

"Phase Transformation in Materials"

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Contents for previous class

Solidification: Liquid --> Solid

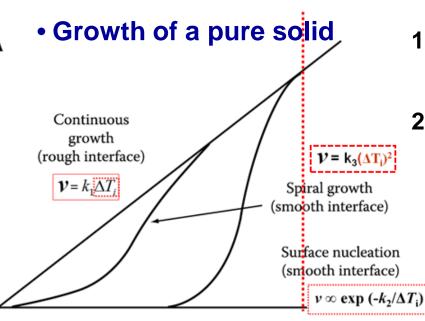
< Nucleation > & < Growth >

• Equilibrium Shape and Interface Structure on an Atomic Scale

 singular (smooth) interface
 rough interface

 Thermal Roughening
 Image: Comparison of the second s

Heating up to the roughening transition.



Growth rate, ν

1) Continuous growth

: Atomically rough or diffuse interface

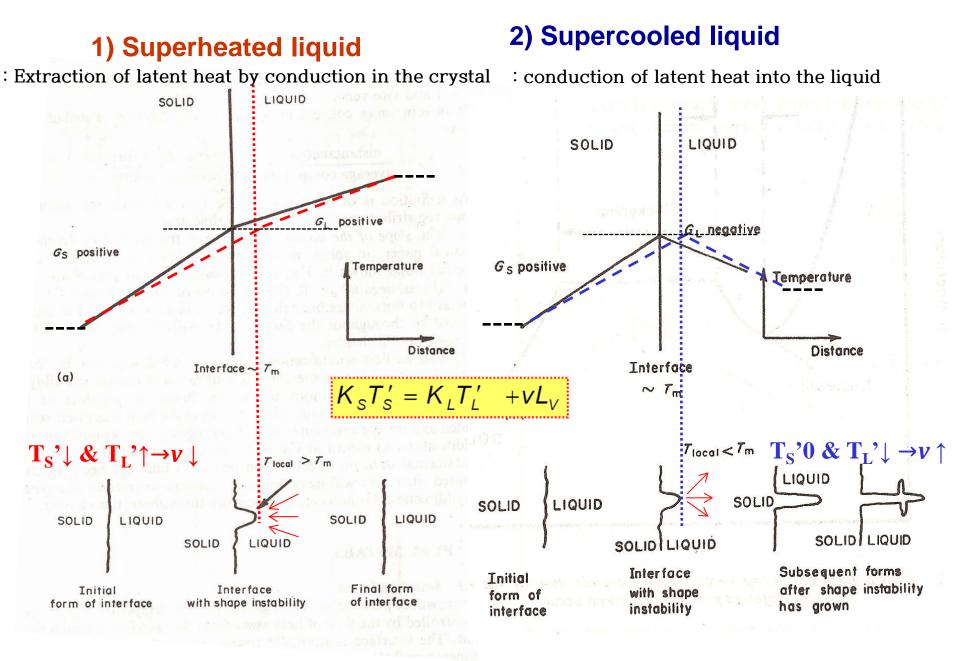
2) Lateral growth

- : Atomically flat of sharply defined interface
- a) Surface (2-D) nucleation b) Spiral growth

Kinetic roughening

When the growth rate of the singular Interface is high enough, it follows the ideal growth rate like a rough interface.

"Removal of latent heat" → Heat Flow and Interface Stability



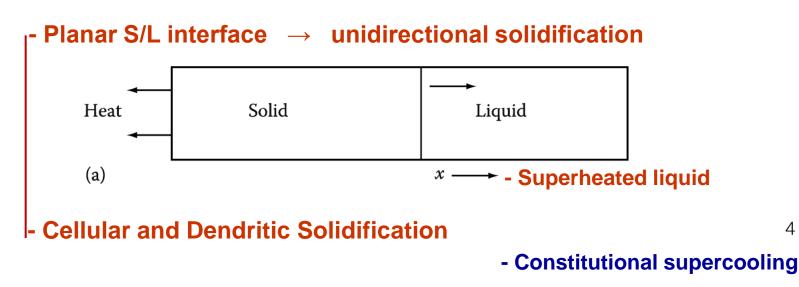
Q: Alloy solidification?

- 1. Solidification of single-phase alloys
- Three limiting cases

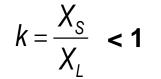
1) Equilibrium Solidification: perfect mixing in solid and liquid

2) No Diffusion in Solid, Perfect Mixing in Liquid

3) No Diffusion on Solid, Diffusional Mixing in the Liquid



1. Solidification of single-phase alloys



k : partition coefficient *X* : mole fraction of solute

In this phase diagram of straight solidus and liquidus, *k* is const. (independent of *T*).

Fig. 4.19 A hypothetical phase diagram. T $k = X_s/X_L$ is constant. T_1 $X_{\rm L}$ T_2 X_{S} Liquidus T_3 Soliping $T_{\rm E}$ kX_0 X_{\max} X_{Solute} X_0 $\frac{X_0}{k}$ $X_{\rm E}$ Heat Solid Liquid (a) \mathbf{x} .

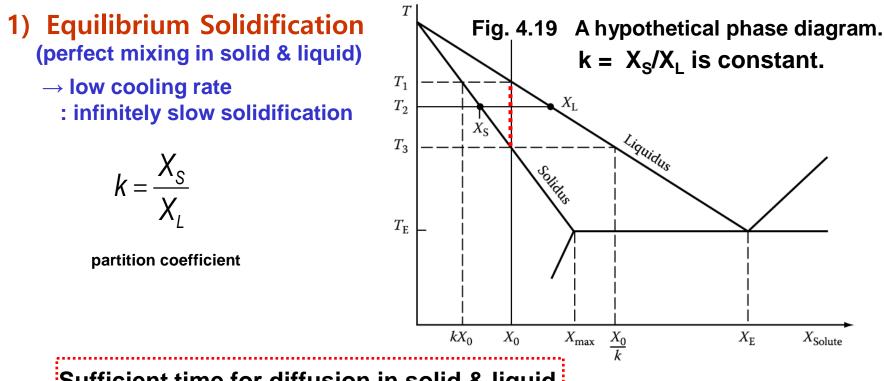
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Planar S/L interface \rightarrow unidirectional solidification ^{Heat}

1. Solidification of single-phase alloys

Three limiting cases

- 1) Equilibrium Solidification (perfect mixing in solid & liquid)
- 2) No Diffusion in Solid, Perfect Mixing in Liquid
- 3) No Diffusion on Solid, Diffusional Mixing in the Liquid



- Sufficient time for diffusion in solid & liquid
- Relative amount of solid and liquid : lever rule
- Solidification starts at $T_1 (X_s = kX_0)$ and ends at $T_3 (X_L = X_0/k)$.

