

Numerical Models for River Mixing







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- 9.3 River Models
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Objectives

- Introduce concept of river modeling
- Study fundamentals of river hydraulics
- Introduce rivers models and case studies of river modeling





Introduction

Open channel hydraulics (Fixed-bed)

• Analysis of free surface flows

River study



Artificial channel



Lab experiment in fixed-bed



Fluvial hydraulics (Movable-bed, Sediment transport + Geomorphology)

Flow analysis in a river and sediment transport

Sediment transport



River bed change



Lab experiment in moving-bed





River Hydraulics

Environmental hydraulics

Study of flow dynamics in the water body to handle environmental problems by human activities



Ecological hydraulics





Combined study of hydraulics and biological dynamics to understand the ecosystem







River Modeling

Definition

Describe the real system of river dynamics using physical or mathematical approach

Purpose

Understanding and prediction of river dynamics





Modeling Process

Uncertainty

Most models are intermediate forms between physical-based models and empirical models.

Parameter

Model have its own parameters to represent their characteristics.

Calibration

- Comparison of model output with observations to tune the model parameters
 - \rightarrow The calibrated models can be called empirical models

Validation

Comparison of output from the calibrated models with observations to evaluate validity of the calibrated models.







Classification of open channel flow



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Flow resistance
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- Consistently working on the water flow as opposite to drag force
- Geomorphological characteristics on the flow resistance



 Frictional resistance on the boundary between the water flow and bed material and form resistance facing the water flow by the bed forms and obstacles





- Flow resistance
 - Shear stress in uniform flow
 - ~ Flow with constant cross section and slope
 - \rightarrow Uniform flow, $\frac{\partial U}{\partial t} = 0$
 - ~ Hydrostatic assumption $F_1 = F_2$ as opposite direction
 - $\rightarrow F_1 = F_2$
 - ~ Momentum equation about entire water flow

$$\rightarrow \gamma A l \frac{\partial U}{\partial t} = \gamma A l sin\theta - \tau_0 P l$$

~ Flow direction due to gravity parallel to wall shear stress

$$\rightarrow \tau_0 = \gamma \frac{A}{P} \sin\theta = \gamma RS$$





Flow resistance equation – Uniform flow equation

- Calculate uniform flow with geometric characteristics and resistance on the boundary
- Chezy's equation
- ~ Set Darcy Weisbach equation
 - = Shear stress equation

$$\rightarrow \tau_0 = \gamma RS \equiv \left(\frac{f}{8}\right) \rho U^2$$
$$\rightarrow U = C\sqrt{RS}$$

where, f = friction factor,

$$C = Chezy's \text{ coefficient } \left(C = \sqrt{8g/f}\right)$$

Manning's equation

~ Empirical equation from the experimental data to determine *C*

$$\rightarrow C = \frac{R^{1/6}}{n}$$
$$\rightarrow U = \frac{1}{n} R^{2/3} S^{1/2}$$

where, n = Manning's coefficient





Manning's roughness coefficient

~ Average values of *n* proposed by Chow (1959), considering various bed surface conditions

Type of channel and description	Minimum	Normal	Maximum
D. Natural Streams			
D-1. Minor streams (top width < 30.48 m)			
a. Streams on plain			
1. Clean, straight, full stage, no rifts or deep pools	0.025	0.030	0.033
2. Same as above, but more stones and weeds	0.030	0.035	0.040
3. Clean, winding, some pools and shoals	0.033	0.040	0.045
4. Same as above, but some weeds and stones	0.035	0.045	0.050
8. Very weedy reaches, weedy, deep pools floodways with heavy	0.075	0.100	0.15
stand of timber and underbrush			
b. Mountain streams			
1. Bottom: gravels, cobbles, and few boulders	0.030	0.040	0.050
2. Bottom: cobbles with large boulders	0.040	0.050	0.070
D-3. Major streams (top width > 30.48 m)			
a. Regular section with no boulders or brush	0.025		0.060
b. Irregular and rough section	0.035		0.100

Ref.: Chow (1959)

Estimation of roughness coefficient in the open channel (USGS, 1989)

~ Cowan's equation (1956)

$$n = (n_b + n_1 + n_2 + n_3 + n_4)m$$

where, n_b = Bed material

- n_1 = Irregularity
- n_2 = Cross-sectional shape
- $n_3 = \text{Obstructions}$
- n_4 = Vegetation
- m = Channel meandering





