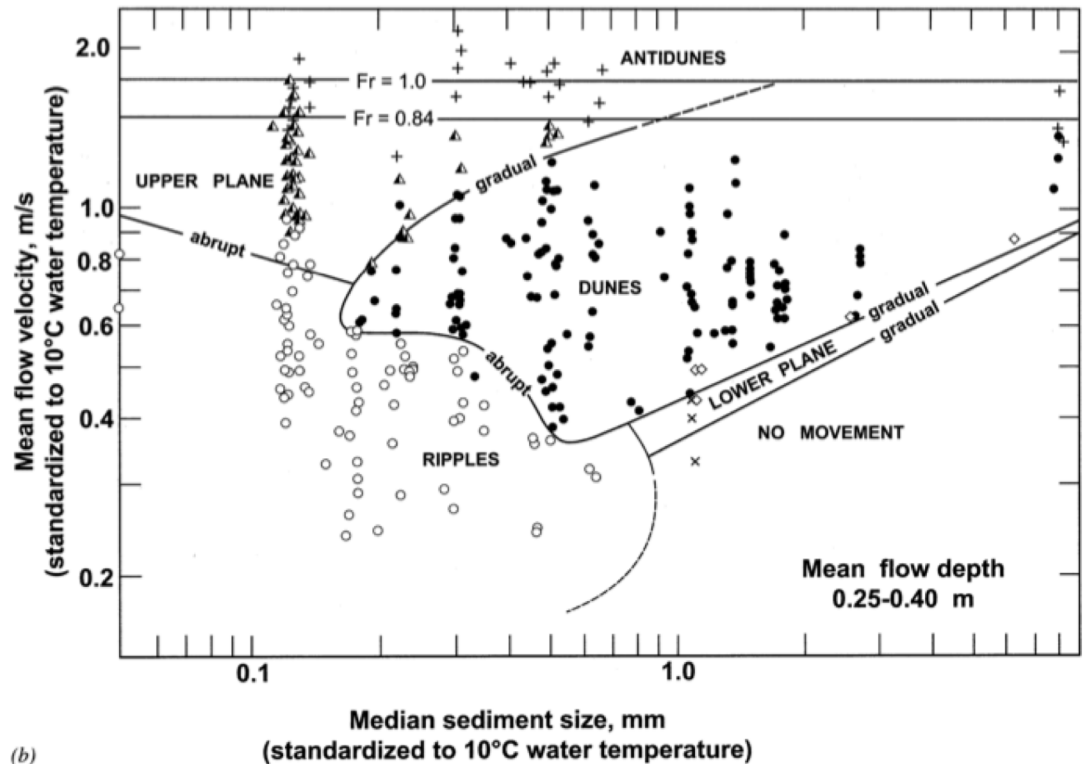
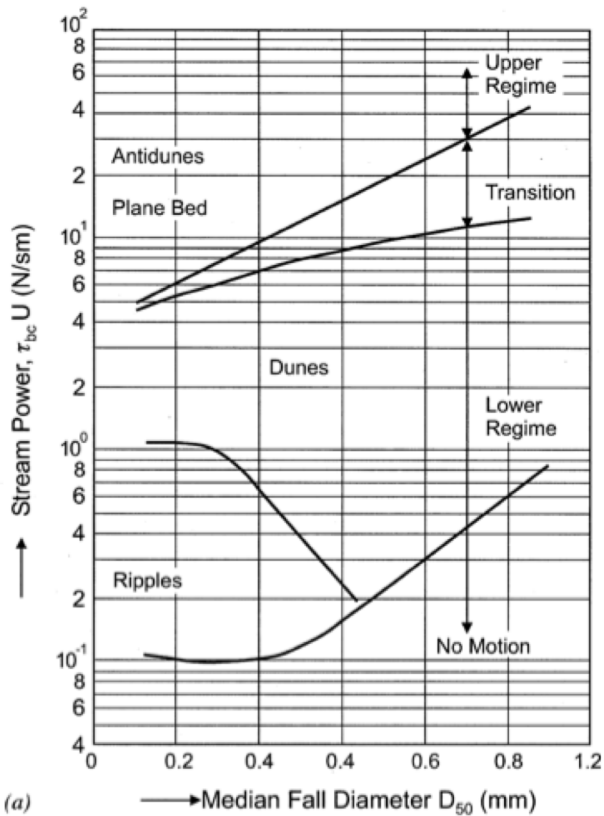
1. Progression of bed forms