Composition vs x at T_2

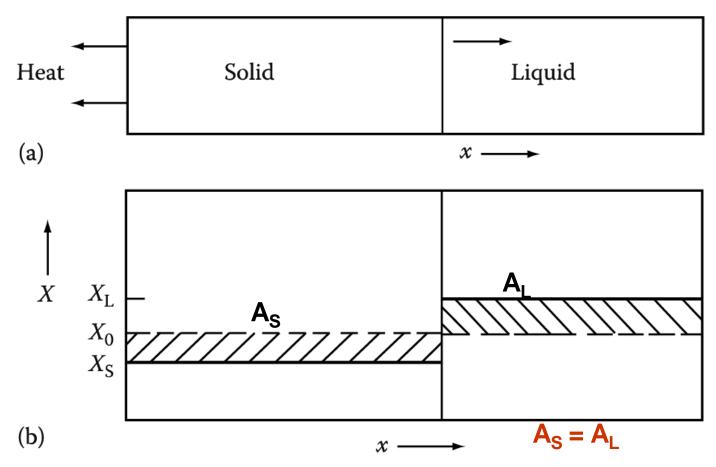
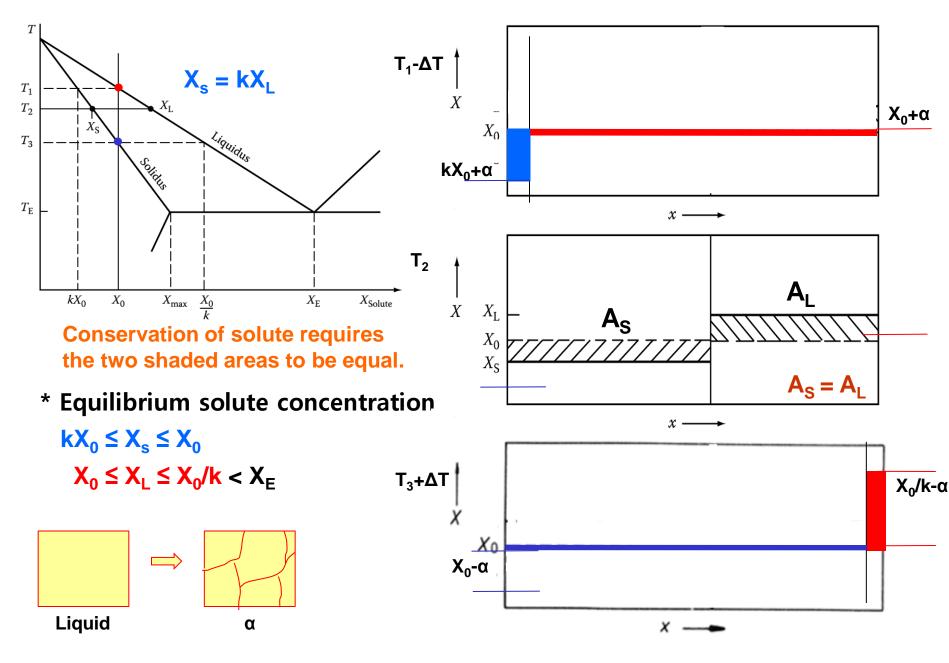


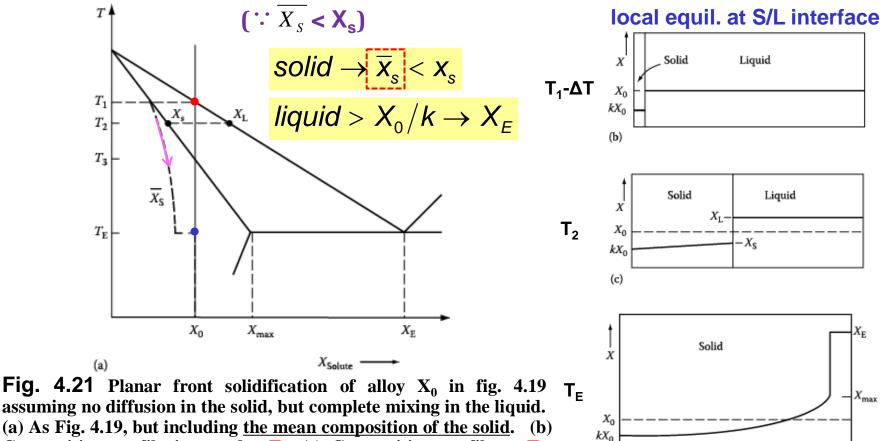
Fig. 4.20 Unidirectional solidification of alloy X_0 in Fig. 4.19. (a) A planar S/L interface and axial heat flow. (b) Corresponding composition profile at T_2 assuming complete equilibrium. Conservation of solute requires the two shaded areas to be equal. $A_s = A_L$

1) Equilibrium Solidification : perfect mixing in solid and liquid



2) Non-equilibrium Solidification: No Diffusion in Solid, Perfect Mixing in Liquid

- : high cooling rate, efficient stirring
- Separate layers of solid retain their original compositions mean comp. of the solid ($\overline{X_s}$) < X_s
- Liquid become richer than $X_0/K \rightarrow X_E$ at the last part of solidification.
- Variation of $X_s :$ solute rejected to the liquid \rightarrow solute increase in the liquid