Gradually-varied flow

Derivation



- Calculation of the water surface curve with the standard step method
 - Solve unknowns in the non-linear equation, apply the energy equation into upstream and downstream of the channel with the trial & error method or numerical analysis
 - Trial & error method commonly used for water surface curve in rivers (ex. HEC-RAS)



Trial & error method $H_1 = H_2 + \frac{1}{2}(S_{f1} + S_{f2})\Delta x$

Solve **unknown total energy** (H_1) of the upstream using **total energy** (H_2) of the downstream and assuming **unknown water elevation** (y_1) of the upstream

Numerical analysis					
$f(y_1) = y_1 + \alpha_1 \frac{Q^2}{2gA_1^2} - \frac{1}{2}\Delta x S_{f1}$					
+ $\left(z_1 - z_2 - y_2 - \alpha_2 \frac{Q^2}{2gA_2^2} - \alpha_2 \frac{Q^2}{2gA_2^2}\right)$	$\left(-\frac{1}{2}\Delta x S_{f^2}\right) = 0$				

Solve the non-linear equation about **unknown water depth** (y₁) of the upstream using **bisection method** or **Newton method**



Unsteady flow

Derivation



 $F_2 = \gamma h_c A + \frac{\partial}{\partial x} (\gamma h_c A) \Delta x$

Applying Newton's second law into the control volume

$$\Sigma F = ma = \rho A \Delta x \frac{dV}{dt} = \rho A \Delta x \left[\frac{\partial V}{\partial t} + V \frac{\partial V}{\partial x} \right]$$

$$F_1 - F_2 + W \sin \alpha - \tau_0 p \Delta x = \rho A \Delta x \left[\frac{\partial V}{\partial t} + V \frac{\partial V}{\partial x} \right]$$

$$\implies \frac{\partial Q}{\partial t} + \frac{\partial (VQ)}{\partial x} + g A \left(\frac{\partial z}{\partial x} + S_f \right) = 0 \quad \text{(St.Venant Equation)}$$

1-D models for unsteady flow analysis

HEC-RAS US Army Corps o Engineers	 Widely used in international research institutes Compatible with evaluation of various hydraulic structures
g	
SWMM US EPA	 Developed for rainfall-runoff in urban areas Effective in pipe flow analysis considering hydrological properties
MIKE 11 DHI	 Commercial software for flood simulations Hydrodynamic and water quality simulation with user-friendly GUI



2. River Hydraulics Shallow Water Hydraulics

Shallow water equation

Time-averaged Navier-Stokes equation

 $\frac{\partial \overline{u_i}}{\partial t} + \overline{u_j} \frac{\partial \overline{u_i}}{\partial x_j} + \frac{\partial \overline{u_i' u_j'}}{\partial x_j} = -\frac{1}{\overline{\rho}} \frac{\partial \overline{p}}{\partial x_i} - g \delta_i + v_L \frac{\partial^2 \overline{u_i}}{\partial x_j \partial x_j}$

Depth-averaging the 3-D Navier-Stokes equation with hydrostatic assumption

$$\frac{\partial u_i}{\partial t} + u_j \frac{\partial u_i}{\partial x_j} = -\frac{1}{\rho_0} \frac{\partial p_a}{\partial x_i} - g \frac{\partial (H+h)}{\partial x_i} - \frac{g}{\rho_0} \frac{\partial}{\partial x_i} \int_z^{H+h} \rho' dz - g \delta_{3i} + (v_L + v_T) \frac{\partial^2 u_i}{\partial x_j \partial x_j} + v_T \frac{\partial}{\partial x_j} \left(\frac{\partial u_j}{\partial x_i} \right)$$

(Bottom: $z = H(x, y)$ Surface: $z = H + h(x, y, t)$)

Applying the kinematic free surface condition and non-slip boundary on the bottom





2. River Hydraulics Shallow Water Hydraulics

Turbulence modeling

Hydrodynamic model - RANS(Reynolds Averaged Navier-Stokes Equation)

$$\frac{\partial \overline{u_i}}{\partial t} + \overline{u_j} \frac{\partial \overline{u_i}}{\partial x_j} = -\frac{1}{\rho} \frac{\partial \overline{p}}{\partial x_i} + g_i + \frac{\partial}{\partial x_j} \left[\nu \left(\frac{\partial \overline{u_i}}{\partial x_j} + \frac{\partial \overline{u_j}}{\partial x_i} \right) \right] - \frac{\partial}{\partial x_j} \underbrace{\overline{u_i u_j}}_{\text{Reynolds stress term}}$$