- At some point, the velocity reaches a value near the critical value in the Froude sense.
- Near this point, the dunes are often suddenly and dramatically washed out.
- This results in a flat bed known as an “***upper regime***” (supercritical) flat bed.
- Further increases in velocity lead to the formation of anti dunes and finally to the chute and pool pattern. The last of these is characterized by a series of hydraulic jumps.
- In the case of a bed coarser than 0.5mm, the ripple regime is replaced by a zone characterized by a “***lower-regime***” (subcritical) flat bed.



1. Regimes

(a) Simons and Richardson (1966) (b) Boguchwal and Soutard (1990)





1. Progression of bed forms

- The effect of bedforms on flow resistance can be explained as follows. As noted earlier for equilibrium flows in wide straight channels, the relation for bed resistance can be expressed in the form

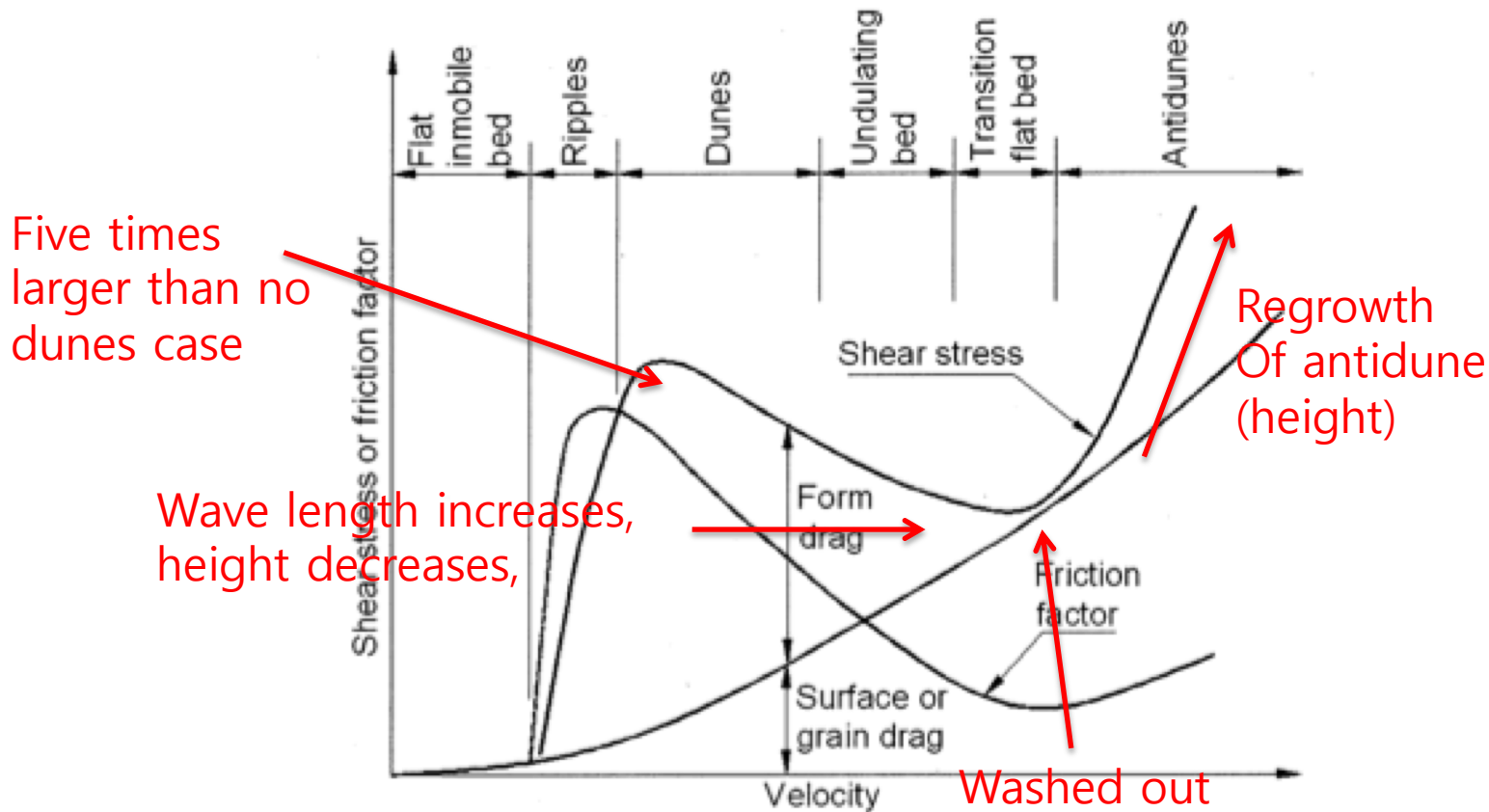
$$\tau_b = \rho C_f U^2$$