(d) 0

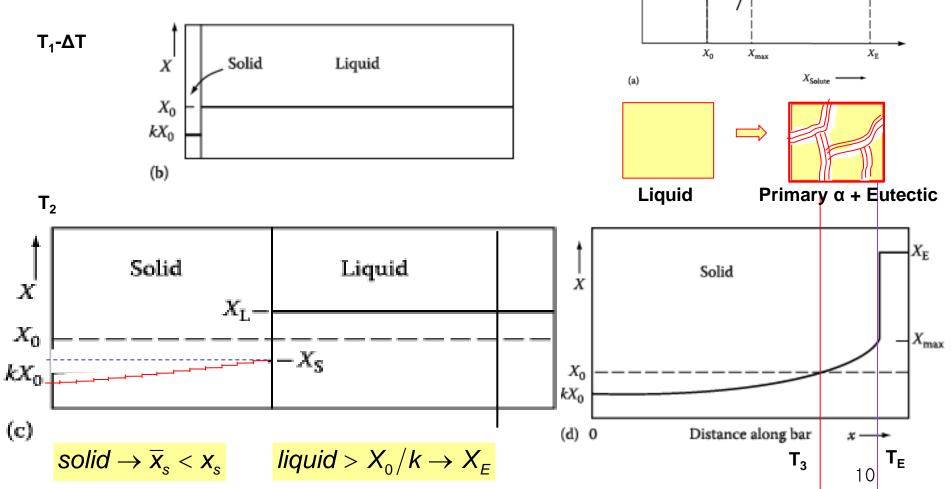
Distance along bar

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(a) As Fig. 4.19, but including the mean composition of the solid. (b) Composition profile just under T_1 . (c) Composition profile at T_2 (compare with the profile and fraction solidified in Fig.4.20b) (d) Composition profile at the eutectic temperature and below.

2) No Diffusion in Solid, Perfect Mixing in Liquid

- : high cooling rate, efficient stirring
 - Separate layers of solid retain their original compositions
 - mean comp. of the solid ($\overline{X_s}$) < X_s



Τ

 T_1

 T_2

 T_3

 \overline{X}_{S}

L

 X_L

Mass balance: non-equilibrium lever rule (coring structure)

When cooled by dT from any arbitrary T, determine the followings.

Ignore the difference in molar volume T_{E} between the solid and liquid.

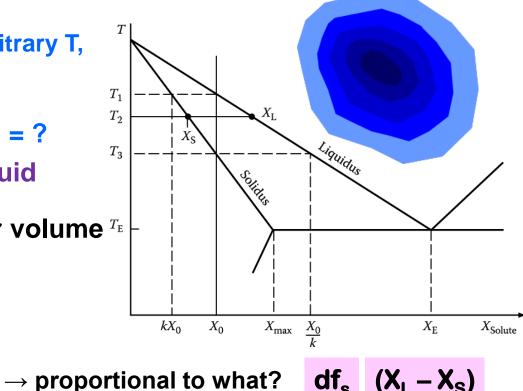
f_s: volume fraction solidified

solute ejected into the liquid=? solute increase in the liquid=?

$$(X_L - X_S)df_S = (1 - f_S)dX_L$$

when
$$f_{S}$$
 = 0 \rightarrow X_{S}, X_{L}?

Initial conditions



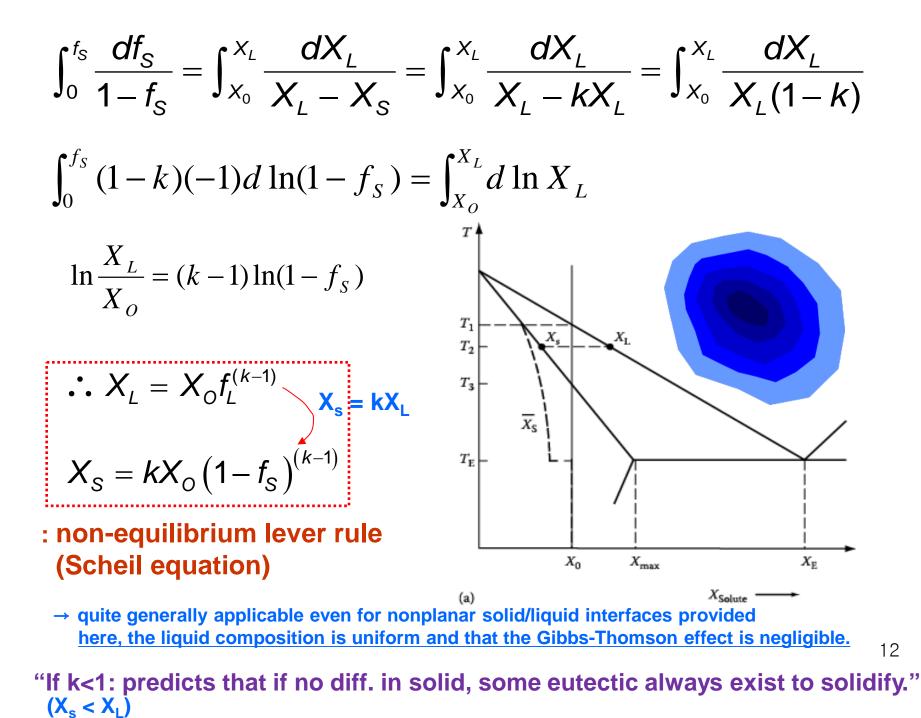
 \rightarrow proportional to what?

 $\frac{df_s}{(1-f_s)} \frac{(X_L - X_S)}{dX_L}$

Solve this equation.

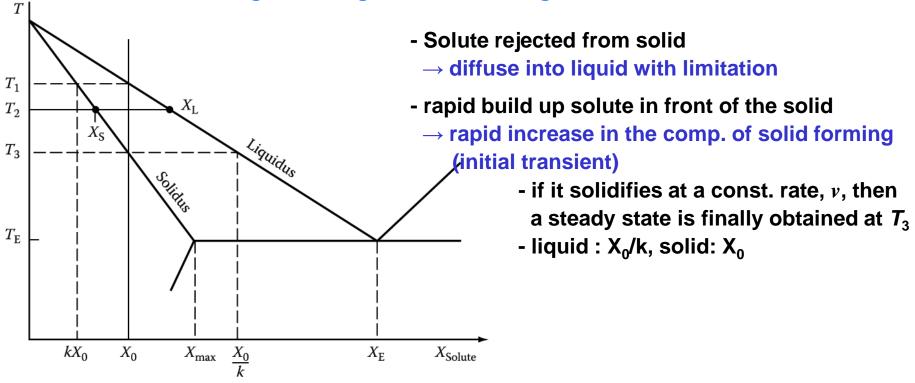
$$X_{S} = kX_{0}$$
 and $X_{L} = X_{0}$

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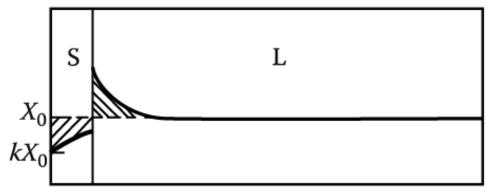