Modeling the Reynolds stress term from time-averaging of 3-D Navier-

Stokes equation, using turbulence models





2. River Hydraulics Shallow Water Hydraulics

Turbulence modeling

Turbulence models

Introducing the concept of turbulent viscosity by Boussinesq approximation

$$-\overline{u_{i}'u_{j}'} = v_{t}\left(\frac{\partial\overline{u_{i}}}{\partial x_{j}} + \frac{\partial\overline{u_{j}}}{\partial x_{i}}\right) + \frac{2}{3}k\delta_{ij}$$

Zero-Equation Model

$$v_t = l_m^{2} \left| \frac{\partial u}{\partial z} \right|$$

Determine mixing length,

No PDE equation to describe

the transport of turbulent

flux

One-Equation Model

$$v_t = c_\mu \sqrt{k}L$$

Determine *k* from

one transport equation

Two-Equation Model

$$v_t = c_{\mu} \frac{k^2}{\varepsilon}$$

Determine k and ε from two transport equations ($k - \varepsilon$ model)

- k-*Ω*, SST, RNG, …





Model Classification

Dimensions of model

- 3-D: DNS, RANS (Time-averaged model)
- 2-D: Depth-averaged or horizontally averaged models
- 1-D: Cross-sectional averaged model

Input & output data

- Deterministic model : Model output fully determined by parameters and input data
- Stochastic model : Parameters and input data leading to randomized output



Analysis method

- Physics-based model : Represents the physical process in the real world
- Data-based model : Estimates the phenomenon based on the acquired data





Model Classification

- 🔋 3D Model
- OpenFOAM
 - C++ based Open Source CFD toolbox
 - Uses Linux OS
 - Calculate PDE with FVM method
 - Supports parallel computing



출처: Mark Schmeeckle, Arizona State Univ.

- EFDC (Environmental Fluid Dynamics Computer code)
 - Developed in 1992 by Virginia Institute of Marine Science
 - Applicable to various surface flows as rivers, lakes, wetlands, estuaries etc
 - Physical model based on Blumberg and Mellor(1987)
 - RANS computation with Boussinesq approximation and hydrostatic pressure





SMS

Model Classification

- 3 2D Model
 - SMS (Surface-water Modeling Solution)
 - Numerical model based on FEM and depth-averaging
 - River flow and transport modeling in rivers, lakes
 - Consists of flow model(RMA2), transport model (RMA4), sediment transport model(FESWMS), particle tracing model (PTM) etc
 - RAMS(River Analysis and Modeling System)
 - Conservative and non-conservative transport modeling, mass injection modeling assuming contaminant accidents
 - Various mixing analysis of river and lake variables such as BOD/DO, Temperature, Algal bloom, etc





Ref: www.aquaveo.com



Ref: Seo, etc(2014) "RAMS tech manual"

Homepage: http://ehlab.snu.ac.kr



3. River Models RAMS (River Analysis and Modeling Systems)

RAMS Software

- Able to simulate physical phenomena in natural rivers with complex topography by 2D finite element calculations
- RAMS consists of river flow model (HDM-2D), pollutant transport model (CTM-2D), particle dispersion model (PDM-2D)
- Graphic User Interface is combined with computing engines
- Increased accuracy for the pollutant transport model with dispersion linked with flow direction and various pollutant input
- Web: http://ehlab.snu.ac.kr
- E-mail: seoilwon@snu.ac.kr









RAMS program consists of a 2D flow analysis model and a pollutant transport model that is combined with a GUI for user convenience



RAMS

Governing eq. of HDM-2D

Continuity eq. :
$$\frac{\partial h}{\partial t} + h \frac{\partial u_j}{\partial x_j} + u_j \frac{\partial h}{\partial x_j} = 0$$

Momentum eq. : $\frac{\partial u_i}{\partial t} + u_j \frac{\partial u_i}{\partial x_j} = -g \frac{\partial H}{\partial x_i} - g \frac{\partial h}{\partial x_i} + v_T \frac{\partial^2 u_i}{\partial x_j \partial x_j} - g n^2 \frac{u_i \sqrt{u_j u_j}}{h^{4/3}} - \frac{\partial S_{ij}}{\partial x_j}$