- The effect of bedforms is to increase the bed shear stresses to values often well above that associated with the skin friction of a rough bed alone.
- At very low values of U , the parabolic law is followed.
- As ripples and then dunes are formed, the bed shear stress rises to a maximum value.



2. Variations of bed shear to mean velocity

- Over the given erodible bed (Raudkivi, 1990)





3. Dimensionless characterization of bedform regime

- Discussion so far, we can conclude that there are three important parameters describing bed forms

Shields stress : τ^*

Shear Reynolds number : $R_p = \frac{u_* D}{\nu}$

Froude number : $F = \frac{U}{\sqrt{gH}}$

- Parker and Anderson have shown that equilibrium relations of sediment transport for uniform material in a straight channel can be expressed in terms of just two dimensionless hydraulic parameters. (R and R_{ep})



3. Dimensionless characterization of bedform regime

- Density difference and a particle Reynolds number

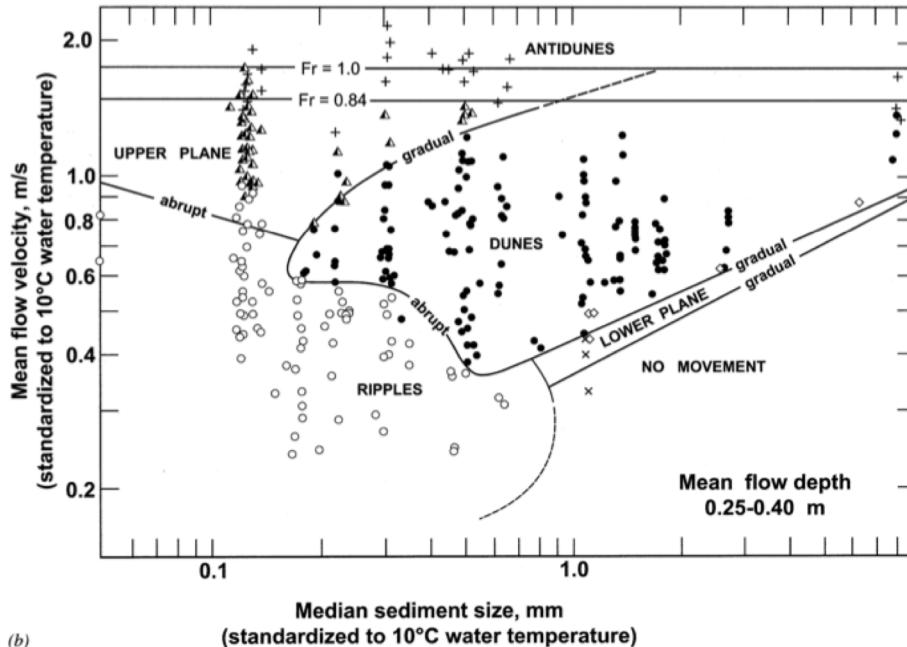
$$R_{ep} = \frac{\sqrt{gRDD}}{\nu} \quad R = \frac{\rho_s - \rho}{\rho}$$

