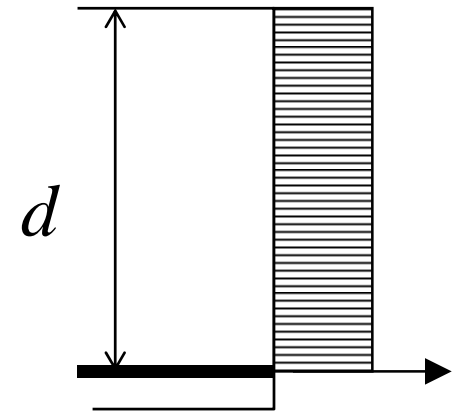
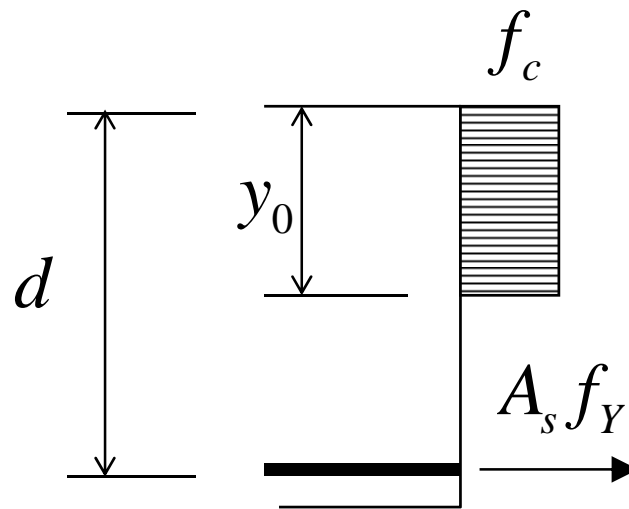
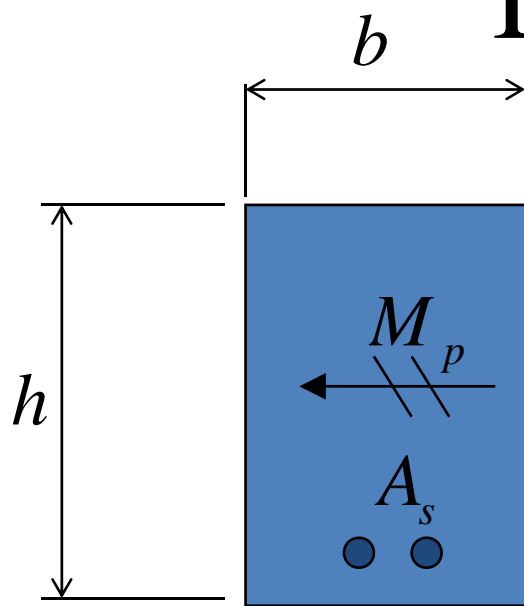


# Chap. 5 Beams

- Beams in Bending
- Beams in Shear
  - Transverse reinforcement
  - Without transverse reinforcement
  - Effective Concrete Compressive Strength
  - Arch Actions
  - Design
  - With Normal Forces
- Beams in Torsion