Governing eq. of CTM-2D

$$\frac{\partial(h\overline{C})}{\partial t} + \frac{\partial\left(\overline{u}_{i}h\overline{C}\right)}{\partial x_{i}} = \frac{\partial}{\partial x_{i}}\left(hD_{ij}\frac{\partial\overline{C}}{\partial x_{j}}\right) + Q + kh\overline{C}$$

Governing eq. of PDM-2D





Model Classification

Two dimensional model

- iRIC (international River Interface Cooperative)
 - GUI interface software package for flow and sediment transport models developed by Hokkaido University and United States Geological Survey
 - Consists of pre-processor, post-processor, and model





Model Classification

🔋 1D Model

Hydrodynamic model – 1 dimensional Saint Venant equation

$$\frac{1}{A}\frac{\partial Q}{\partial t} + \frac{1}{A}\frac{\partial}{\partial x}\left(\frac{Q^2}{A}\right) + g\frac{\partial h}{\partial x} - g\left(S_0 - S_f\right) = 0$$

Transport model – 1 dimensional advection-transport equation

$$\frac{\partial C}{\partial t} + U \frac{\partial C}{\partial x} = \frac{\partial}{\partial x} \left(K \frac{\partial C}{\partial x} \right)$$

Model	Developer	Characteristics
HEC-RAS	US Army Corps of Engineers	 Used worldwide in many institutions Capable of assessment of various riverine structures
SWMM	US EPA	 Developed for urban rainfall runoff analysis Hydrologic characteristics applied to rainfall events, specialized for water distribution network design
MIKE 11	DHI	 Commercial software model for flood modeling User friendly GUI with various hydraulic / advection models







4. River Modeling -RAMS application-Flow modeling in confluent channel

Confluent channel modeling boundary conditions

Flow characteristics (Weber etc, 2001)



HDM-2D boundary conditions

$Q_{\rm m}~({\rm m^{3/s}})$	0.043
$Q_{\rm b}~({\rm m^{3/s}})$	0.127
<i>h</i> (m)	0.296
<i>B</i> (m)	0.914
U_{∞} (m/s)	0.628
Fr	0.37



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Flow modeling in confluent channel

HDM-2D numerical modeling results



4. River Modeling - RAMS application -Flow modeling in confluent channel

Separation zone changes with application of dispersion stress







4. River Modeling - RAMS application -Flow modeling in meandering channel





Case	U.B.C. (cms)	D.B.C. (m)	V _{xx} (m²/s)	V _{xy} (m²/s)	V _{yy} (m²/s)	<i>n</i> (m ^{-1/3} s)
M1	0.00	0.15		0.040		
M2	0.03	0.40		0.013		





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Flow modeling results in meandering channel

HDM-2D model results



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Transport modeling results in meandering channel



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Tracer tests in the meandering channel

Results of PDM-2D







Andong River Experiment Center

Simulation conditions



No. of elements: 5565 No. of nodes: 5852 No. of elements: 6846 No. of nodes: 7194 No. of elements: 8316 No. of nodes: 8734





Andong River Experiment Center



4. River Modeling - RAMS application -Andong River Experiment Center

Simulation results of PDM-2D

Case AMC12
 0.5 2.4 4.3 6.2 8.1 10.0
 Case AMC15
 Case AMC15
 Case AMC17



2 Calculation results of D_T with sinuosity change



Rutherford (1994) - $D_T/Hu^* = 0.30 \sim 0.90$, for meandering channels

Case	AMC12	AMC15	AMC17
D_{T}/hu^*	0.67	0.73	0.83
Sinuosity	1.2	1.5	1.7





4. River Modeling - RAMS application -Sum River two dimensional tracer experiment modeling

Sum River tracer test

Test outline

Rhodamine WT 20% solution 1900 mL(20,000 ppm) injection





Simulation condition

Model	HDM-2D			Model HDM-2D CTM-2D			1-2D
Variable	Q (m ³ /s)	<i>h</i> (m)	$D_{\rm L}~({\rm m2/s})$	$D_{\mathrm{T}} (\mathrm{m2/s})$			
Value	5.9	63.2	0.03	0.84	0.019		





Sum River two dimensional tracer experiment modeling



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Sum River two dimensional tracer experiment modeling



Hongcheon River

Simulation conditions

No. of Node : 8162 No. of Element : 7770 Wall boundary condition: no slip Inflow vel. profile : parabolic distribution







Hongcheon River



Hongcheon River

Simulation results of PDM-2D







4. River Modeling - RAMS application -Pollutant mixing in the Han River













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Upstream of Jamsil submerged weir : BOD scenario simulation