$$\text{Bedform type} = f(\pi_1, \pi_2; R_{ep}, R)$$

π_1 and π_2 can be replaced τ^* and F with S , and H / D



3. Dimensionless characterization of bedform regime



(b)

- Finer particles can be washed out when velocity is high and change abruptly to upper regime from ripples

- It means that finer particles cannot have dune regime.

- When $F < 1$, regime shift depends on the sediment size pretty much.



3. Dimensionless characterization of bedform regime

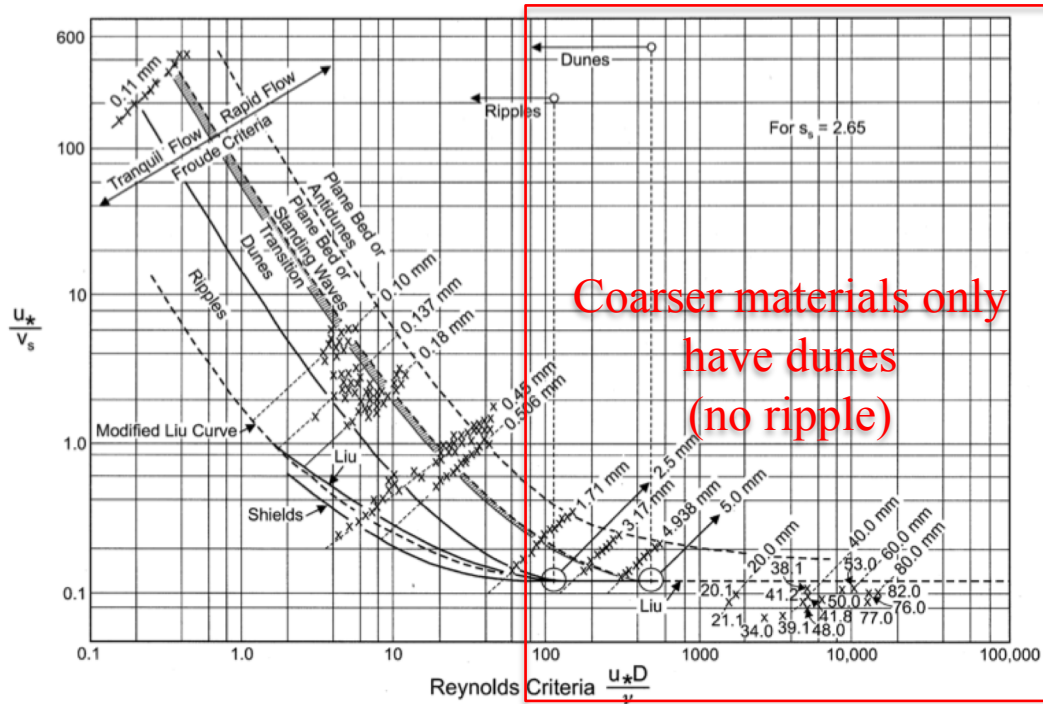
- The discriminator due to Liu (1957) (check the figure in the next slide) uses one dimensionless hydraulic parameter

$$\frac{u_*}{v_s} \text{ (a surrogate of } \tau^* \text{) vs. } R_{ep}$$

- The diagram is of interest in that it covers sizes much coarser.
 - The various regimes become compressed as grain size increases
 - For the case of very coarse material, the flow must be supercritical for any motion to occur. As a result, neither ripples or dunes are to be expected.