# Beams in Bending



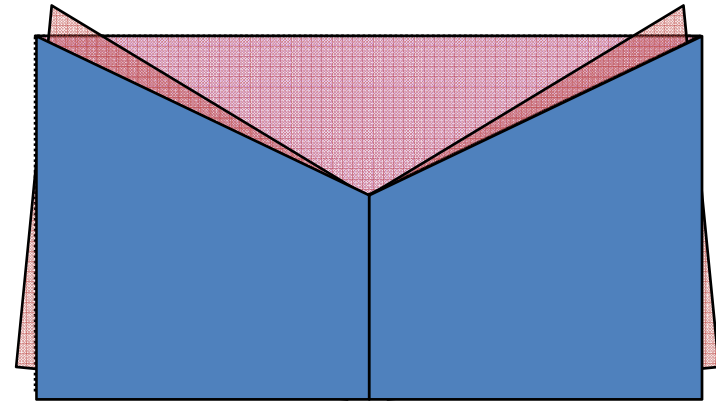
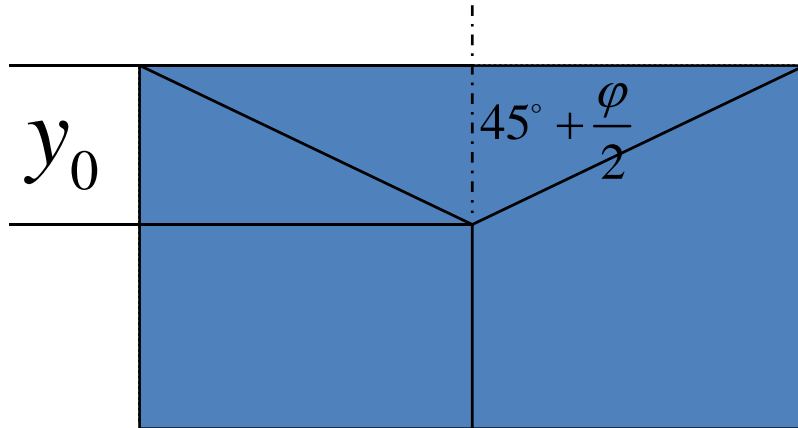
$$A_s f_Y = y_0 b f_c$$

$$\frac{y_0}{d} = \Phi$$

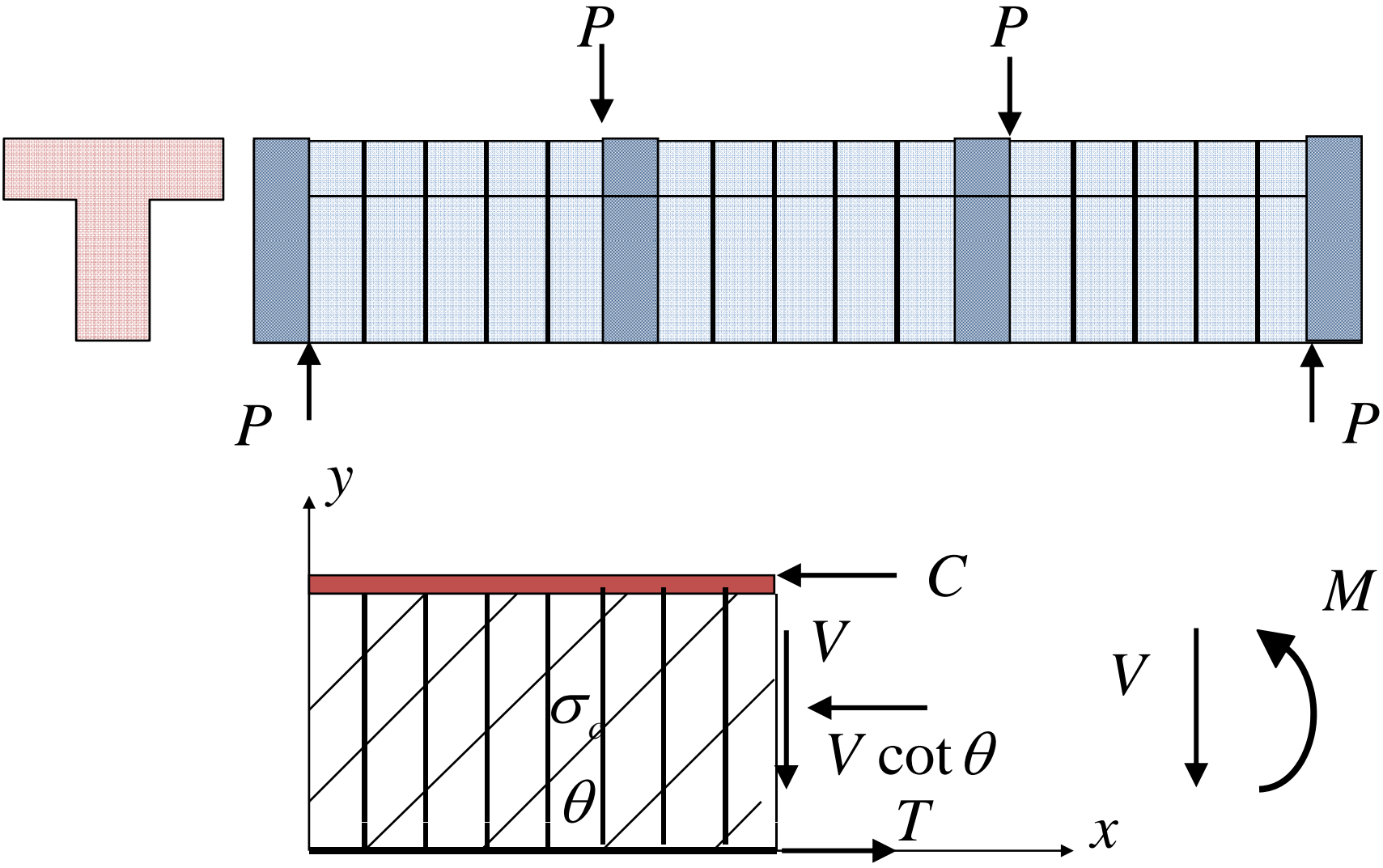
$$M_p = \left(1 - \frac{1}{2} \Phi\right) \Phi b d^2 f_c$$