3) No Diffusion on Solid, Diffusional Mixing in the Liquid

: high cooling rate, no stirring -> diffusion

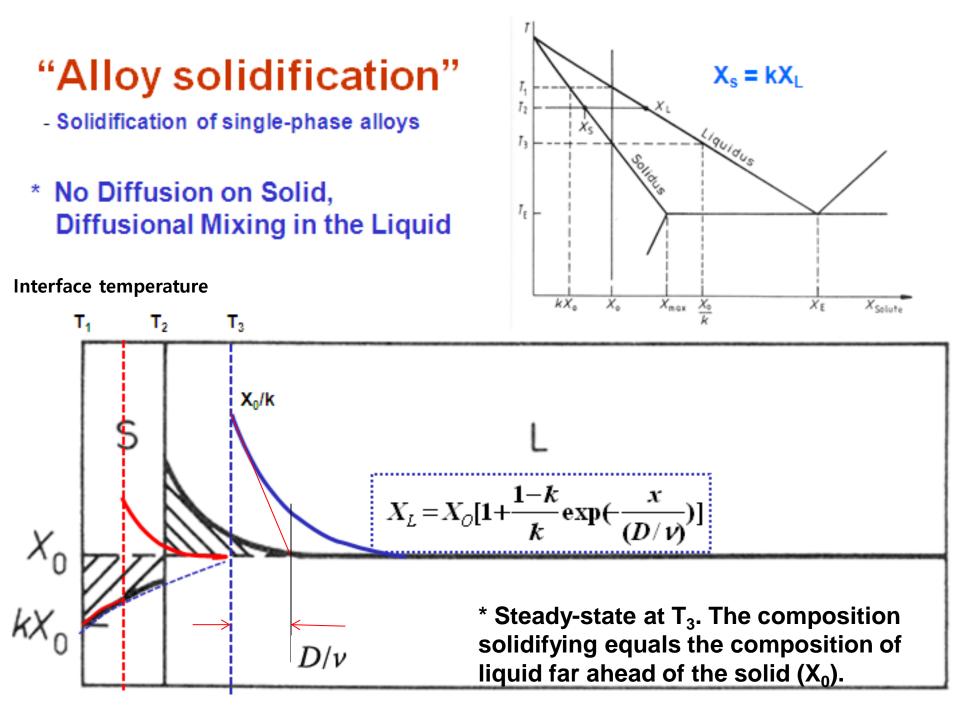






Composition profile at $T_2 < T_{S/L} < T_3$?

Steady-state profile at T_3 ? at T_E or below?



No Diffusion on Solid, Diffusional Mixing in the Liquid

During steady-state growth,

(Interface →liquid: Diffusion rate)

Rate at which solute diffuses down the concentration gradient away from the interface = Rate at which solute is rejected from the solidifying liquid

(Liquid→Solid: solute rejecting rate)

Set up the equation.

$$J = DC_L' = v(C_L - C_S)$$

$$J = -D\frac{\partial X_L}{\partial x} = v(X_L - X_S)$$

(Solidification rate of alloy: excess solute control)

$$\mathbf{K}_{S}T'_{S} = \mathbf{K}_{L}T'_{L} + \mathbf{V}L_{V}$$

(Solidification rate of pure metal: latent heat control, 10⁴ times faster than that of alloy)

Solve this equation.

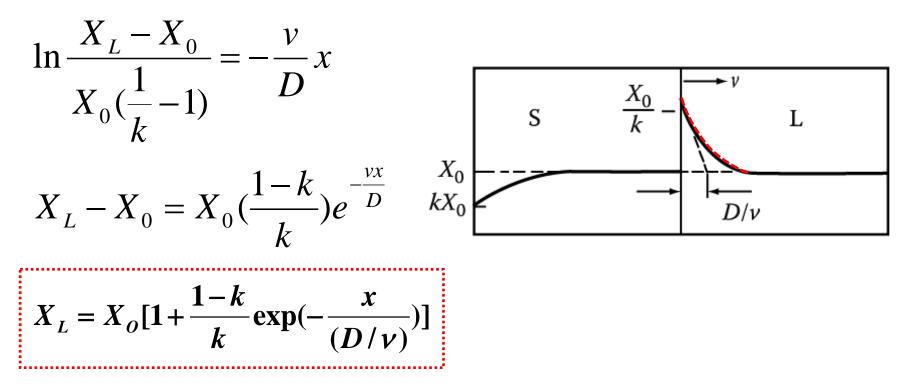
 $X_s = X_0$ for all $x \ge 0$ steady-state

$$\frac{dX_L}{X_L - X_0} = -\frac{v}{D}dx$$

$$\ln(X_L - X_0) = -\frac{v}{D}x + c$$

$$x = 0; X_L = X_0 / k$$
 steady-state

$$c = \ln(\frac{X_0}{k} - X_0)$$



(X_L decreases exponentially from X_0/k at x=0, the interface, to X_0 at large distances from the interface. The concentration profile has a characteristic width of D/v.)