3. Dimensionless characterization of bedform regime



- In fact, dunes can occur over a limited in the case of coarse material.
- For coarser grain sizes, the dune regime is preceded by a fairly wide range consisting of lower-regime flat bed.
- Many gravel-bed rivers never leave this lower-regime flat bed region, even at bankfull flow.



4. Effects of bed forms on river stage

- The presence or absence of bed forms on the bed of a river can lead to curious effects on river stage.
- According to the standard Manning-type relation for a non-erodible bed, the following should hold

$$U = \frac{1}{n} H^{2/3} S^{1/2}$$

- Channel is wide enough to allow the hydraulic radius to be replaced with the depth H .
- Depth increases with increasing velocity (but only in rigid bottom).



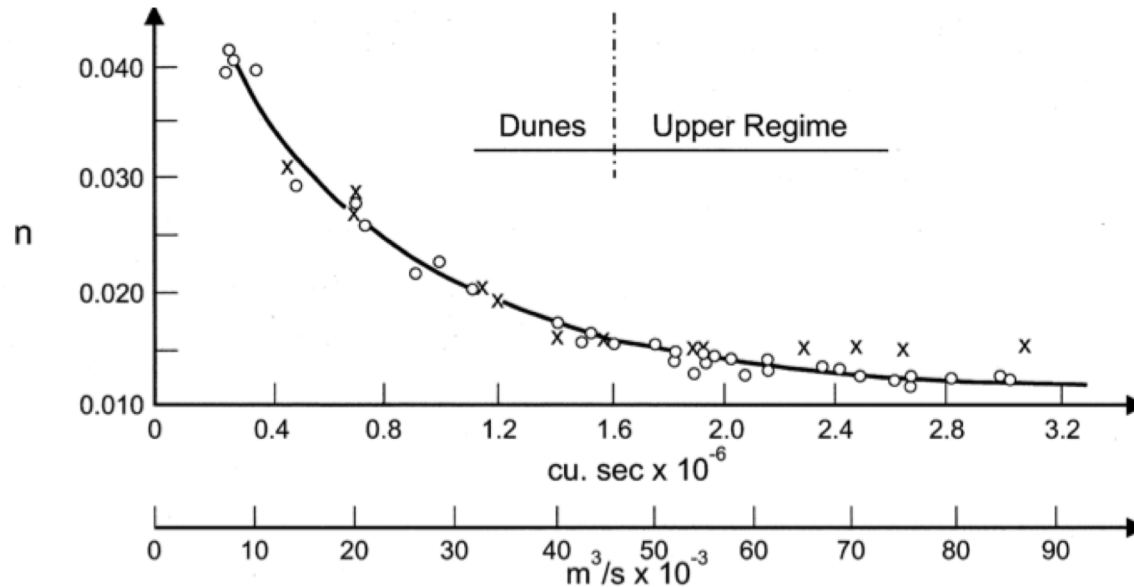
4. Effects of bed forms on river stage

- In a sand-bed stream, resistance decreases as U increases over a wide range of conditions (wiping out ripple etc).
- At equilibrium,

$$\tau_b = \rho C_f U^2 = \rho g H S$$
- This decrease in resistance implies that depth does not increase as rapidly in U in a movable-bed stream.
- In fact, as the transition to upper regime quite suddenly, resulting in a dramatic decrease in resistance.
- The actual result can be an actual decrease in depth as velocity increases.