$$M_p = b d^2 f_c$$

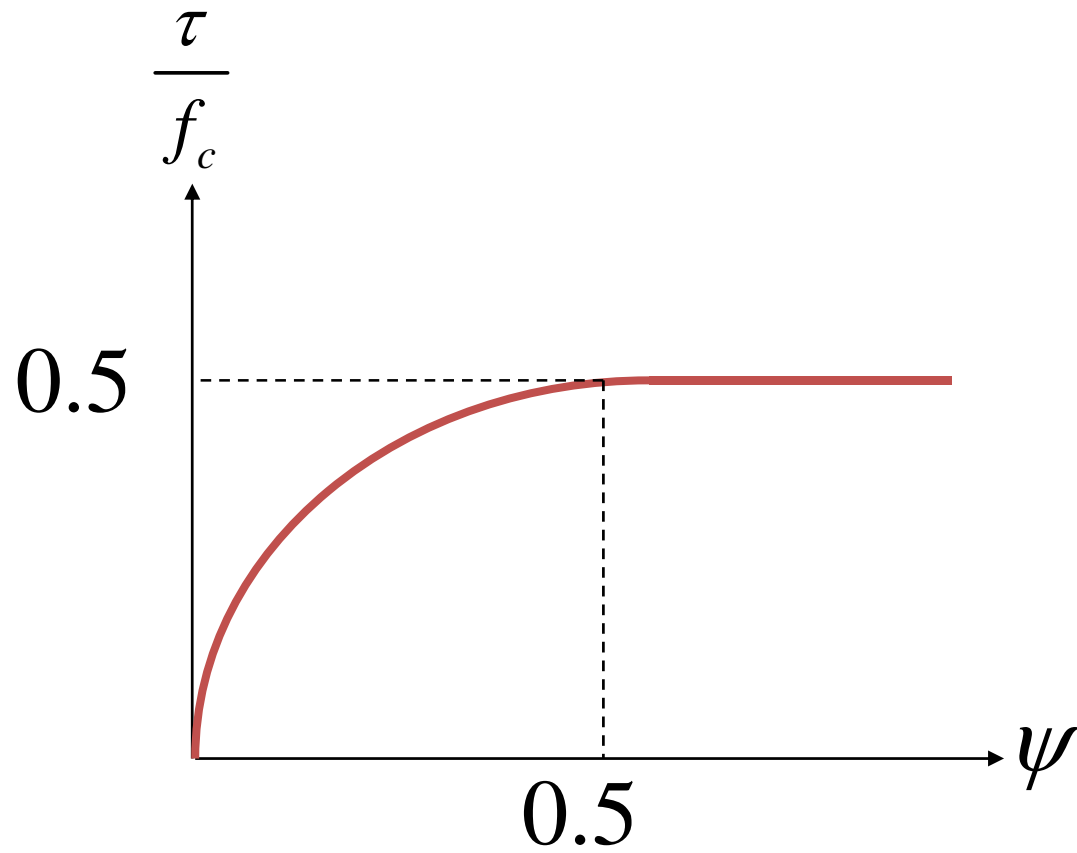
# Failure Mechanism in Bending



# Beams in Shear

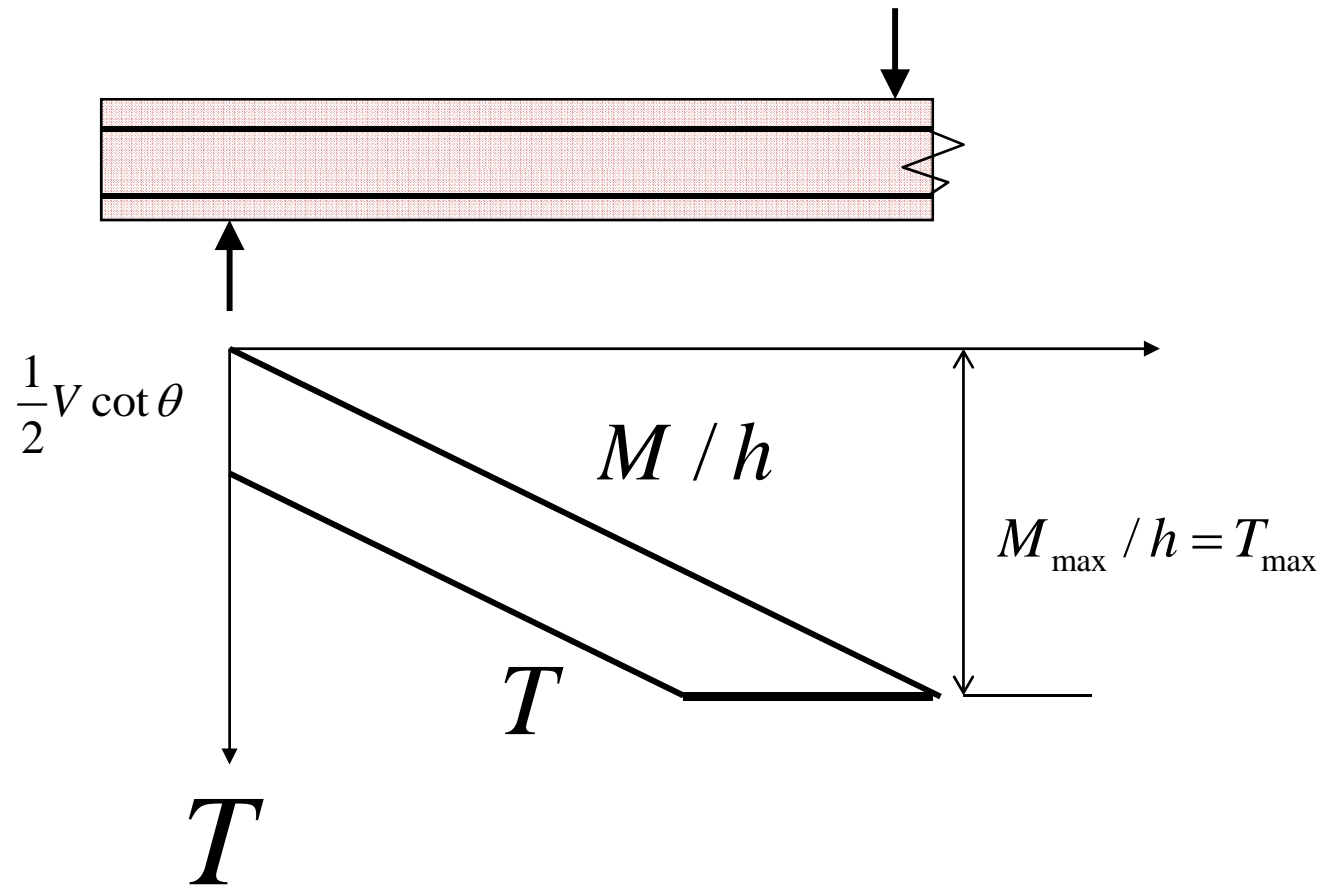