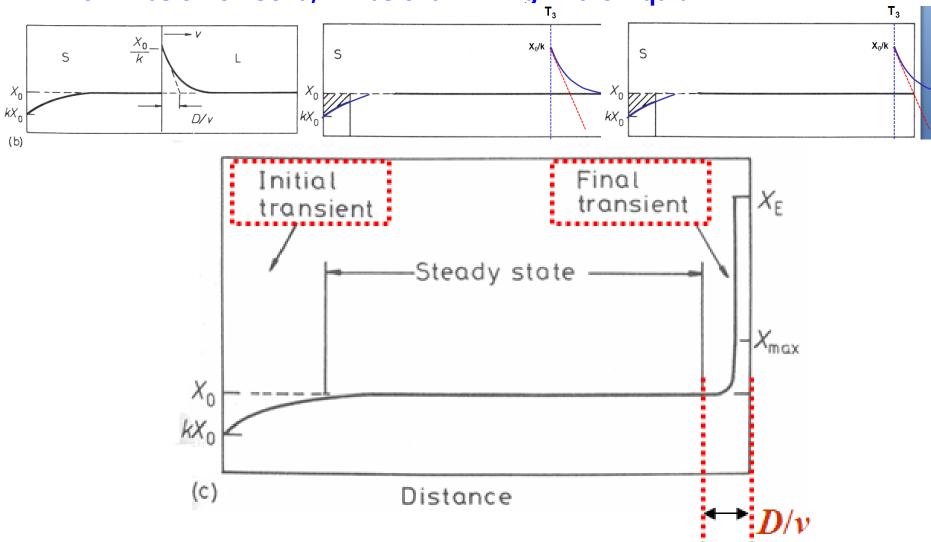
- The concentration gradient in liquid in contact with the solid :

$$J = -DX'_{L} = v(X_{L} - X_{S}) \qquad X'_{L} = -\frac{X_{L} - X_{S}}{D/v}$$

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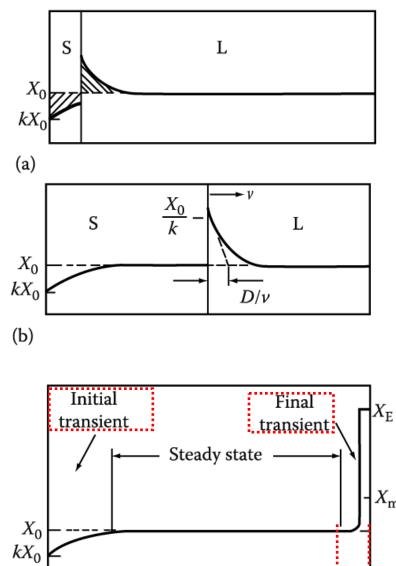
"Alloy solidification" - Solidification of single-phase alloys

* No Diffusion on Solid, Diffusional Mixing in the Liquid



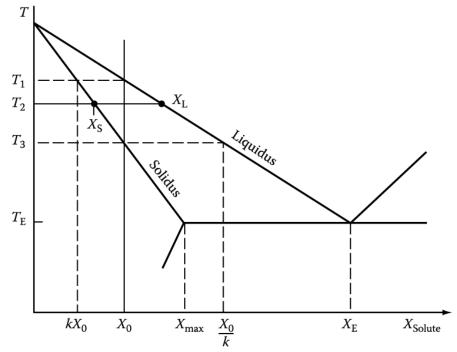
When the solid/liquid interface is within ~D/v of the end of the bar the bow-wave of solute is compressed into a very small volume and the interface composition rises rapidly leading to a final transient and eutectic formation.

No Diffusion on Solid, Diffusional Mixing in the Liquid

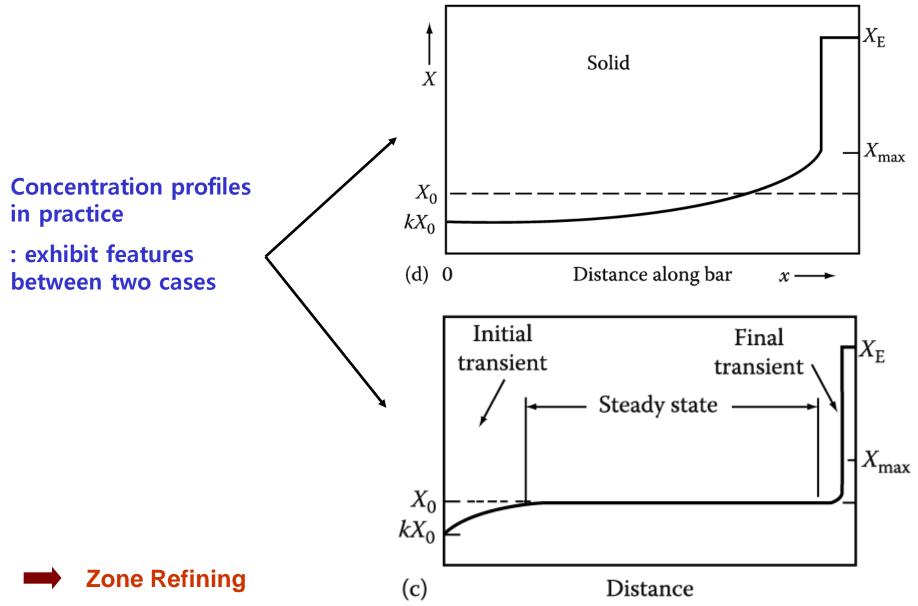


Distance

(c)



- Fig. 4.22 Planar front solidification of alloy X₀ in Fig. 4.19 assuming no diffusion in solid and no stirring in the liquid.
- (a) Composition profile when S/L temperature is between T_2 and T_3 in Fig. 4.19.
- χ_{ma} (b) Steady-state at T₃. The composition solidifying equals the composition of liquid far ahead of the solid (X_0) .
- Composition profile at T_E and below, showing (C) the final transient. D/v

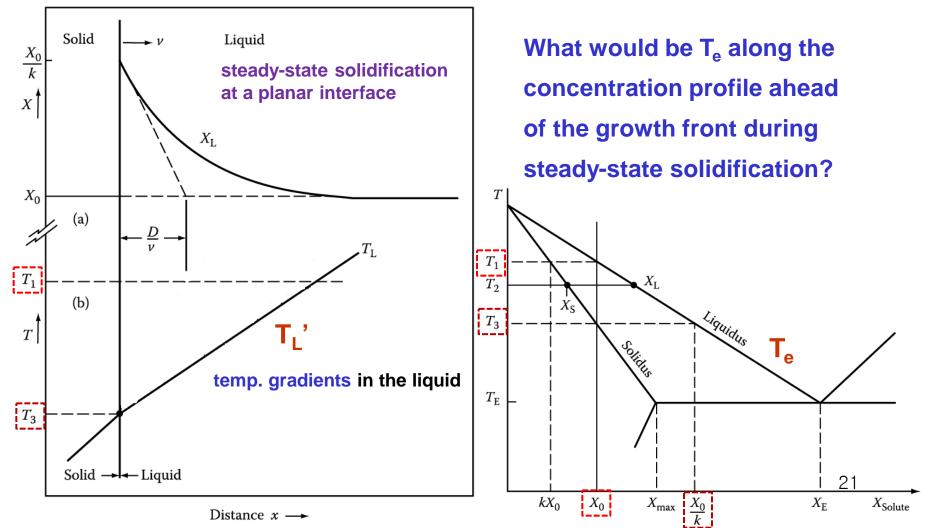


Q: Cellular and Dendritic Solidification by "constitutional supercooling" in alloy

2. Cellular and Dendritic Solidification

Fast Solute diffusion similar to the conduction of latent heat in pure metal, possible to break up the planar front into dendrites.