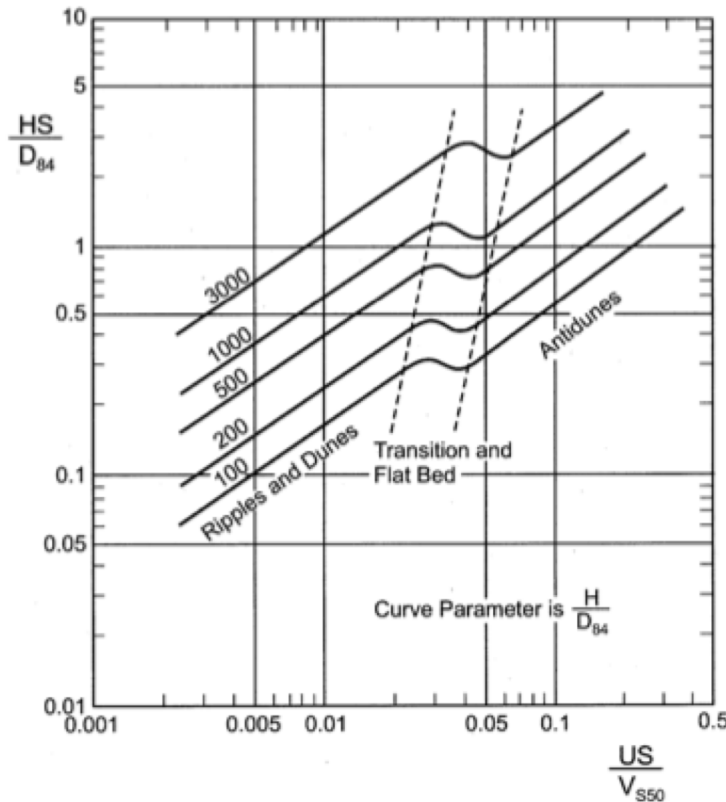
4. Effects of bed forms on river stage



- The above plot shows how Manning's n decreases as the flow discharge increases and the dunes are first elongated and finally washed out
- O : observations (Stevens and Simmons), x : computations. (Chollet and Cunge, 1980)
- Numerical model overestimate in the upper regime where most of the flow resistance should be mainly due to grain friction.



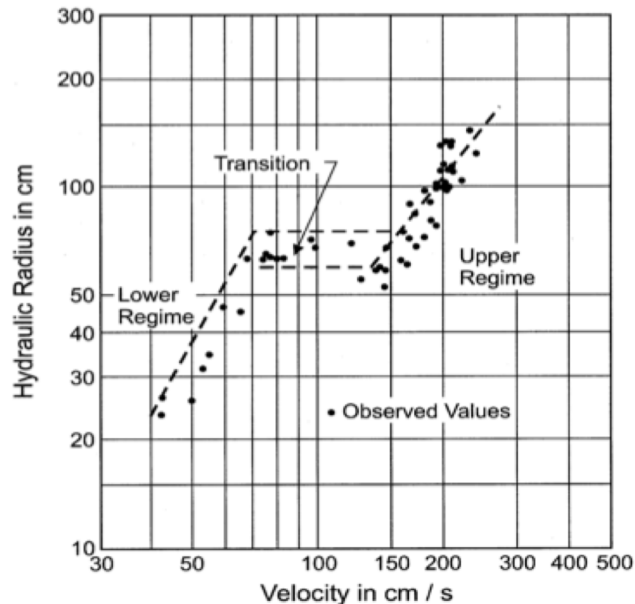
4. Effects of bed forms on river stage



- The effect of the transition phenomenon on flow-stage discharge
 - Illustrated with a flow resistance diagram (Cruickshank and Maza, 1973)
 - Flume and river data were used to develop this dimensionless diagram showing the transition from the lower regime to the upper regime.
 - In the transition region the flow depth is seen to decrease as the flow velocity increases.



4. Effects of bed forms on river stage



- State – discharge relationship
 - Rio Grande, New Mexico
 - Cruickshank-Maza relations capture the behavior of the hydraulic radius,
 - which increase with flow velocity along the lower regime (ripples and dunes), remains almost constant for a wide range of flow velocities during the transition
 - and continues to increase again in the upper regime due to the development of antidunes.

- Double values state-discharge
 - The discharge at which the dunes are obliterated is a little below bank-full in sand-bed streams with medium to high bed slopes.
 - As a result, flooding is not as severe as it would be otherwise.
 - The precise point of transition is generally different depending on whether the discharge is increasing or decreasing.
- Temperature also control the transition to dunes or vice versa.