# Lower Bound Solution

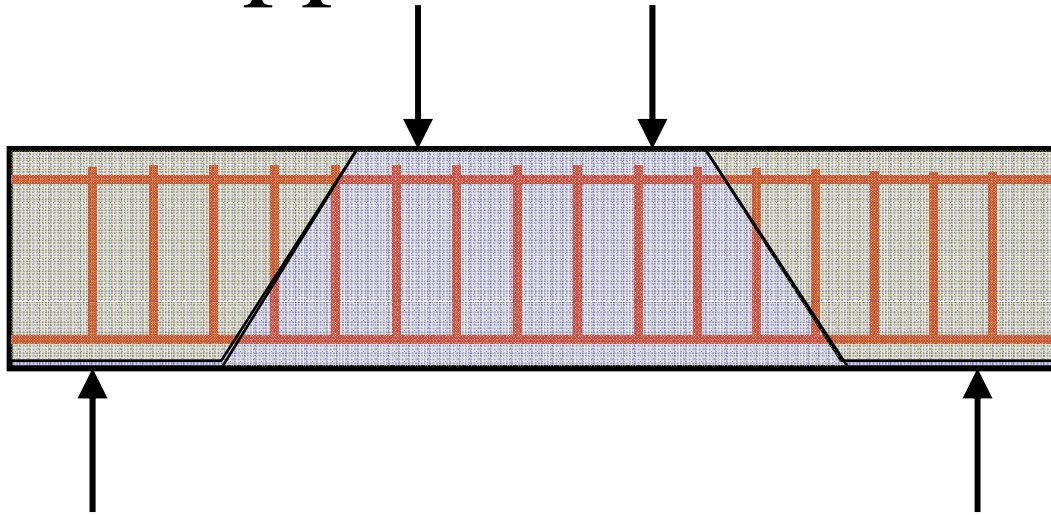


$$\frac{\tau}{f_c} = \begin{cases} \sqrt{\psi(1-\psi)} \\ \frac{1}{2} \end{cases}$$