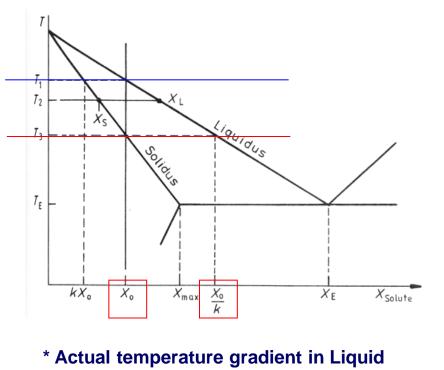
 \rightarrow complicated, however, by the possibility of temp. gradients in the liquid.



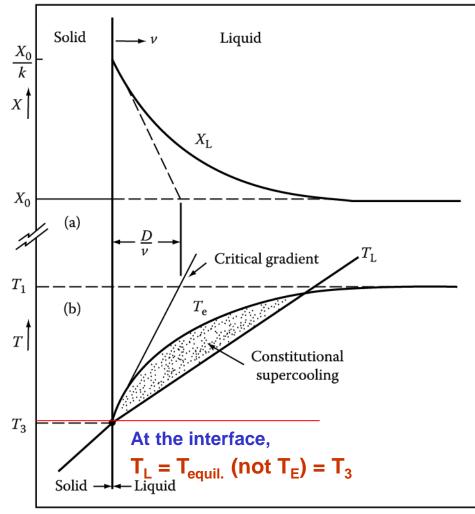
* Constitutional Supercooling

No Diffusion on Solid, Diffusional Mixing in the Liquid

Steady State



T_L' * equilibrium solidification temp. change T_{equil.}



Distance $x \rightarrow$

 $T_L' > (T_1 - T_3)/(D/v)$: the protrusion melts back \rightarrow Planar interface: stable $T_L' /v < (T_1 - T_3)/D$: Constitutional supercooling \rightarrow cellular/ dendritic growth22

Q: Planer → Cell structure → Dendrite?

by constitutional supercooling in superheated liquid

If temperature gradient ahead of an initially planar interface is gradually reduced below the critical value, (constitutional supercooling at solid/liquid interface)

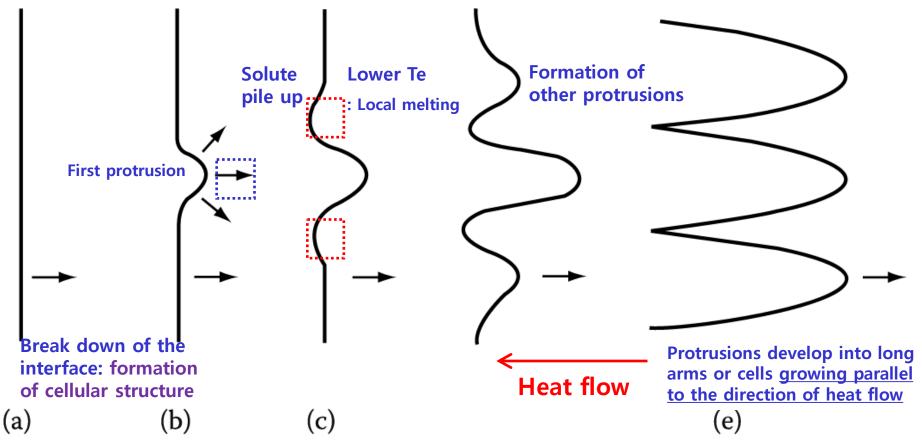
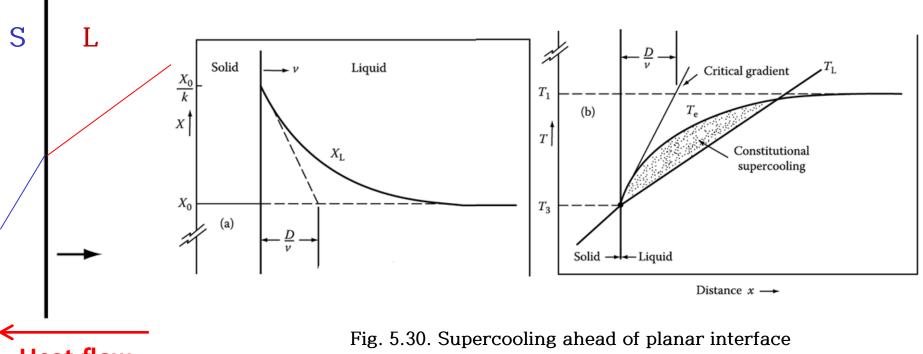


Fig. 4.24 The breakdown of an initially planar solidification front into cells

If temperature gradient ahead of an initially planar interface is gradually reduced below the critical value, (constitutional supercooling at solid/liquid interface)