Concentration mixing results



Downstream of Jamsil submerged weir : BOD scenario simulation

Flow and transport concentration simulation condition







Downstream of Jamsil submerged weir : BOD scenario simulation

Concentration simulation results







Downstream of Jamsil submerged weir : Phenol scenario simulation

Simulation of conservative pollutant mixing using PDM-2D

Flow conditions (HDM-2D simulation results)



<i>Q</i> (m ³ /s)		Dollutant		No. of	
Han River	Jurang Creek	Anyang Creek		iviass (ky)	particles
183.9	1.4	2.2	Phenol	1,000	10,000





Downstream of Jamsil submerged weir : Phenol scenario simulation

Simulation results using PDM-2D







4. River Modeling - RAMS application -Nakdong River : Conservative pollutant mixing

Simulation conditions



Field tracer test conducted at downstream of confluence2 tributaries are merging from left side of Nakdong River



4. River Modeling - RAMS application -Nakdong River : Conservative pollutant mixing

Simulation results using CTM-2D

Model calibrations with changing $D_{\rm T}$



Concentration distribution



- Initial field of confluence (Sec.1) showed high conductivity value in left
- As cloud moving further downstream, conductivity gradient decreased



Diatom Prediction

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Diatom bloom in the Nakdong River, South Korea

- Diatom blooms in spring and winter to impact on water quality deterioration
- Model calibration and validation using daily observation data



Continuous injection on unsteady regime

Daily concentration and discharge used for initial and boundary condition



Scalar : Constituent(ppm) Vector: None Time step : 16.000000

Scalar

22.00000





Spatial distribution of diatom bloom at steady state

Diatom Prediction







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Unsteady simulation with pulse discharge: scenario PD1

Discharge 200 m³/s from Ganjeong weir 3 times (each for 8 hours) during 2 days







Diatom Prediction

Unsteady simulation with pulse discharge: scenario PD2

Discharge 200 m³/s from Ganjeong weir 6 times (each for 4 hours) during 2 days







Unsteady simulation with pulse discharge: scenario PD3

Discharge 200 m³/s from Ganjeong weir 12 times (each for 2 hours) during 2 days







Diatom Prediction









Diatom Prediction

Unsteady simulation with pulse discharge: scenario PD4

Discharge 200 m³/s from Ganjeong weir 6 times (each for 2 hours) during 2 days







4. River Modeling

- EFDC Application-

Nakdong River Buoyant Contaminant Mixing Modeling



EFDC simulation results

Case	Q (m ³ /s)	<i>h</i> (m)	$\frac{K_{\rm H}}{({\rm m}^2/{\rm s})}$	Wind (m/s)	No. of layer	No. of particles
GF11	547	6.0	0.027	0.15	10	35
GF12	681	7.1	0.007	0.50	10	24
GF13	697	8.5	0.002	0.50	10	30





4. River Modeling

- EFDC Application-

Nakdong River Buoyant Contaminant Mixing Modeling

Comparison of particle dispersion





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Water pollution accidents in the Nakdong River



Water pollution accidents in the Nakdong River

Case GSO

Oistance for transverse mixing completion

$$L = 0.4U \frac{W^2}{\varepsilon_t} = 0.4 \times 0.02 \times \frac{200^2}{0.1} = 3.2 \text{ km}$$



Simulation results

Water Column

[Time 0.104]

Dye (mg/l) Depth Averaged



Water pollution accidents in the Nakdong River

Particle distributions



- C_p of Case NGC is higher than Case NGO at the left bank
- More particles were accumulated near the

pumping station when the gate was closed

₃ *t* = 32 hr





4. River Modeling - EFDC Application-Nakdong River EC Mixing Modeling

- Nakdong EC tracer test result comparison
 - Outline

Field experiment date: 2014.05 ~ 2014.11





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Nakdong River EC Mixing Modeling



4. River Modeling 69/70 - EFDC Application-Nakdong River EC Mixing Modeling (y/W=0.1) vertical mixing Continuous input results concentration simulation results Legend 17.50 Col: I = 22, Time: 0.458 Dye (mg/l) 400 700 15.00 Elevation (m) 10.00

7.50

5.00

2.50

Water Column 300 [Time 0.083] 1031 Dye (mg/l) Depth Averaged 1.00 (m/s)

Flow 12000 13000 14000 15000 Longitudinal distance (m)





16000

Nakdong River EC Mixing Modeling

Flow velocity modeling comparison



EC lateral mixing comparison