# Shift in Tension Force in Stringer



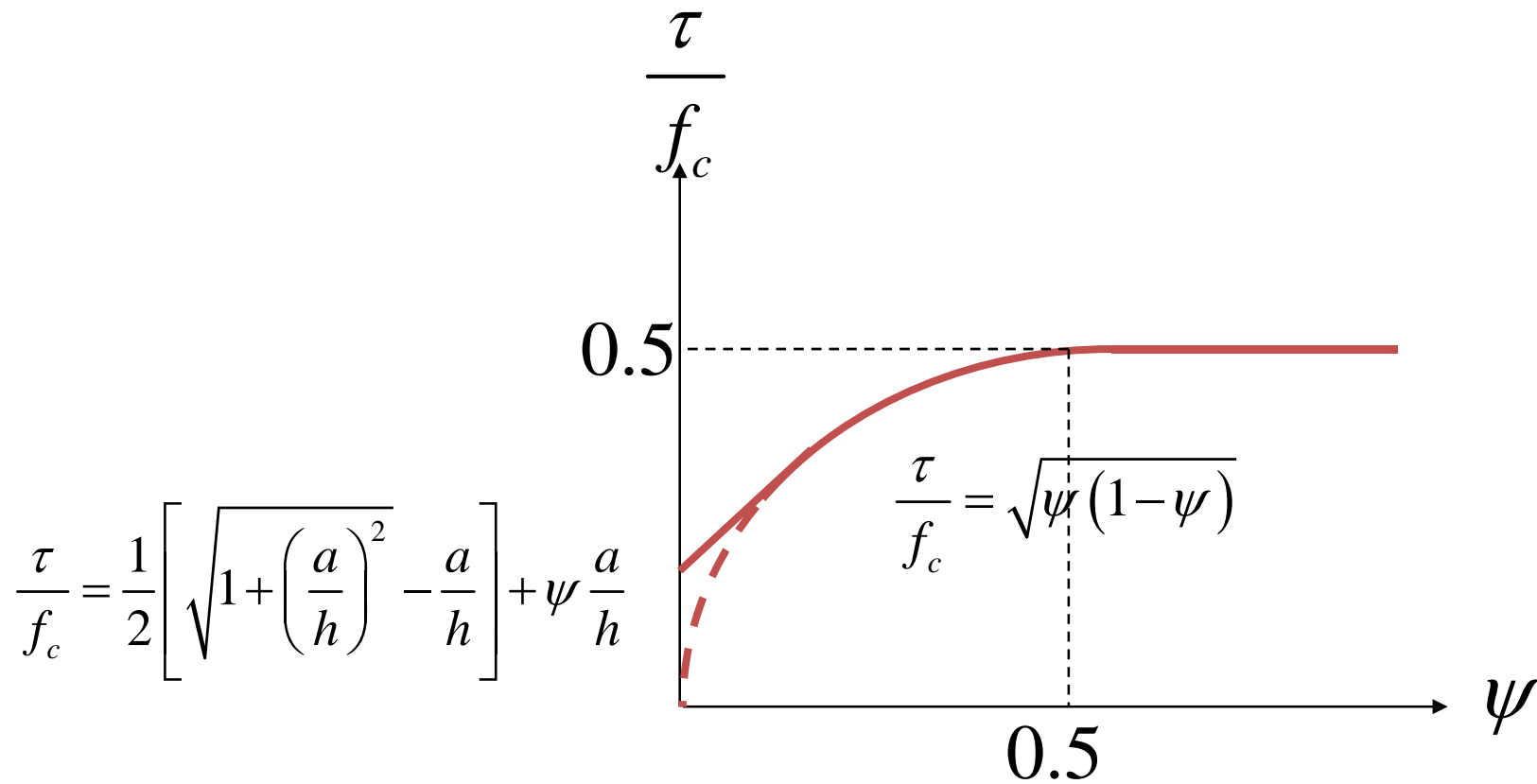
# Upper Bound Solution



$$\beta = 2\theta \quad \tan \theta = \sqrt{\frac{\psi}{1-\psi}}$$