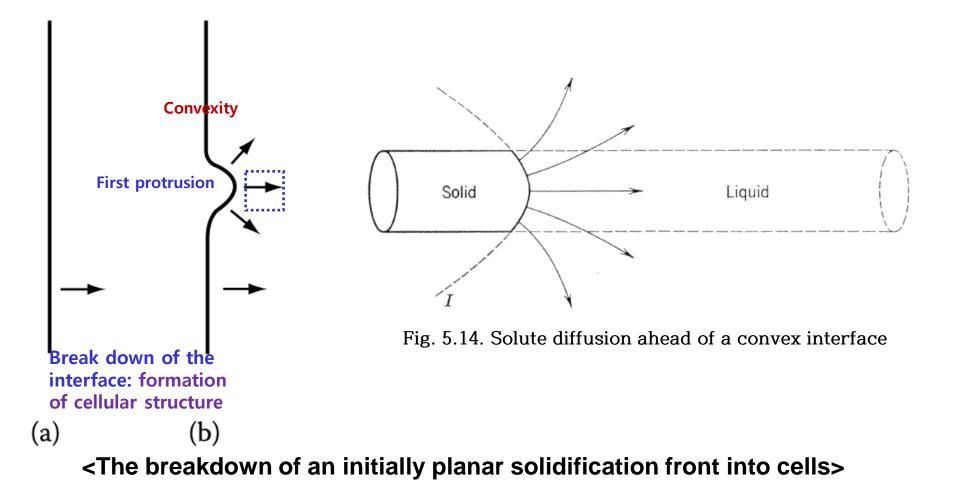


Heat flow

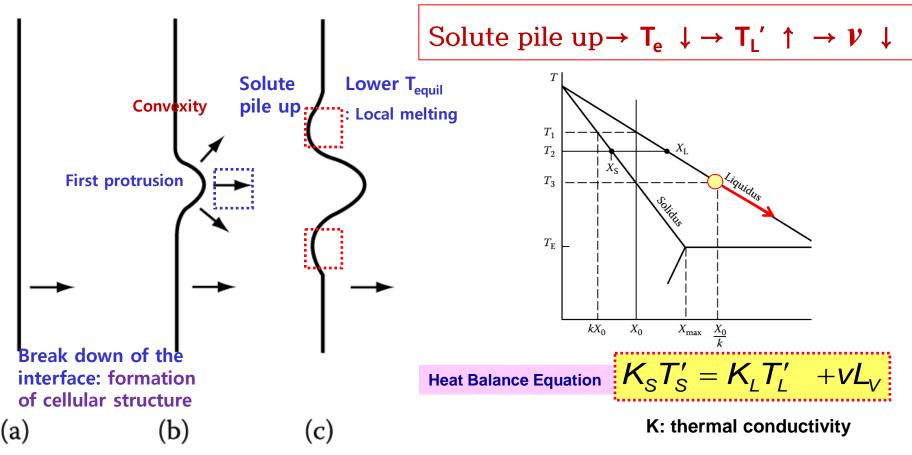
(a)

<The breakdown of an initially planar solidification front into cells>

If temperature gradient ahead of an initially planar interface is gradually reduced below the critical value, (constitutional supercooling at solid/liquid interface)

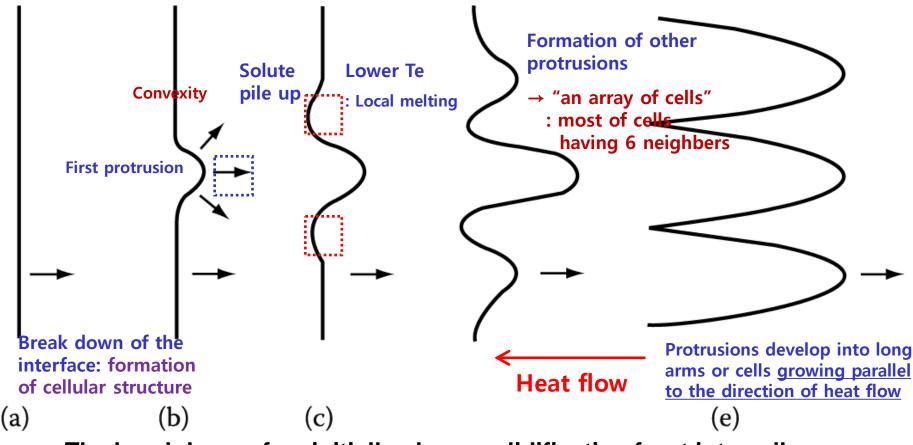


If temperature gradient ahead of an initially planar interface is gradually reduced below the critical value, (constitutional supercooling at solid/liquid interface)



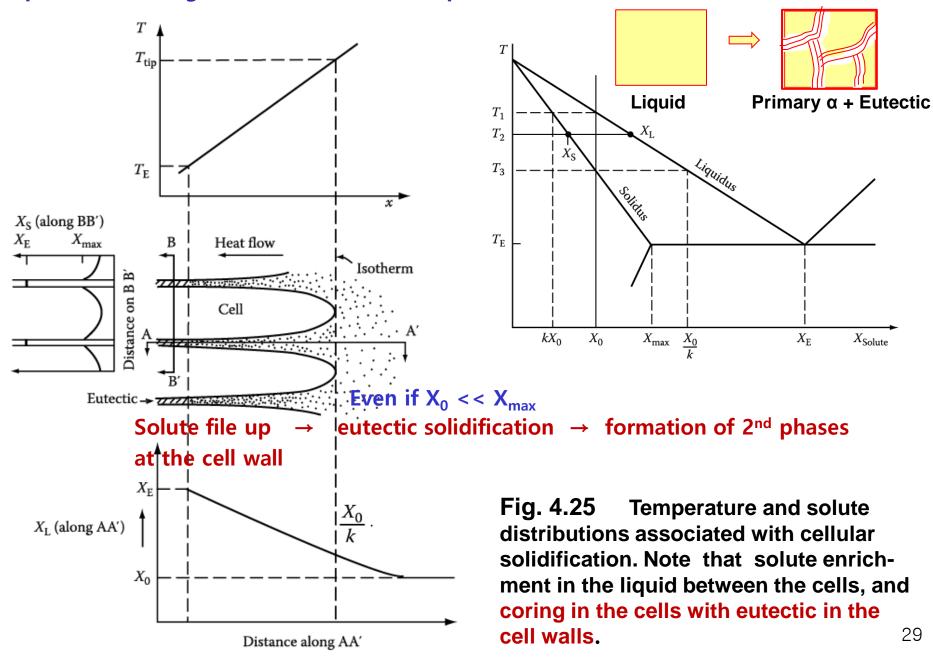
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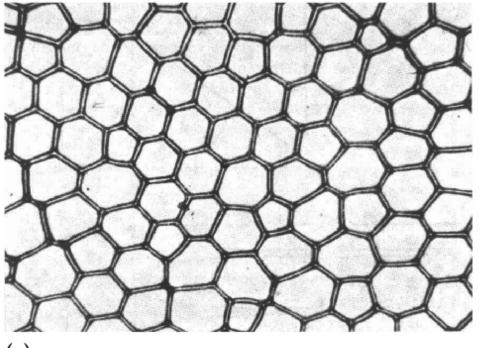
If temperature gradient ahead of an initially planar interface is gradually reduced below the critical value, (constitutional supercooling at solid/liquid interface)