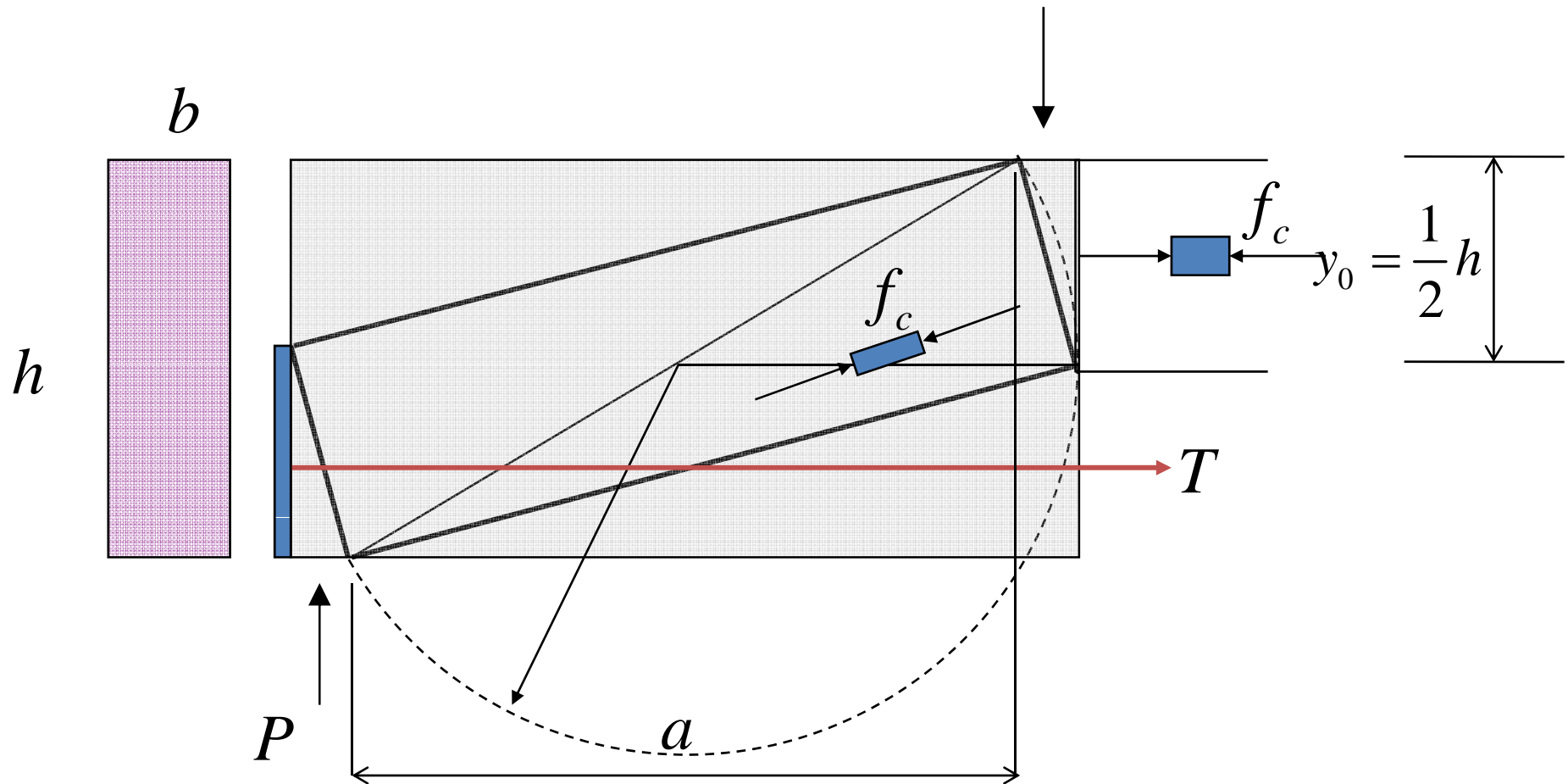
$$\frac{\tau}{f_c} = \frac{1}{2} \left[ \sqrt{1 + \left(\frac{a}{h}\right)^2} - \frac{a}{h} \right] + \psi \frac{a}{h}$$

# Upper Bound Solutions

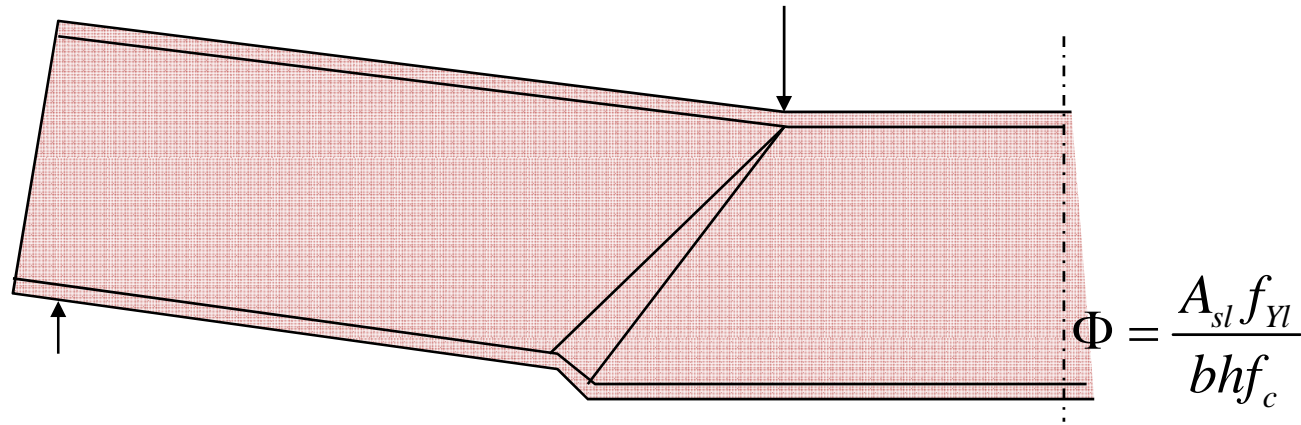




# Shear Capacity without Shear Reinforcement



# Influence of Longitudinal Reinforcement on Shear Capacity



$$T_Y = \frac{Pa}{h} + \frac{1}{2} P \cot \theta$$

$$\tau = \frac{P}{bh} = r f_{Yw} \cot \theta$$

$$\frac{\tau}{f_c} = \psi \left[ \sqrt{\frac{2\Phi}{\psi} + \left(\frac{a}{h}\right)^2} - \frac{a}{h} \right]$$