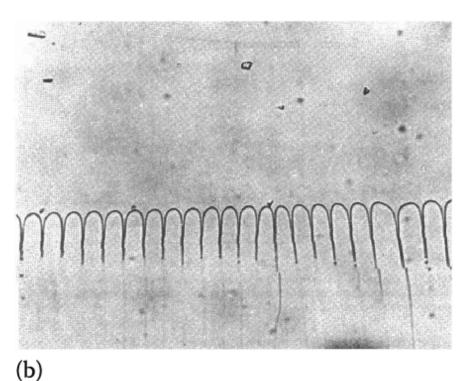


<The breakdown of an initially planar solidification front into cells>

Tips of the cells grow into the hottest liquid and therefore contain the least solute.







30

(a)

* Cellular microstructures

Note that each cell has virtually the same orientation as its neighbors and together they form a single grain.

- (a) A decanted interface of a cellularly solidified Pb-Sn alloy (x 120)
 (after J.W. Rutter in Liquid Metals and Solidification, American Society for Metals, 1958, p. 243).
- (b) Longitudinal view of cells in carbon tetrabromide (x 100) (after K.A. Jackson and J.D. Hunt, Acta Metallurgica 13 (1965) 1212).

Temp. and solute distributions associated with cellular solidification. 1) Note that solute enrichment in the liquid between the cells, and Т coring in the cells with eutectic in the cell walls. T_{tip} T_1 T_2 $X_{\rm L}$ X_{S} T_E Liquidus T_3 Solipinz х $X_{\rm S}$ (along BB') $X_{\rm E}$ X_{max} Heat flow $T_{\rm E}$ Isotherm on B B **T**₁ Cell stance kX_0 X_0 $X_{\max} \quad \underline{X_0}$ $X_{\rm E}$ X_{Solute} Tips of the cells grow into the Eutectic -> -----2) hottest liquid and therefore contain the least solute. $X_{\rm E}$ 3) Even if $X_0 << X_{max}$ $X_{\rm L}$ (along AA') Solute file up \rightarrow eutectic solidification \rightarrow formation of 2nd phases at the cell wall X_0

Distance along AA'

Liquid

Primary α + Eutectic

31

The change in morphology from cells to dendrites

- * Cellular microstructures are only stable for a certain range of temp. gradients.
- → Sufficiently low temp. gradients → Creation of constitutional supercooling in the liquid between the cells causing interface instabilities in the transverse direction (although, No temp. gradient perpendicular to the growth direction)
- → Develop arms, i.e. dendrites form & Change in the direction of the primary arms away from the direction of heat flow into the crystallographically preferred directions i.e. (100) for cubic metals.

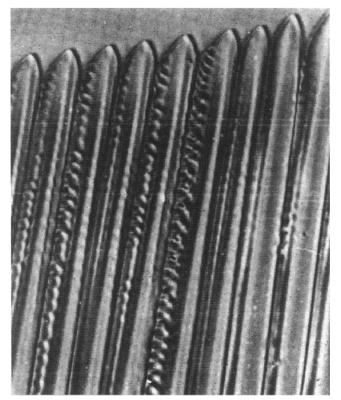


Fig. 4.27 Cellular dendrites in carbon tetrabromide. (After L.R. Morris and W.C. Winegard, Journal of Crystal Growth 6 (1969) 61.)

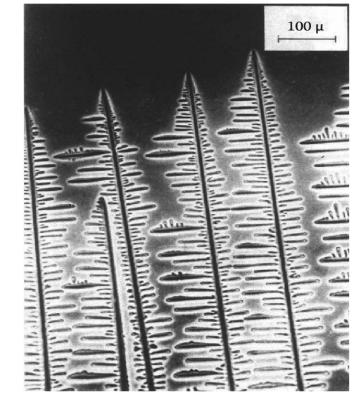


Fig. 4.28 Columnar dendrites in a transparent organic alloy.

(After K.A. Jackson in Solidification, American Society for Metals, 1971, p. 121.)

Cellular and Dendritic Solidification

At the interface, $T_L = T_e$ (not T_E) = $T_3 \rightarrow T_{L, \text{ liquid}} = T_1 : T' = T_1 - T_3$ (superheating)

Criterion for the stable planar interface:

 $T_1' > (T_1 - T_3)/(D/v)$: the protrusion melts back_steeper than the critical gradient (T₁-T₃: Equilibrium freezing range of alloy) $T_1'/v > (T_1-T_3)/D$

 \longrightarrow Large solidification range of T₁-T₃ or high v promotes protrusions.

need to well-controlled experimental conditions (temp. gradient & growth rate)

Constitutional supercooling:

Formation of Cell and Dendrites Structures

Solute effect : addition of a very small fraction of a percent solute with

very small k ($k = \frac{X_s}{X_i}$) \rightarrow (T₁-T₃) \uparrow promotes dendrites.

Cooling rate effect : Higher cooling rate allow less time for lateral diffusion of the rejected solute and therefore require smaller cell or dendrite arm spacings to avoid constitutional supercooling.

Solidification of Pure Metal

: Thermal gradient dominant



Solidification of single phase alloy: Solute redistribution dominant

a) Constitutional supercooling

Planar \rightarrow Cellular growth \rightarrow cellular dendritic growth \rightarrow Free dendritic growth

응고계면에 조성적 과냉의 thin zone 형성에 의함 Dome 형태 선단 / 주변에 hexagonal array T↓→ 조성적 과냉영역 증가 Cell 선단의 피라미드형상/ 가지 들의 square array/ Dendrite 성장방향쪽으로 성장방향 변화 성장하는 crystal로 부터 발생한 <u>잠열을 과냉각 액상쪽으로 방출</u>함 에 의해 형성 Dendrite 성장 방향/ Branched rod-type dendrite

→ "Nucleation of new crystal in liquid" 성장이 일어나는 interface 보다 높은 온도

b) Segregation

: normal segregation, grain boundary segregation, cellular segregation, dendritic segregation, inversegregation, coring and intercrystalline segregation, gravity segregation